

MR790676 (87j:57014) 57R30**Ghys, Étienne (F-LILL)****Une variété qui n'est pas une feuille. (French) [A manifold that is not a leaf]***Topology* **24** (1985), *no. 1*, 67–73.

The author gives a clever construction of a noncompact, connected n -manifold L , $n \geq 3$, that cannot be homeomorphic to a leaf in any compact, C^0 -foliated $(n+1)$ -manifold. In this construction, L has one end and, as this end is approached, a generator of p -torsion in $\pi_1(L)$ appears for each successive prime p . Roughly, the idea is to show that L , if a leaf, would be asymptotic to a leaf having intrinsically contradictory topology.

It should be remarked that a similar construction has been given by T. Inaba et al. [*Kodai Math. J.* **8** (1985), no. 1, 112–119; [MR0776712 \(86f:57024\)](#)]. They assumed C^2 smoothness, which makes the asymptotic behavior of L much easier to manage. Finally, if $n = 2$, the case left open in these papers, the exact opposite is true. All orientable surfaces can be leaves in suitable C^∞ foliations of all closed 3-manifolds and all nonorientable surfaces in all closed, nonorientable 3-manifolds [J. Cantwell and the reviewer, “Every surface is a leaf”, *Topology*, to appear].

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