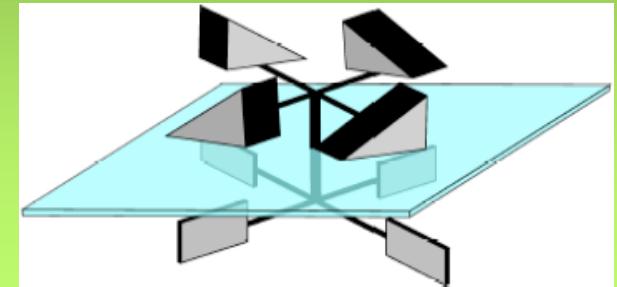


From Maxwell demon to Brownian refrigerator



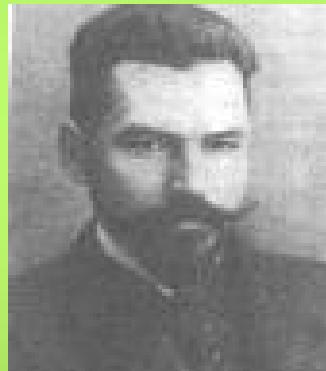
Christian Van den Broeck
christian.vandenbroeck@uhasselt.be

universiteit
▶▶ hasselt



James Clark Maxwell.

Maxwell demon
Maxwell
Theory of Heat 1871

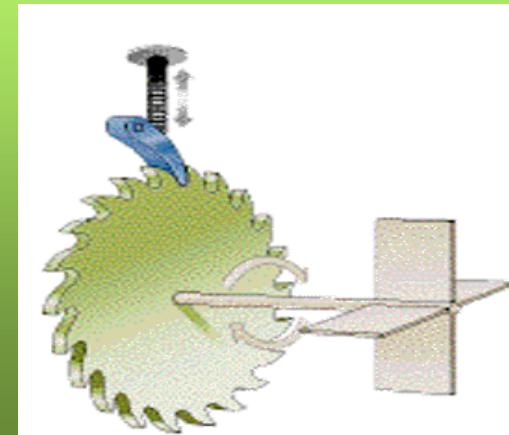


Smoluchowski
Munster 1912

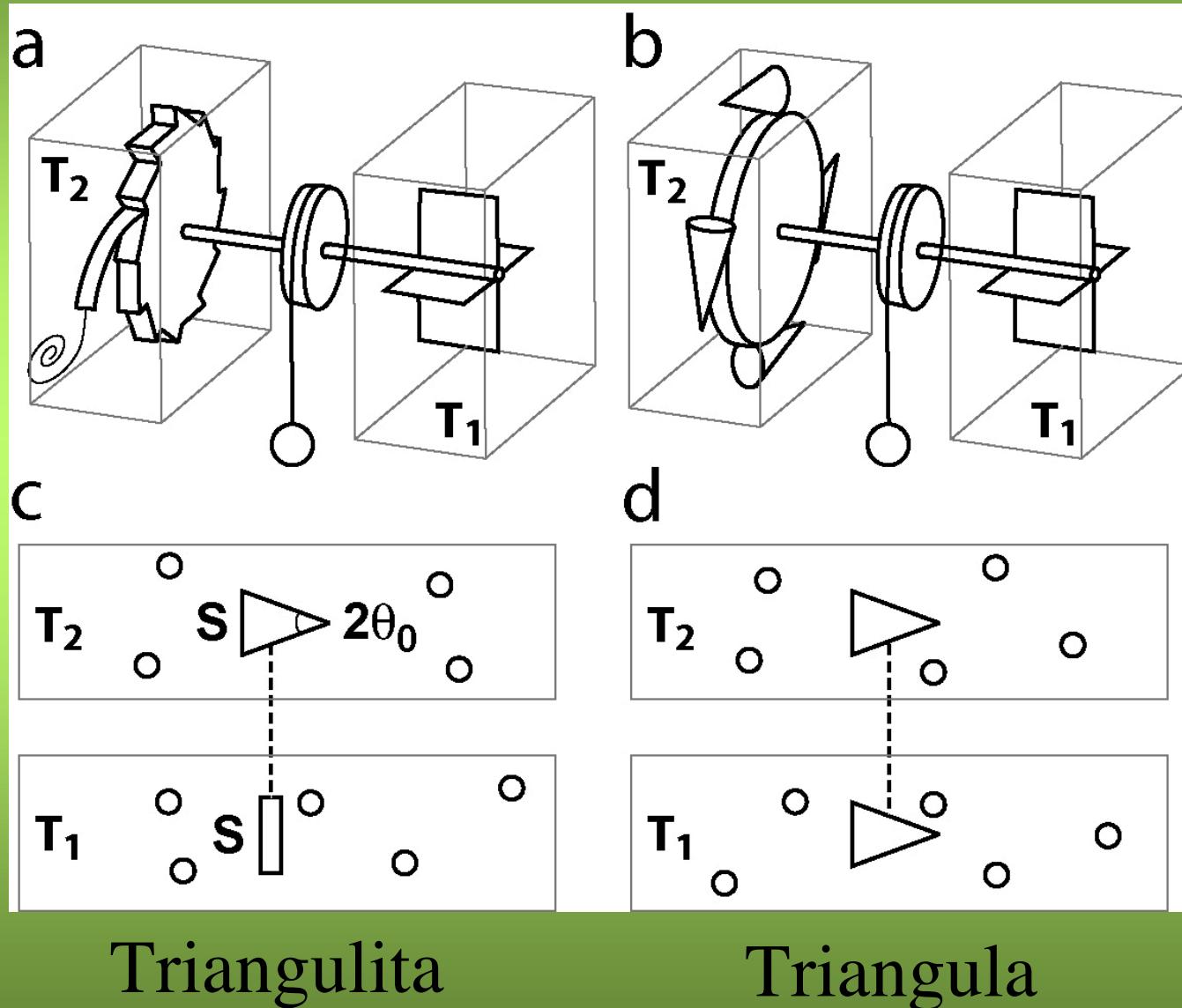
es mit einem kleinen, einseitig wirkenden Ventil
ein Zahnrad mit einer Sperrklinke



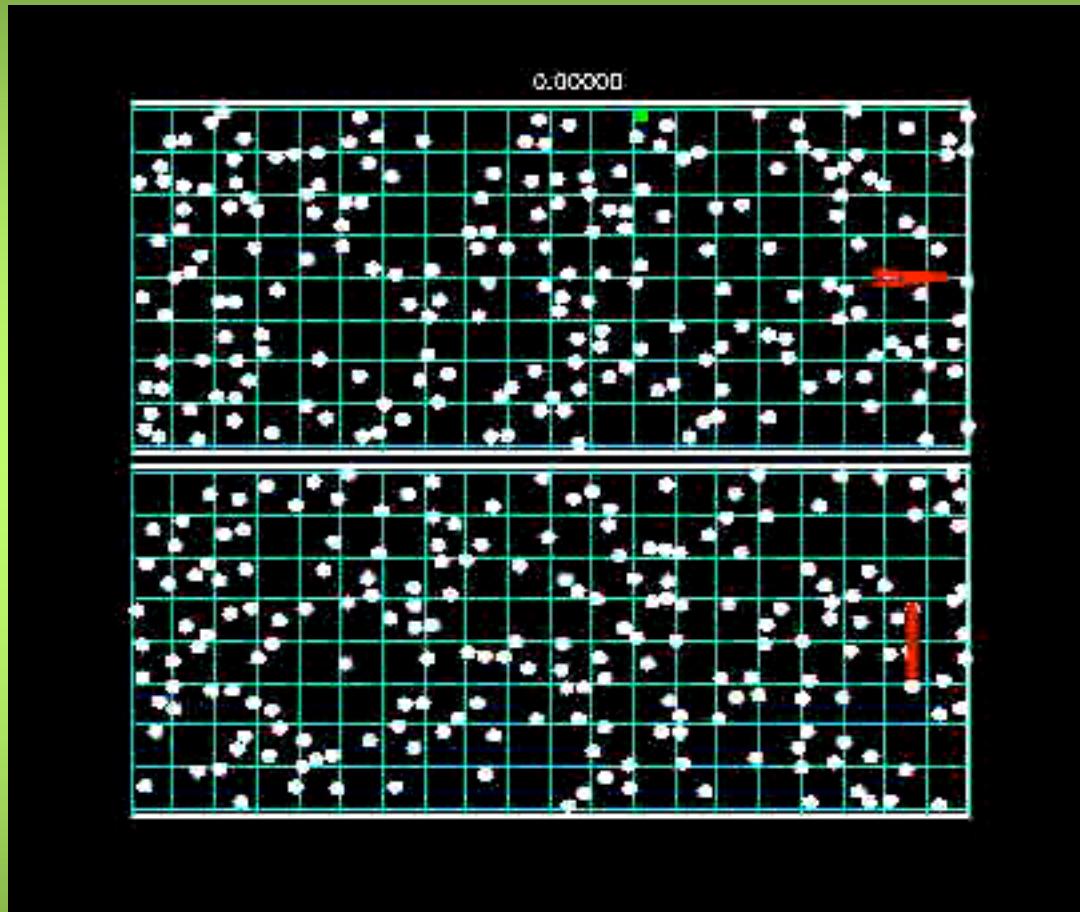
Feynman
Caltech 1961



Simplified Feynman Smoluchowski ratchet

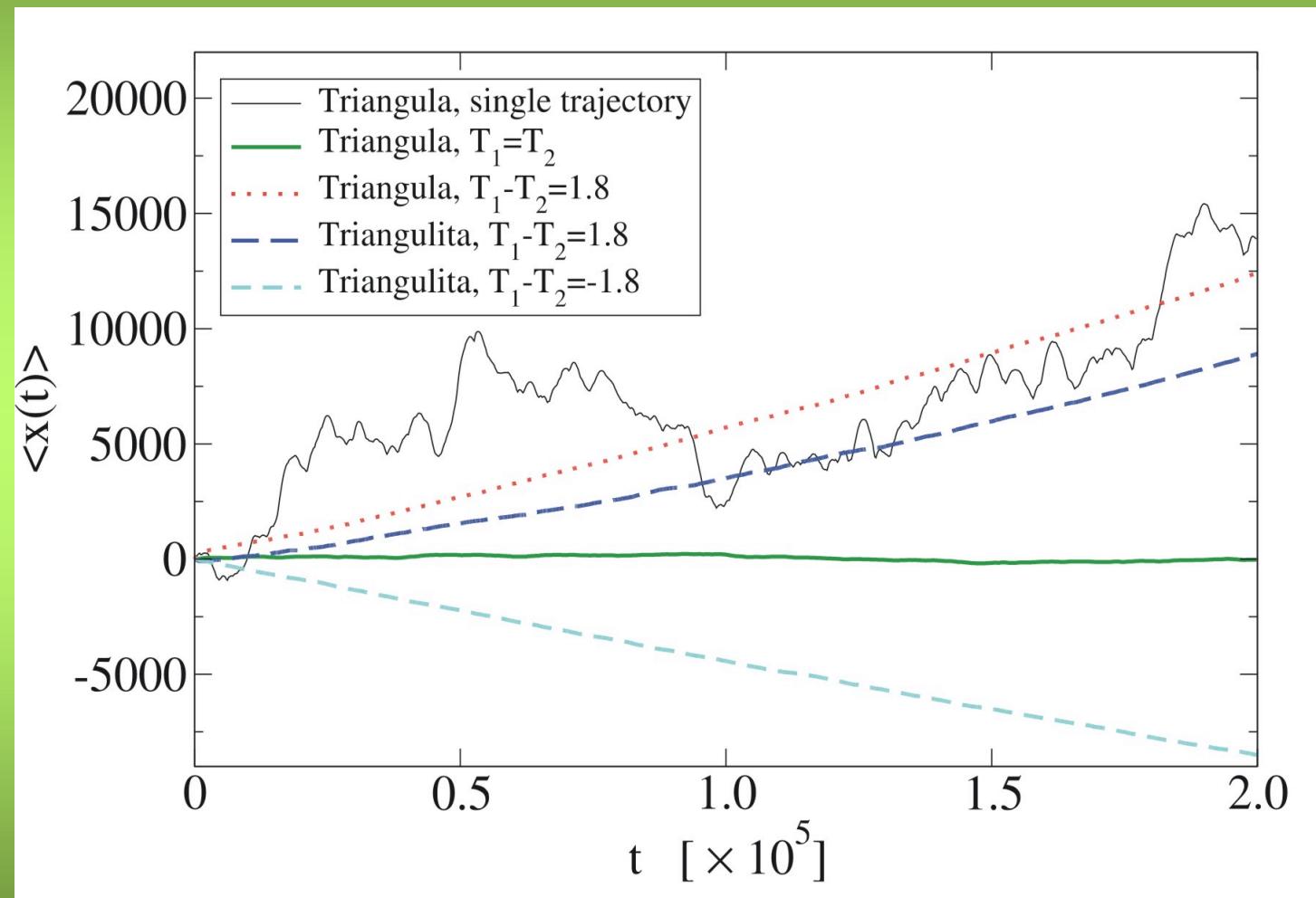


Triangulita molecular dynamics



Triangula and Triangulita

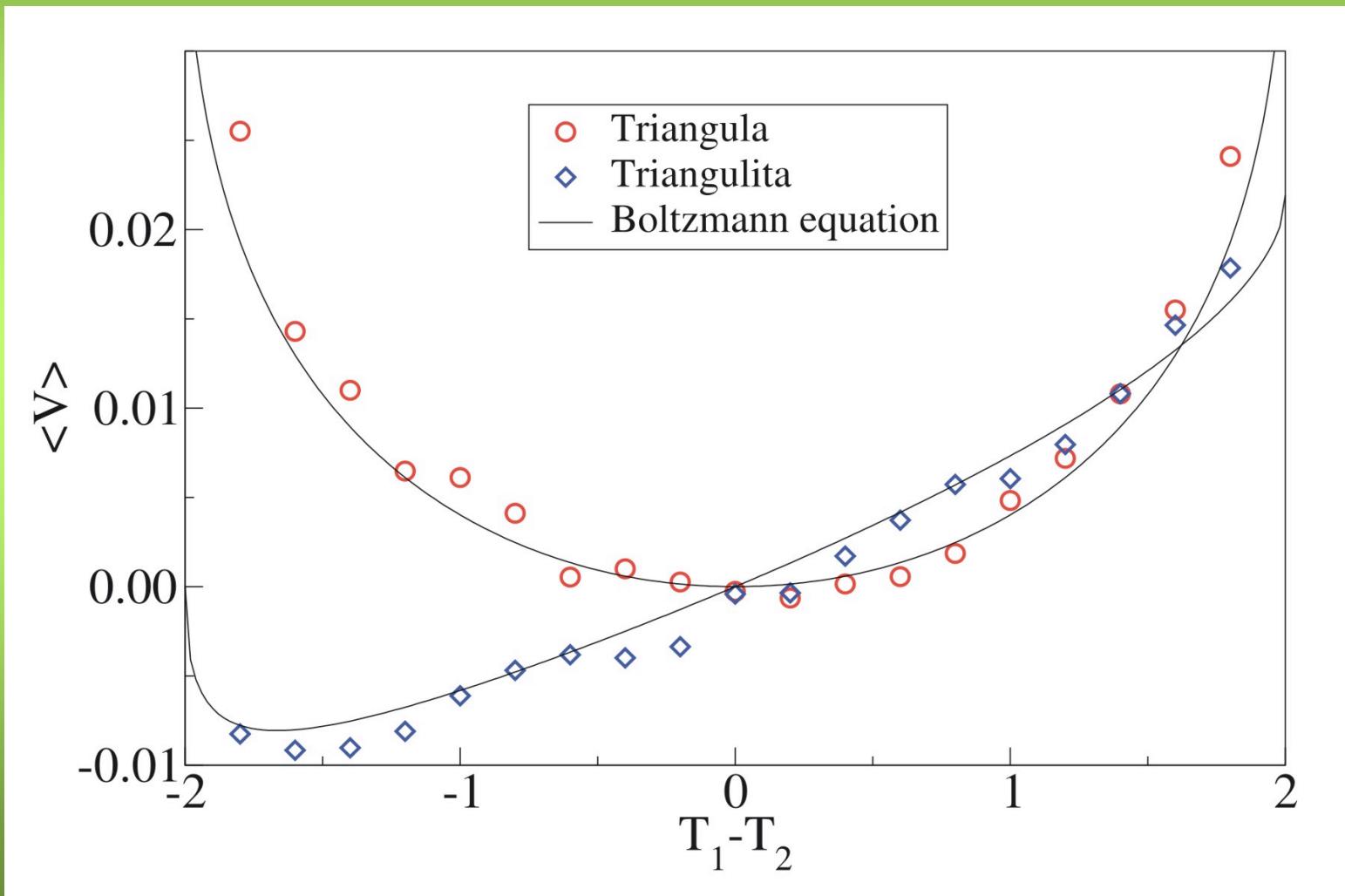
$T_1 = T_2$ unbiased Brownian motion



$T_1 \neq T_2$ biased Brownian motion : Brownian motor

Theory: Boltmann-Master equation

Numerical experiment: molecular dynamics

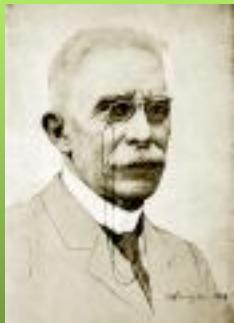
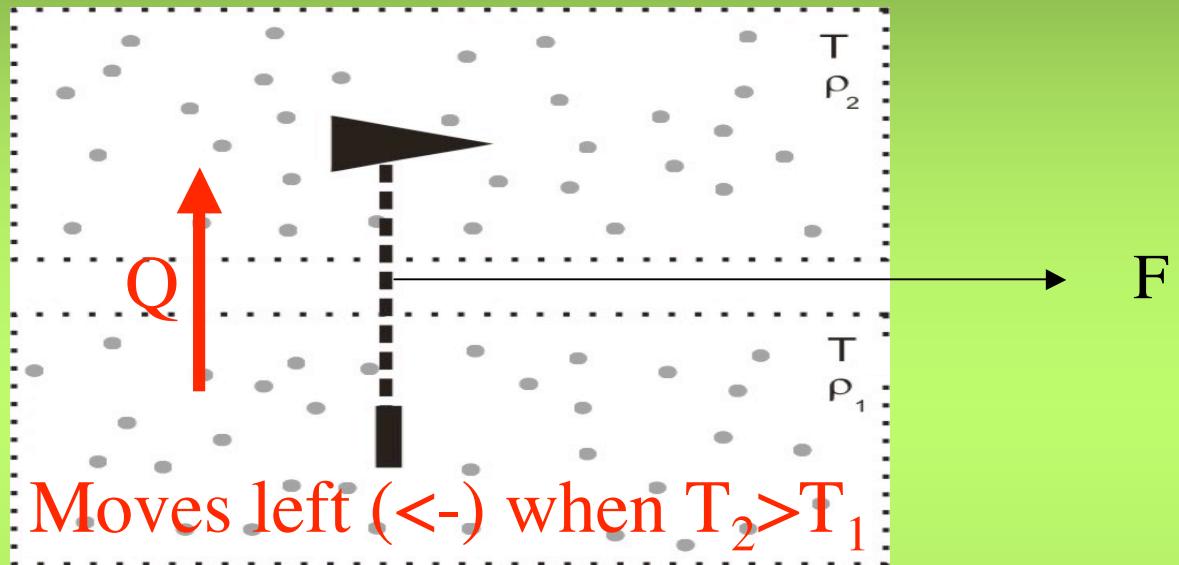


Brownian refrigerator ?!

Equilibrium

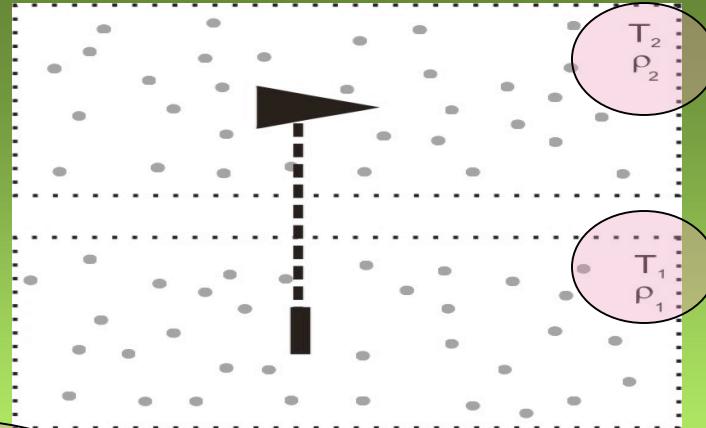
$$T_1 = T_2 = T$$

Apply force F
Effect?



Le Chatelier: an action on a system at equilibrium induces processes that attenuate or counteract the original perturbation.

Implication $Q \sim F$!



T-gradient
thermodynamic force \rightarrow particle motion
 \rightarrow flux

$$X_2 = \Delta T / T^2$$

cross effect

$$J_1 = \dot{x}_1$$

$$J_1 = L_{12} X_2$$

Onsager symmetry

mechanical force F

$$J_2 = L_{21} X_1$$

$$L_{12} = L_{21}$$

heat flux

$$X_1 = F/T$$

$$J_2 = \dot{Q}_2$$



Linear irreversible thermodynamics



$$\begin{aligned} J_1 &= L_{11}X_1 + L_{12}X_2 \\ J_2 &= L_{21}X_1 + L_{22}X_2. \end{aligned}$$

T-gradient \rightarrow particle flux

$$X_2 = \Delta T/T^2 \quad J_1 = \dot{x}_1$$

Since $L_{12} = L_{21}$.

Force \rightarrow heat flux

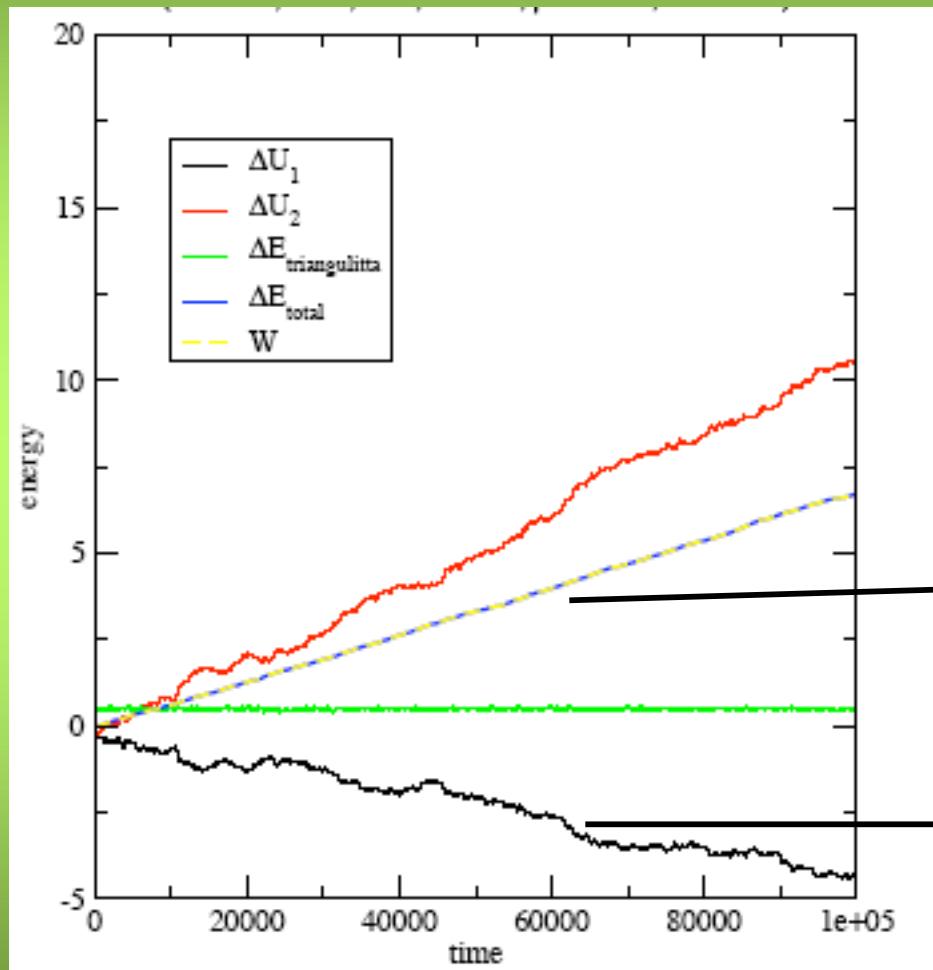
$$X_1 = F/T \quad J_2 = \dot{Q}$$

$$\begin{aligned} \langle V \rangle_{\text{Triangulita}} &= \rho_1 \rho_2 (1 - \sin^2 \theta_0) \frac{\sqrt{2\pi k_B m}}{2M} \\ &\times \frac{(T_1 - T_2) \sqrt{T_1}}{[2\rho_1 \sqrt{T_1} + \rho_2 \sqrt{T_2} (1 + \sin \theta_0)]^2} \end{aligned}$$

$$\begin{aligned} L_{12} &= \rho_1 \rho_2 (1 - \sin^2 \theta_0) \left(\frac{m}{M} \right) \sqrt{\frac{\pi k_B}{2m}} \\ &\times \frac{T^{3/2}}{[2\rho_1 + \rho_2 (1 + \sin \theta_0)]^2}. \end{aligned}$$

$$\begin{aligned} \dot{Q}_{1 \rightarrow 2} &= \rho_1 \rho_2 (1 - \sin^2 \theta_0) \left(\frac{m}{M} \right) \sqrt{\frac{\pi k_B T}{2m}} \\ &\times \frac{F}{[2\rho_1 + \rho_2 (1 + \sin \theta_0)]^2}. \end{aligned}$$

Application external force F ($X_1 = F/T$)?



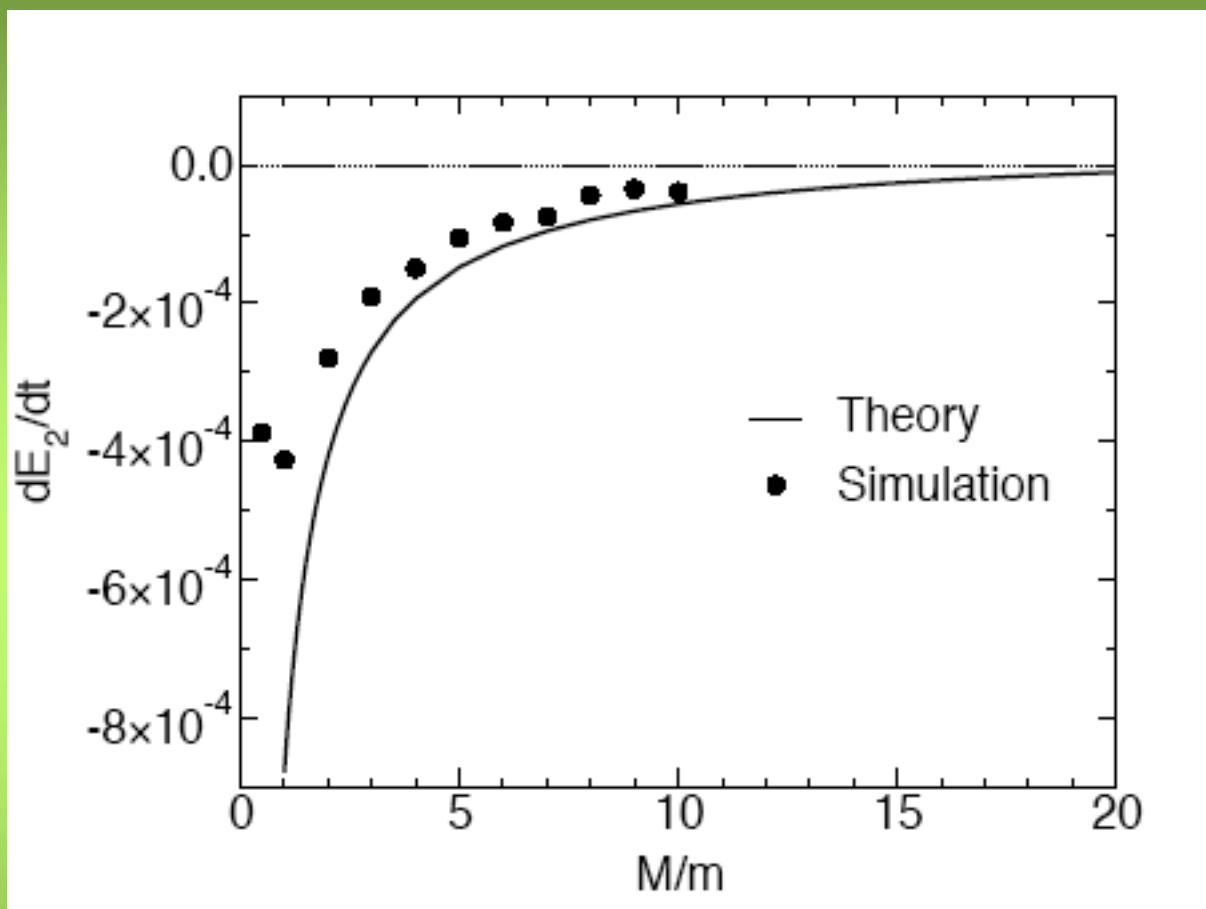
particle motion

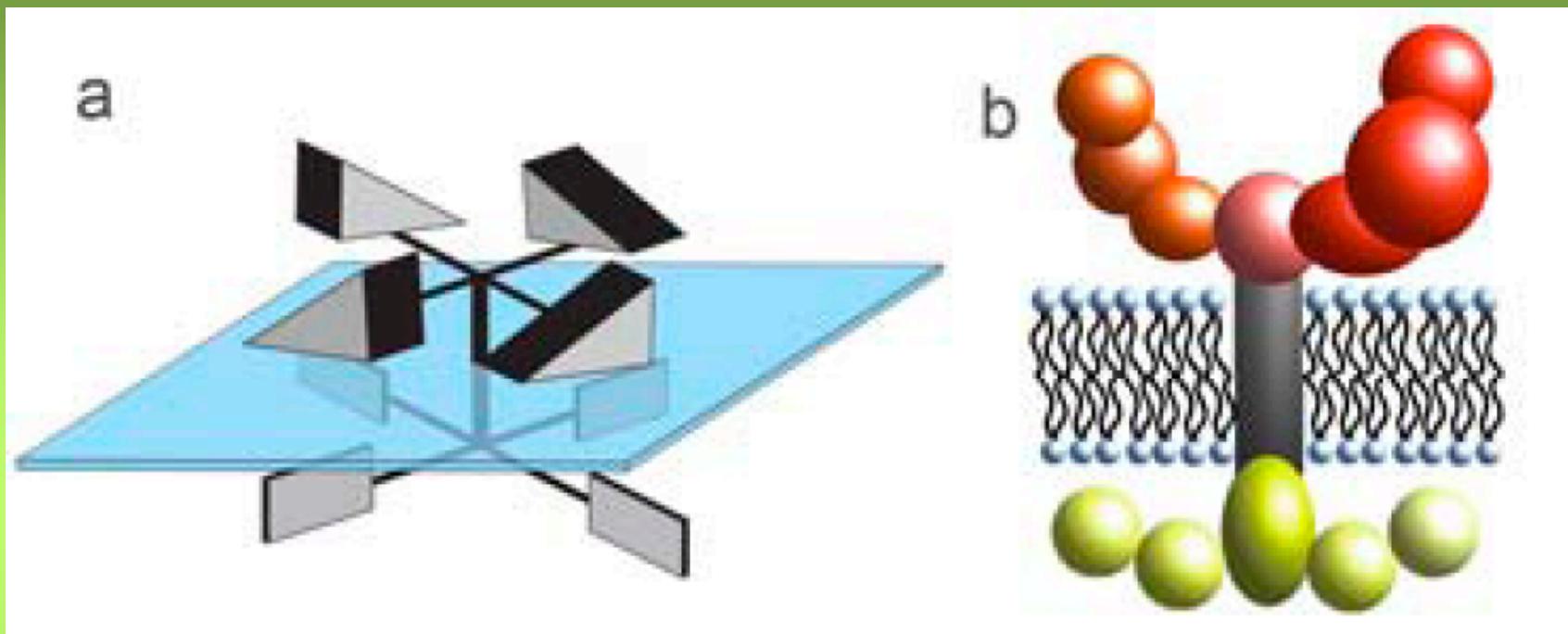
$$\begin{aligned} J_1 &= L_{11}X_1 + \cancel{L_{12}X_2} \\ J_2 &= L_{21}X_1 + \cancel{L_{22}X_2}. \end{aligned}$$

heat flow

Joule heating
 $F J_1 \sim F^2$

Cooling flux
 $\dot{Q} = J_2 \sim F$





physiological condition $T \sim 300 \text{ K}$ $M \sim 10^5 \text{ m}$ $F \sim 0.1 \text{ pN}$

$$\dot{Q} \sim 5 \cdot 10^{-17} \text{ J/sec}$$

aqueous reservoir of $0.1 \mu\text{m}$ diameter: cooling of 1 K/min

DISCUSSION

Feynman-Smoluchowski ratchet is unnecessarily complicated
Fully microscopic mechanical model

Hard disk molecular dynamics: only round-off error
Theory: perturbation in m/M , but exact, no adjustable parameters

$T_1 = T_2$: no Maxwell demon

$T_1 \neq T_2$: Brownian motor \sim speed of sound * $\sqrt{m/M}$

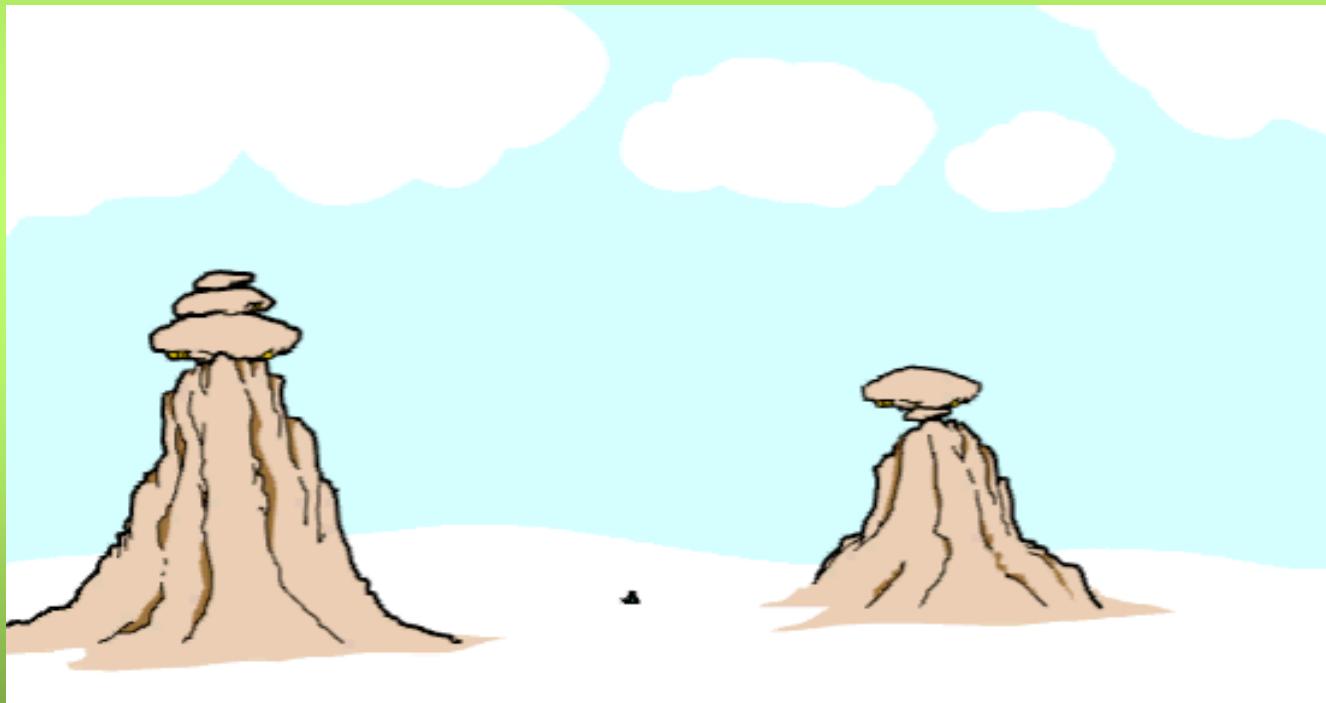
Onsager symmetry: from motor to refrigerator

Heat flux \sim power input * $\sqrt{m/M}$

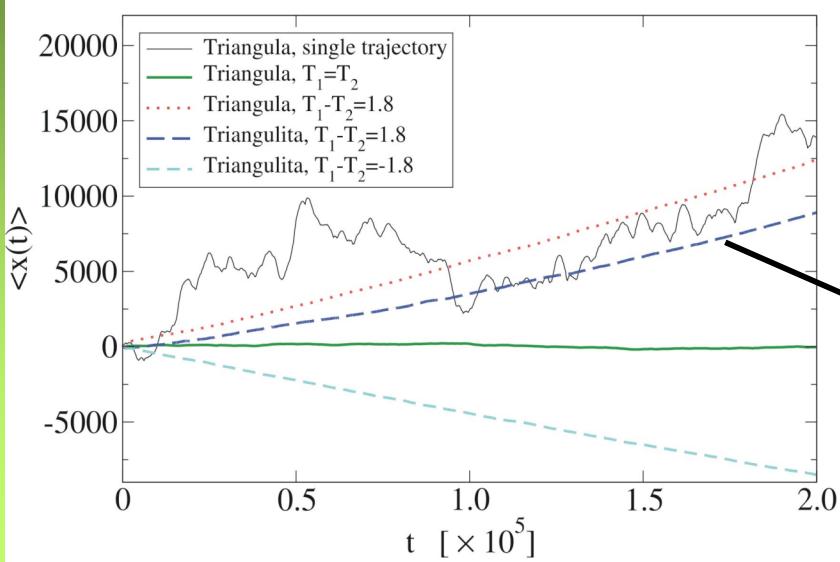
Dominates for small applied force (torque)

Carnot efficiency: yes in principle

- C. Van den Broeck, R. Kawai and P. Meurs, Phys Rev Lett **93**, 090601 (2004)
P. Meurs, C. Van den Broeck and A. Garcia, Phys Rev E**70**, 051109 (2004)
C. Van den Broeck, P. Meurs and R. Kawai, New J Phys **7**, 10 (2005)
C. Van den Broeck, Phys Rev Lett **95**, 190602 (2005)
C. Van den Broeck and R. Kawai, Brownian refrigerator, Phys Rev Lett (2006)

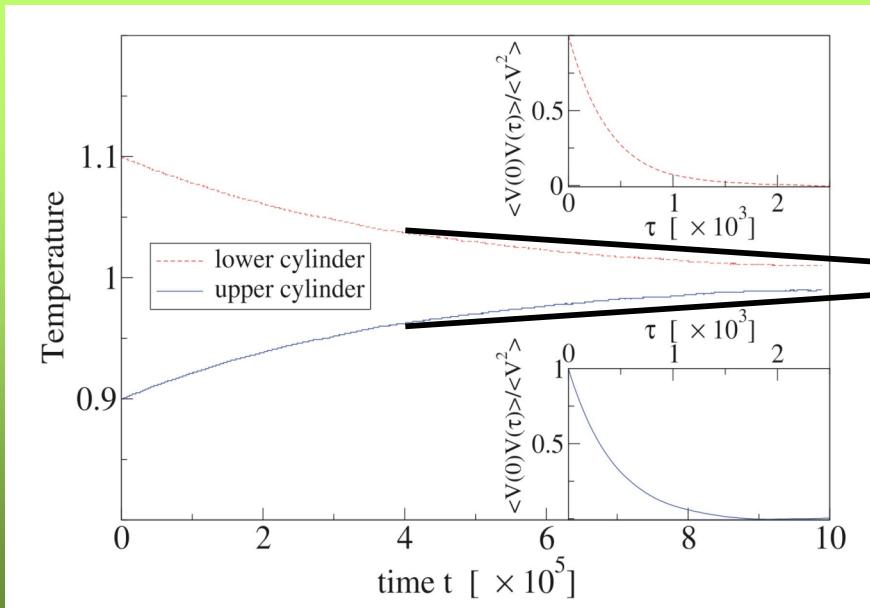


$\Delta T = T_2 - T_1$ external force $F=0$



$$\begin{aligned} J_1 &= \cancel{L_{11}X_1 + L_{12}X_2} \\ J_2 &= \cancel{L_{21}X_1 + L_{22}X_2}. \end{aligned}$$

$$\langle V \rangle_{\text{Triangula}} = \rho_1 \rho_2 (1 - \sin \theta_0) \frac{\sqrt{2\pi k_B m}}{4M} \frac{(T_1 - T_2)(\sqrt{T_1} - \sqrt{T_2})}{[\rho_1 \sqrt{T_1} + \rho_2 \sqrt{T_2}]^2}.$$



$$\dot{Q}_{1 \rightarrow 2} = \kappa (T_1 - T_2)$$