

# ENTANGLEMENT PROPERTIES OF LATTICE BOSONS FROM A VARIATIONAL WAVE FUNCTION

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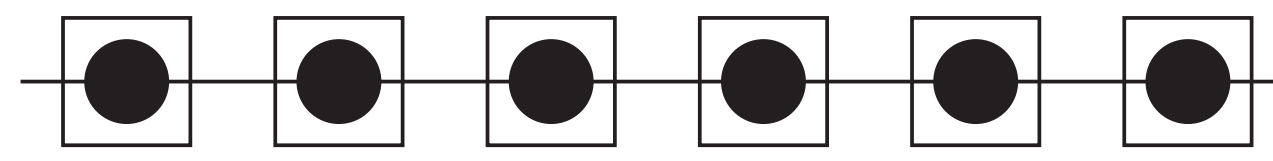
## INTRODUCTION

State of a  $N$ -spin  $\frac{1}{2}$  system:  $|\psi\rangle = \sum_{\vec{\sigma}} C(\vec{\sigma}) |\vec{\sigma}\rangle$   
 $\rightarrow 2^N$  variables

Through gradient algorithm, find  $|\psi\rangle$  which minimizes  $\langle\psi|H|\psi\rangle$ , with the assumption

$$|\psi\rangle = \sum_{\vec{\sigma}} \left( \prod_P C_P(\vec{\sigma}_P) \right) |\vec{\sigma}\rangle$$

## EPS ALGORITHM

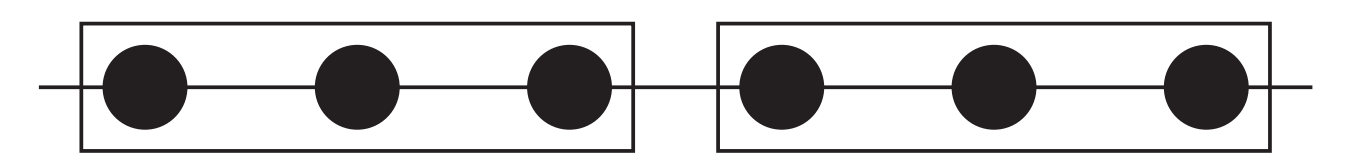


Mean field

$\rightarrow 2N$  variables

But:

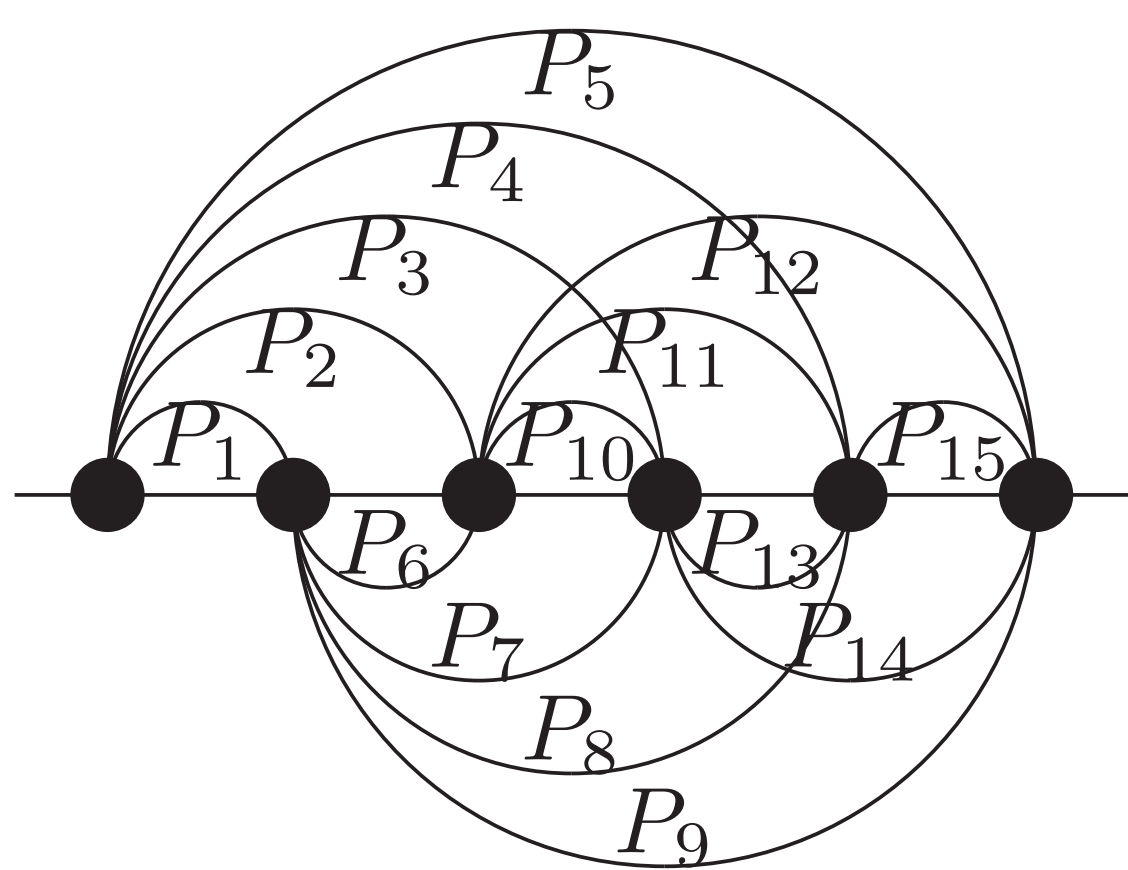
$$\langle S_i^z S_j^z \rangle - \langle S_i^z \rangle \langle S_j^z \rangle = \begin{cases} \frac{1}{4} - \langle S_i^z \rangle^2 & \text{if } i = j \\ 0 & \text{if not} \end{cases}$$



EPS with plaquettes of size 3

$\rightarrow 2^3 N$  variables

## EPS DELOCALIZED



EPS with delocalized plaquettes of size 2

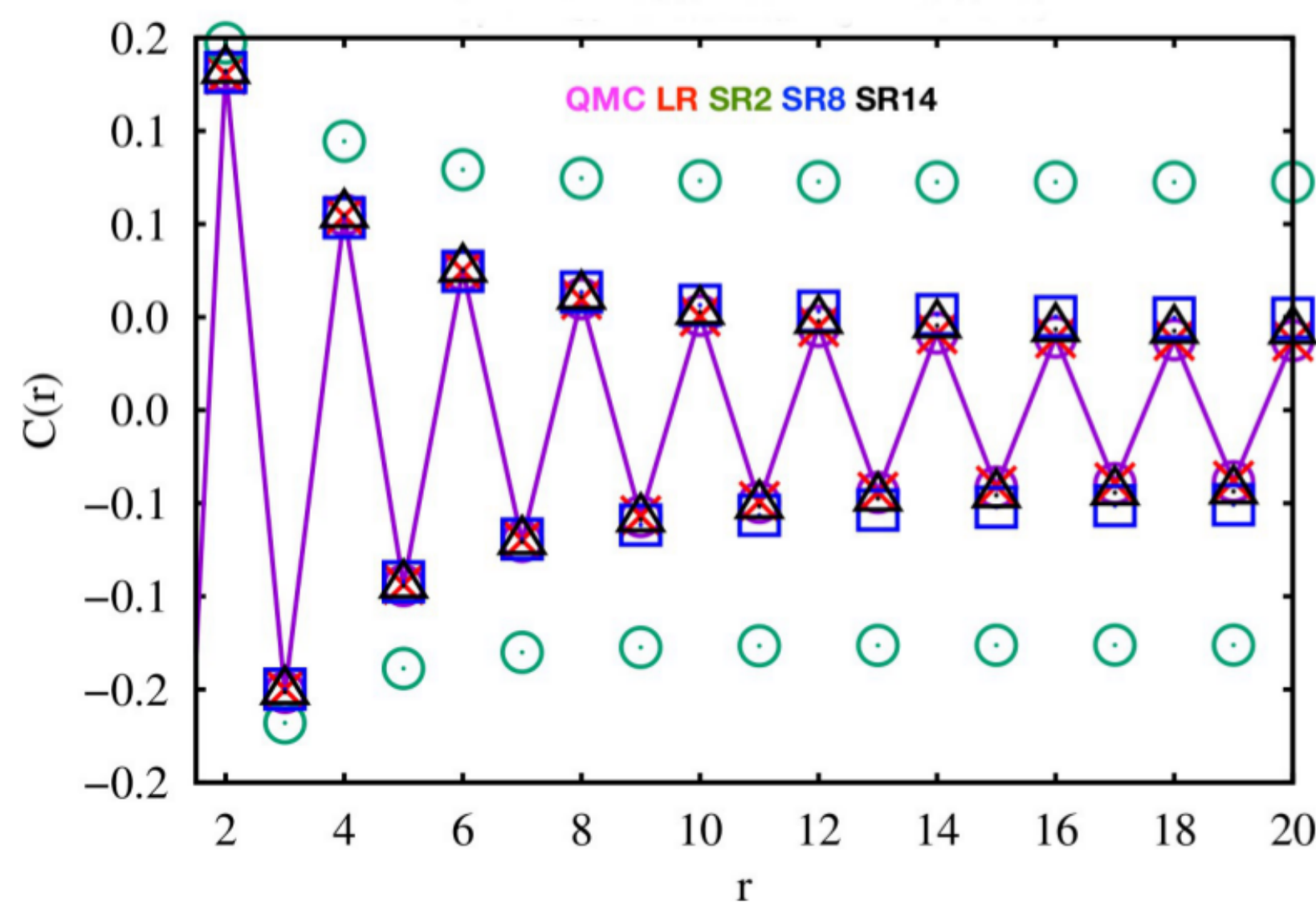
$\rightarrow N^2$  variables

Reduced with considerations on symmetries.

$\propto N$  variables

## HEISENBERG CHAIN

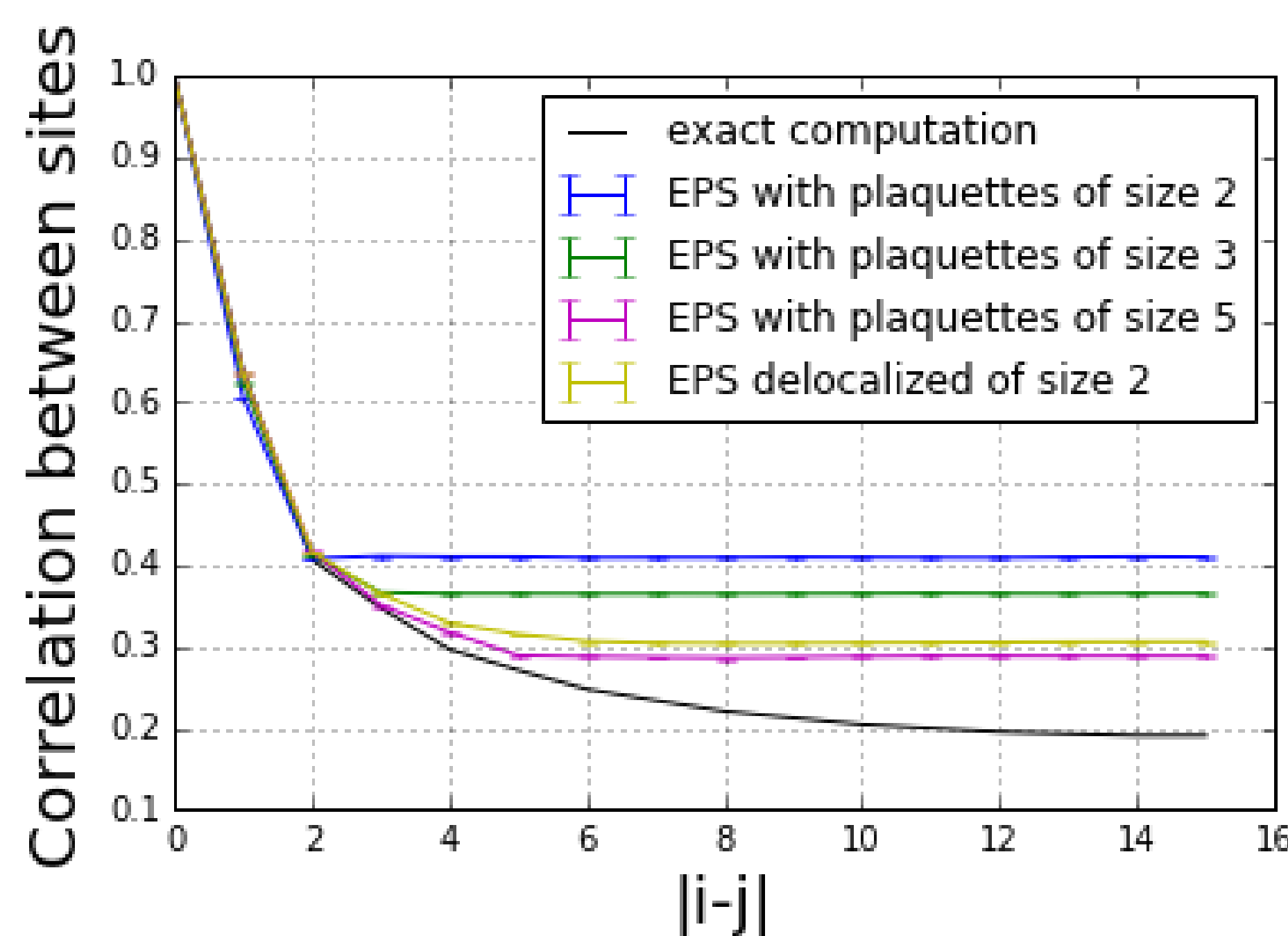
$$H = J_1 \sum_i \vec{S}_i \cdot \vec{S}_{i+1}$$



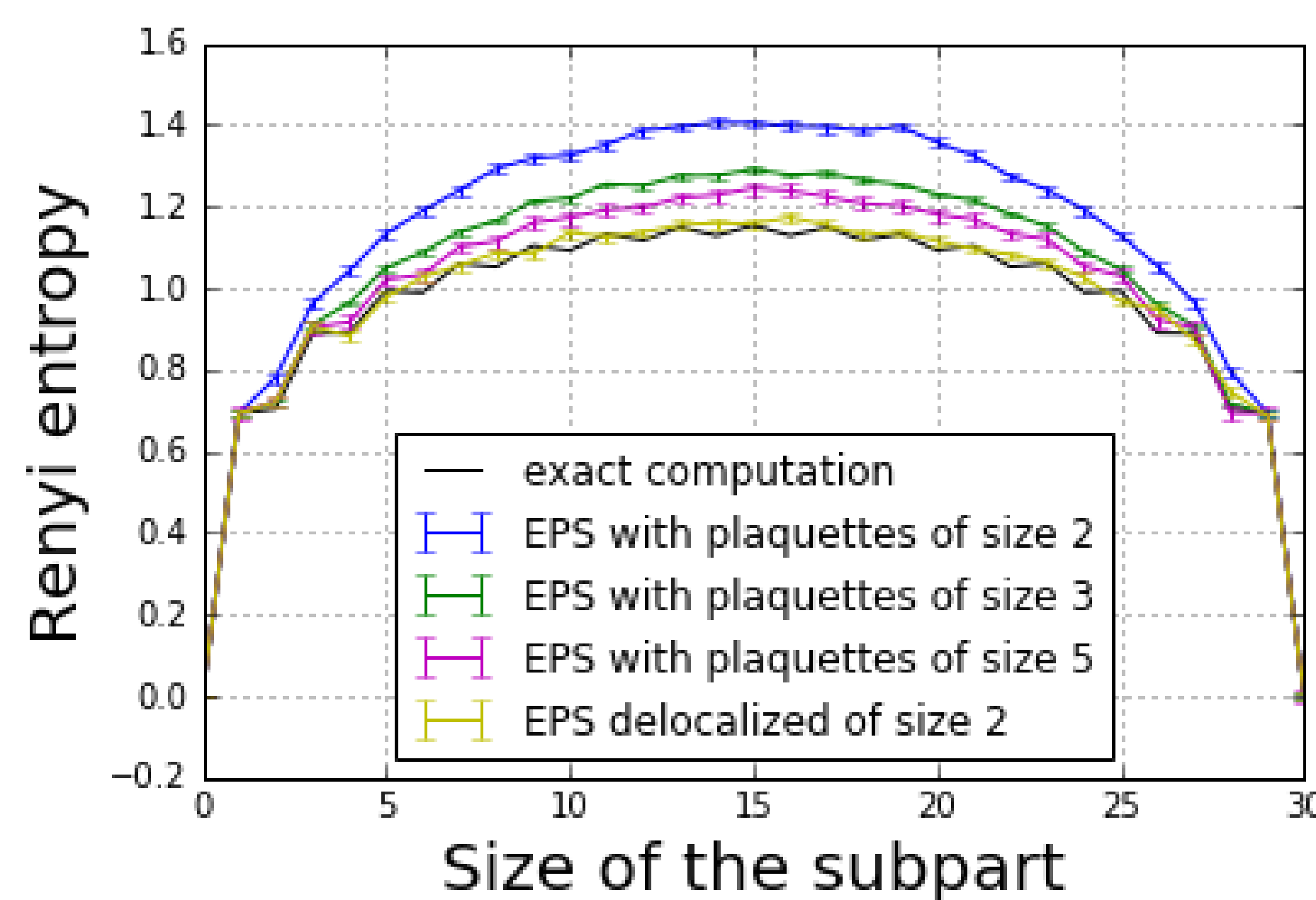
Correlation function between sites  $i$  and  $j$  of a system of size 40

## XX-CHAIN

$$H = J \sum_i (S_{i+1}^x S_i^x + S_{i+1}^y S_i^y)$$



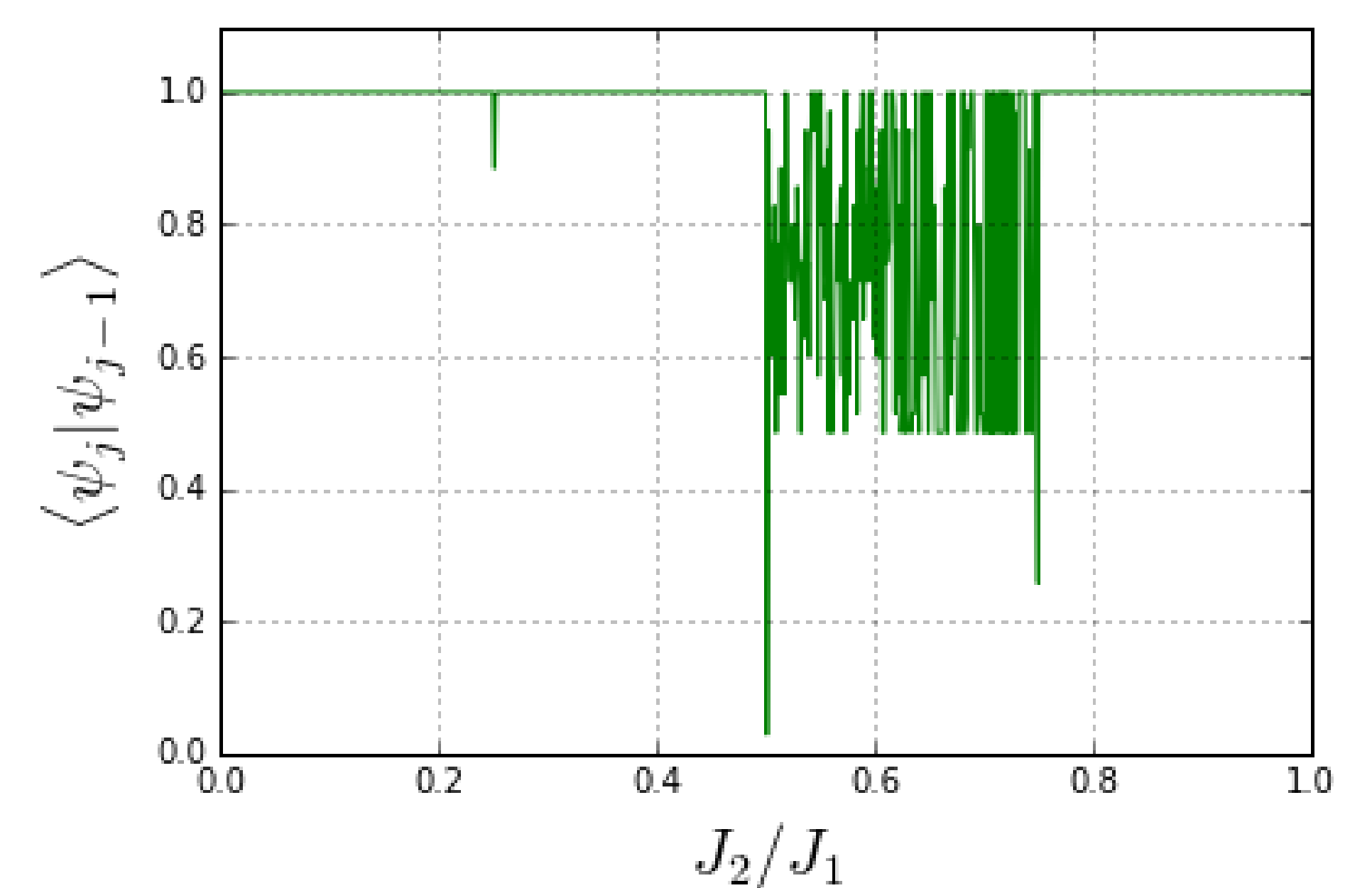
Correlation function along x axis between sites  $i$  and  $j$  of a system of size 30



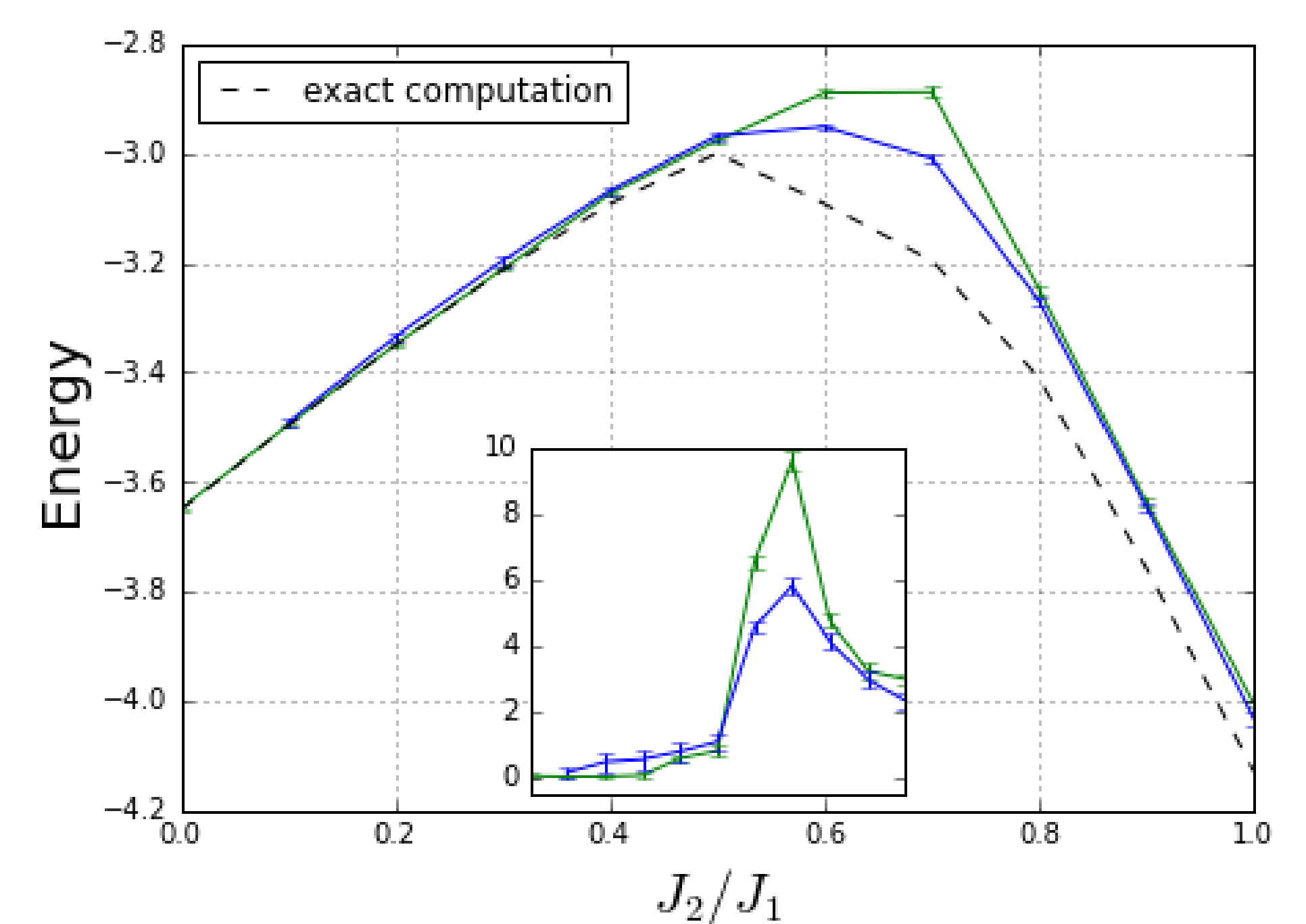
Entanglement entropy as a function of the size of the subsystem of a system of size 30

## $J_1 J_2$ CHAIN

$$H = J_1 \sum_i \vec{S}_i \cdot \vec{S}_{i+1} + J_2 \sum_i \vec{S}_i \cdot \vec{S}_{i+2}$$



Sign structure



Energy as a function of the parameter  $J_2/J_1$

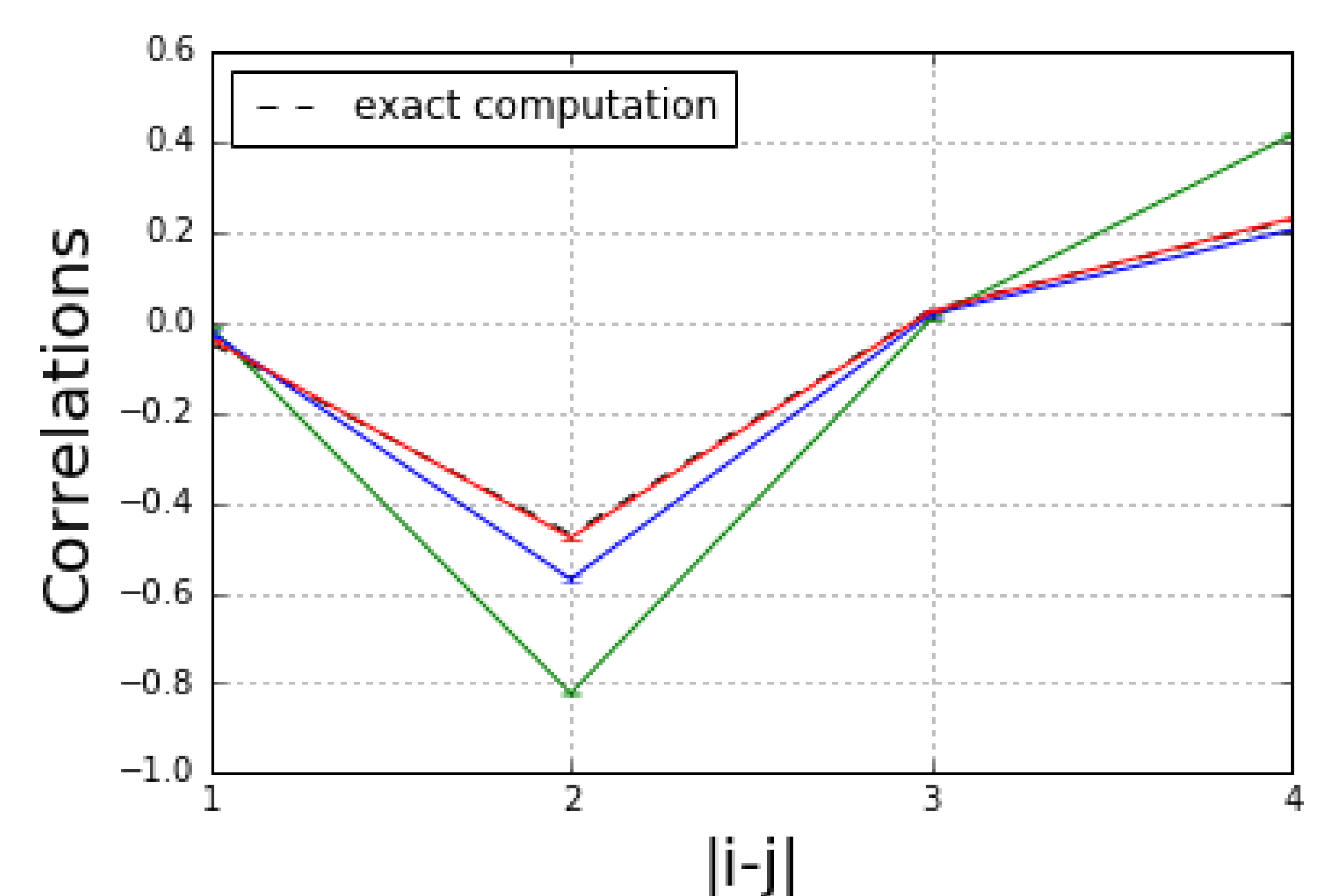
## CONCLUSION

- EPS algorithm with short range plaquettes reproduces well short range correlations but fails to reproduce long range
- EPS algorithm with delocalized plaquettes better reproduces the overall shape of the curve, but costs more calculation time.  
Using symmetries seems to be a good compromise, but how to choose the symmetries we consider in the Ansatz ?
- The sign structure influences the convergence of the algorithm.
- Is it possible to find the sign structure of a system with this algorithm ?

## REFERENCES

- $\rightarrow$  F. Mezzacapo, N. Schuch, M. Boninsegni and J.I. Cirac, "Ground-state properties of quantum many-body systems: entangled-plaquette states and variational Monte Carlo", *New journal of Physics*, **11**(2009).
- $\rightarrow$  M.E.J. Newman, G.T. Barkema, *Monte Carlo Methods in Statistical Physics*, Oxford University Press (1999).

## CORRELATIONS WITH $J_2 = J_1$



Correlation function between sites  $i$  and  $j$  of a system of size 8