Heat transfer and evaporative cooling in the function of pot-in-pot coolers

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A pot-in-pot cooler is an affordable electricity-free refrigerator which uses the latent heat of vaporization of water to maintain a low temperature inside an inner compartment. In this article, we experimentally investigate the influence of the main physical parameters in model pot-in-pot coolers. The effect of the wind on the evaporation rate of the cooling fluid is studied in model experiments while the influence of the fluid properties (thermal conductivity, specific heat, and latent heat) is elucidated using a variety of cooling fluids (water, ethanol, and ether). A model based on a simplified heat conduction equation is proposed and is shown to be in good quantitative agreement with the experimental measurements.

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I. INTRODUCTION

A pot-in-pot cooler, clay-pot cooler, or zeer, is a simple and cheap electricity-free evaporative cooling device. It consists of a porous outer pot, in which a smaller waterproof inner pot (often glazed clay) containing the foodstuff is fitted. The space between the pots is filled with sand, which allows water to slowly percolates to the outer surface of the pot where it evaporates (see Fig. 1). Since the evaporation of water is an endothermic process, the energy required is taken from the system, causing the temperature in the inner pot to drop by typically \( 5^\circ \text{C} \) to \( 20^\circ \text{C} \).\(^1,2\)

The use of pot-in-pot coolers can be tracked to 2500 BC in Egypt and as early as 3000 BC in Indus Valley civilizations\(^3\) but interest in such affordable and simple devices has recently been renewed.\(^4,5\) Similar devices can be found in different cultures: a botijo is a traditional element of the Spanish culture and consists of a single porous clay pot, usually filled with water. It relies on the same principle although the stored fluid itself acts as the refrigerant.\(^6\) Pot-in-pot coolers are still widely used and their design and optimization is the focus of a vast technical engineering literature (see Refs. 7–12 and references therein).

The goal of this paper is to propose simple hands-on experiments to explore the physics behind the pot-in-pot cooler in simplified model experimental set-ups rather than actual devices. A simplified theoretical approach, based on strong hypotheses is presented, and shows very good agreement with the experimental data. In a single project-based laboratory work, students could practice modelling and grasp fundamental concepts in thermodynamics which are often addressed in separate experiments. Namely, the proposed setup is a great introduction to the concepts of heat conduction,\(^13-15\) latent heat,\(^16,17\) or supercooling,\(^18\) and can demonstrate that water can be frozen into ice through evaporation.\(^19,20\)

The article is organized as follows. Section II is dedicated to the modeling of the simplified systems. The influences of the wind speed and of the nature of the liquids used are studied and a simplified governing equation is proposed. In Sec. III, experimental results on the cooling of various versions of clay-pot coolers are presented, and the agreement with the theoretical predictions is discussed.

II. MODELING

In this section, simplifying hypotheses are presented, the influences of the key parameters (size, nature of the evaporating fluid, wind) are discussed and a simplified governing equation is proposed.

A. From real pot-in-pot coolers to experimental models

Let us first discuss important parameters controlling the cooling efficiency of a real pot-in-pot cooler, as displayed in Fig. 1 and in Fig. 2(a). As explained in the introduction, the matter within the pot—referred to as the “cooled matter” in the remainder of the text—is cooled through the evaporation of a liquid stored between the inner and outer pots—referred to as the “evaporating liquid” in the remaining of the text. The size of the cooler is the first important parameter. As is customary in heat conduction problems, the total heat

![Fig. 1. Sketch of a pot-in-pot cooler. The water in the sand filling the gap between the two pots percolates through the porous outer clay pot and evaporates, cooling the entire system. Foodstuff can be safely stored inside the refrigerated inner compartment (often a glazed clay pot).](https://doi.org/10.1119/1.5016041)
capacity scales as the volume, while the thermal losses scale as the surface area of the system. However, in a pot-in-pot cooler, the cooling power (the rate at which thermal energy can be extracted from the system) also scales as the surface and while it initially exceeds the losses, they eventually balance out to reach an equilibrium. Therefore, the equilibrium temperature should be independent of the size (provided that the outer pot is kept wet), whereas the cooling dynamics should be faster for smaller systems.

The thickness of the pots and of the sand-layer is also an important geometric parameter. Increasing this thickness increases the thermal resistance to heat conduction, the effect of which remains unclear. Indeed, a greater resistance will help keep the pot cool, but it will simultaneously limit the cooling provided by the evaporation. Again, the optimal size will depend strongly on the exact conditions of use, and more specifically on the water resources available.

The role of the sand is to stabilize the inner pot inside the outer pot and to evenly distribute the water along the entire height of the pot by means of capillary action. In actual pot-in-pot coolers, the inner pot is glazed to prevent any water leakage inside the cooling compartment. However, as explained in the introduction, a simpler cooling device can be used: a botijo simply consists of a unique porous clay pot in which the stored and cooled liquid also acts as the evaporating liquid (see Fig. 2(b)). This kind of cooler is usually used to cool water (or sometimes wine) although some of the liquid is lost.

In order to simplify the system and focus on the main physical parameters, most of the experiments reported in this article were conducted in long cylindrical containers (test tubes or graduated cylinders) as displayed in the rightmost panel of Fig. 2. The cooled matter was restricted to liquids (water or ethanol) for simplicity. The height is noticeably greater than the diameter and as a crude approximation, the system may be considered two-dimensional. Note that the temperature gradient is mostly radial (the containers were capped) and as a consequence little convection within the fluid is expected. Our model pot-in-pot cylinder is wrapped in a thin paper towel, initially soaked in an evaporating liquid.

B. Nature of the evaporating liquid

As explained above, the origin of the cooling lies in the latent heat of evaporation of the outer liquid. During evaporation at the surface of the porous outer pot, the corresponding energy is taken mostly from the pot itself and to a lesser extent, from the surrounding environment. The latter is however neglected in the energy conservation in the rest of the manuscript.

The optimization of the pot-in-pot cooler thus requires a combination of high latent heat of evaporation $L_v$ (of the evaporating liquid) as well as a high evaporation rate, $\dot{m}_e$. Table I reports the physical properties of the three liquids used (water, ethanol, and ether). The exact computation of the evaporation rate is a rather complex task beyond the scope of the current paper, but to first order, it is given by

$$\dot{m}_e \propto P_{eq}(1 - H),$$

where $P_{eq}$ is the equilibrium vapor pressure of the evaporating liquid and $H$ its corresponding relative humidity (ratio of partial pressure to $P_{eq}$). While the latent heat of water exceeds that of ethanol (by a factor 2) and ether (by a factor 6), the huge discrepancy in their equilibrium vapor pressure (that of ether being 25 times that of water) shows that ether is a much more efficient cooling fluid. Indeed, its evaporation rate is 20 times that of water and 10 times that of ethanol.

C. Influence of air flow on the evaporation rate

A simple and efficient way to reduce the local partial pressure at the surface of the pot is to increase air advection, i.e., to increase the wind. Experiments were conducted using a Petri dish (of diameter 8 cm and height 1 cm) filled with water, surrounded by air at 75% relative humidity and at temperature $T = 23^\circ C$. Air is blown from the side of the cylinder, using a fan. Figure 3(a) shows the evaporation rate as a function of wind speed. The air speed is determined with an anemometer and the evaporation rate is obtained by

Table I. Evaporating liquid thermodynamic data from Ref. 25. Specific heat and latent heat are specified at 298 K and equilibrium vapor pressure is at 373 K.

<table>
<thead>
<tr>
<th>Liquid</th>
<th>Density $\rho$ (kg m$^{-3}$)</th>
<th>Spec. heat $c$ (kJ kg$^{-1}$ K$^{-1}$)</th>
<th>Lat. heat $L_v$ (kJ kg$^{-1}$)</th>
<th>Vapor pressure $P_{eq}$ (kPa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Water</td>
<td>1000</td>
<td>4.18</td>
<td>2,442</td>
<td>2.34</td>
</tr>
<tr>
<td>Ethanol</td>
<td>789</td>
<td>2.44</td>
<td>918</td>
<td>5.8</td>
</tr>
<tr>
<td>Ether</td>
<td>713</td>
<td>2.36</td>
<td>365</td>
<td>58.6</td>
</tr>
</tbody>
</table>
determining the mass of the remaining water as a function of time. The effect of wind is crucial: the evaporation rate is larger by a factor ten when the wind speed is 5 m/s compared to a situation without wind (when the partial pressure at the surface decreases mostly through molecular diffusion) and a wind speed of 5 ± 0.5 m s⁻¹ when advection dominates. The smallest air flow that the fan could produce (1.5 ± 0.2 m s⁻¹) already causes a large increase in the evaporation rate (by a factor 5). The wind speed therefore appears to critically affect the evaporation dynamics and actual pot-in-pot coolers are better used in a windy environment.

D. Governing equation

Let us first consider the heat diffusion in a long solid cylinder, of diameter a, height h, thermal conductivity λ, density ρ and specific heat c, initially at temperature $T_i$, quenched to the ambient temperature $T_0$. The heat diffusion equation in cylindrical coordinates reads

$$\frac{1}{r} \frac{\partial}{\partial r} \left( r \frac{\partial T}{\partial r} \right) = \frac{\rho c}{\tau} \frac{\partial T}{\partial t}. \quad (2)$$

This equation can be analytically solved once boundary conditions are specified. (A Dirichlet boundary condition is used here, i.e., the temperature at the surface is given by $T_0$.) The temperature at the center of the cylinder is given in terms of a series of Bessel functions of the first kind. However, a simplified separated-variables solution can be found and is expected to describe the long-term evolution of the system

$$T - T_0 = (T_i - T_0) e^{-t/\tau}, \quad (3)$$

where

$$\tau = \left( \frac{a}{2j_0} \right)^2 \frac{\rho c}{\lambda},$$

and where $j_0 \simeq 2.405$ is the first zero of the $J_0$ Bessel function.

Note that the temperature relaxation time may be conveniently expressed as $\tau = RC$, where $C = \pi (a/2)^2 \rho c$ is the total heat capacity and $R = 1/(j_0 \pi \lambda)$ is an effective thermal resistance ($h$ being the height of the liquid inside the inner jar). The system can therefore be seen as a simple capacitor charging (or discharging) through a resistor.

In order to validate this approach, experimental measurements were conducted using a solid PVC cylinder (30 mm in diameter and 200 mm in height) initially heated at 52 °C and then placed in a flow of cold ($T_0 = 20^\circ$C) air blowing at $3 \pm 0.3$ m s⁻¹. Obviously no convection occurs in the solid and conduction is the prevalent mode of heat transfer. A small hole was drilled along the axis of the cylinder and the temperature was recorded at its center using a thermocouple. Figure 4 shows the time evolution of the temperature difference $T - T_0$. After typically 100 s, the dynamics of cooling is indeed very well fitted by an exponential law (see red lines and insets). Note that $\tau$ could be computed from tabulated values of the material properties. However, discrepancies might arise due to the simplistic choice of the Dirichlet boundary conditions. Instead, the main result of this paragraph is that the dynamics are indeed well described by an exponential law, which is defined by an effective decay constant $\tau$.

Although the temperature within a solid cylinder (or in the water inside a pot-in-pot cooler) is clearly not uniform, its average value is directly linked to that at its center. Therefore, we propose to model the pot-in-pot cooler as a system of uniform temperature $T$ and heat capacity $C$ (of internal energy $CT$), cooled at a rate given by $m_e L_v$, where $m_e$ is the evaporation rate of the evaporating liquid and $L_v$ its latent heat of vaporization. Energy is lost to the ambient environment at temperature $T_0$ through an effective thermal resistance $R$ so that the heat transfer is given by $1/R(T - T_0)$.

The conservation of energy, or first law of thermodynamics, therefore reads

$$C \frac{dT}{dt} = L_v m_e - \frac{1}{R} (T - T_0). \quad (4)$$

Note that in general $m_e$ does not remain constant throughout an experiment, unless the evaporating liquid is continuously supplied to the system. The predicting power of this simplified equation is discussed in Sec. III.

III. COOLING EXPERIMENTS

A. A real botijo

The first experiment was conducted in a single actual clay-pot, modeling a botijo (see Fig. 2(b)). In this setup, the

Fig. 4. Temperature evolution of a cooled PVC cylinder. Initially, the cylinder is homogeneously heated at 52 °C then placed in a 20 °C air flow. After a transient, the temperature evolution can be described by an exponential law (see a solid red line). The inset shows the same data on a semi-log scale.
cooled liquid (water) therefore also acts as the evaporating liquid. The clay-pot has a 31 volume, a height $h = 20$ cm, an upper diameter of 15 cm, while its walls are 5 mm thick and its mass is 1554 g. The pot is filled with 1.85 l of water. The total heat capacity of the system ($C = 9900$ J K$^{-1}$) is simply computed as the sum of that of the water and of the clay (using a specific heat of 1380kJ kg$^{-1}$ K$^{-2}$). During all measurements, a fan was used to create a constant wind ($10 \pm 2$ m s$^{-1}$).

The relative humidity, measured using a hygrometer, remained between 72% and 74% during the entire experiment. The mass is recorded using a scale (see Fig. 5(a)) and the inner temperature is measured using a thermocouple placed at the center of the pot (Fig. 5(b)) while the ambient temperature $T_0$ remains constant (21 $^\circ$C) during the experiments. In this experiment with a constant ventilation acting on the pot, and a virtually infinite amount of evaporating liquid, the overall mass decreases linearly, indicating a constant evaporation rate, $\dot{m}_e = -41\pm5$ g h$^{-1}$, given by the linear fit shown in Fig. 5(a).

The temperature of the water gradually decreases from 21 $^\circ$C to 15.3 $^\circ$C over the course of four hours and then stabilizes. This corresponds to an equilibrium between the energy loss due to the evaporating water and the positive conductive heat flow from the warmer ambient air through the pot.

The solid curve in Fig. 5(b) represents the theoretical prediction of the evolution of the temperature calculated from Eq. (4) based on a constant evaporation rate

$$\begin{align*}
T &= T_{eq} + (T_0 - T_{eq}) e^{-t/t}\,; \\
T_{eq} &= T_0 + RL_e \dot{m}_e.
\end{align*}
$$

The value of the effective thermal resistance can be computed from the equilibrium temperature $T_{eq}$ and the previously fitted evaporation rate $\dot{m}_e$, as

$$\frac{1}{R_{fit}} = \frac{L_e \dot{m}_e}{T_0 - T_{eq}} = 4.8\pm0.6$ W K$^{-1}$. 

(6)

The agreement between the theory and the experimental measurement is very satisfactory. Indeed, with no further fitting parameter, the characteristic decay time is well predicted. The agreement is all the more satisfactory given that roughly 15% of the water has evaporated over the duration of the experiment, changing the total heat capacity.

Note that the fitted value of the effective thermal resistance can be compared to that of a long water cylinder given in Sec. II D, using only the thermal conductivity of water $\lambda_w$,

$$\frac{1}{R_{cylinder}} = 5.76\pi \cdot \lambda_w h \approx 2.2\pm0.1$ W K$^{-1}$. 

(7)

The values are of the same order of magnitude but differ significantly. Indeed, the clay pot used is far from a 2D system and the surface area of the bottom and the top of the container should be taken into account; the measured resistance is thus considerably less than that of a corresponding infinite cylinder.

B. Model pot-in-pot cooler

A model pot-in-pot cooler, with a limited amount of evaporating liquid, consisting of a plastic test tube, is studied in this section.

1. Experimental details

The test tube has a diameter of 30 mm and a height of 90 mm, while the walls are 1 mm-thick, and it is filled with 50 ml of distilled water. The contribution of the container itself is therefore neglected in the total heat capacity of the system and in the effective thermal resistance. The test tube is wrapped in a paper towel, initially soaked with $m_0 = 5$ g of ethanol, acting as the evaporating liquid. The model pot-in-pot is placed vertically in a constant air flow of $3.2 \pm 0.3$ m s$^{-1}$ created by a fan and, as discussed above, the partial pressure of ethanol in the environment remains negligible throughout the experiment. The time evolution of ethanol mass is recorded by a weight scale and is plotted in Fig. 6(a).

2. Evaporation rate

Contrary to the previous experiment in which the amount of evaporating liquid was virtually unlimited, the evaporation rate of ethanol, $\dot{m}_e$, is not constant but decays exponentially (solid curve in Fig. 6(a)).

A rudimentary first-order explanation of the exponential decay of the evaporation rate can be given. In this model set-up, the paper towel wrapped around the test tube does not remain homogeneously soaked in ethanol as it evaporates. Instead, due to gravity, the upper part of the paper towel dries out quickly whereas the bottom part remains wet for a longer time. The cooling power therefore decreases as the amount of ethanol decreases, leading to a classical ODE (assuming a constant evaporation rate per unit of wet surface, which itself decreases in time). The amount of ethanol therefore decreases exponentially (and so does the evaporation rate)

$$m_e(t) = m_0 e^{-t/t_\sigma},$$

(8)
where the characteristic time, $\tau_m$, depends on the speed of wind, on the nature of the evaporating liquid used, and on the dimensions of the test tube. For the experimental results reported in Fig. 6, $\tau_m \sim 250 \pm 10$ s.

Note that the mass decay shown in Fig. 6(a) is compatible with an exponential decay only over the first 500 s of the experiment. Discrepancies at later time are due to condensation of water vapor contained in the surrounding air onto the ethanol-wet paper towel. However, the discrepancy is small and occurs only after the evaporation rate is already negligible.

3. Temperature evolution

Figure 6(b) represents the time evolution of the temperature measured using a thermocouple at the center of the test tube (black squares). Initially, due to the high evaporation rate, the temperature drops rapidly. As the temperature decreases, the heat loss to the ambient air increases while the cooling power decreases, which leads to a minimum temperature (which does not coincide with the end of the evaporation). Over longer times ($t > 800$ s) the evaporation rate can be considered null and the system simply warms up in the surrounding air. The temperature therefore exponentially relaxes to the ambient temperature, as can be seen in the inset in Fig. 6(b). Not only does this confirm the exponential relaxation but it also allows one to precisely measure the characteristic relaxation time $\tau$.

4. Prediction

To summarize, the evaporation rate of ethanol $\dot{m}_e(t)$ is known, the total heat capacity $C$ is computed from the amount of water used, and the characteristic time $\tau$ linked to the effective thermal resistance is fitted on the final relaxation of the temperature. Equation (4) can therefore be solved and yields

$$T(t) = T_0 - \frac{L_v m_{e,0}}{C} \frac{\tau}{\tau - \tau_m} \left(e^{-t/\tau_m} - e^{-t/\tau}\right).$$

This empirical/analytical solution is shown as a solid curve in Fig. 6(b) and demonstrates a good overall agreement with the experimental data. Let us emphasize again that the value of the thermal resistance was computed during the final relaxation regime in which all the ethanol has evaporated. The initial cooling regime is well fitted while the minimum temperature (and the time at which it is reached) is very well predicted. Again, one can conclude that a complex system such as a pot-in-pot cooler is accurately governed by the simplified governing equation (4).

C. Continuous cooling

In this section, a small quantity of water (9 ml) placed in a thin plastic test tube (5 mm in diameter and 50 mm in height) and wrapped in a wet paper towel, is cooled by evaporating ether.

1. Experimental details

Ether is constantly added to the system (using a pipette) as it evaporates on the paper towel. The test tube is exposed to a strong wind using a compressed air gun ($10 \pm 2$ m s$^{-1}$) in order to further increase the evaporation rate and the experiments were conducted in a fume hood. However, the wind also has counterproductive consequences since a portion of the ether, $1 - \phi$ (estimated below), is blown away before being able to play its role as evaporating liquid. In this experiment, $\dot{m}_e$ is directly measured from the volume released by the pipette. A further limitation is that the ether is added at room temperature, which constitutes a source of energy and tends to warm up the water stored in the tube. Finally, it should be mentioned that in such a small test tube the effect of the temperature probe itself might not be neglected. Not only can it significantly contribute to the total heat capacity, but it also acts as a radiator, conducting heat from the ambient air.

2. Experimental results

Figure 7 shows the time evolution of the water temperature. Initially, the temperature drops quickly at the rate of 1°C degree every 3 s, and within two minutes, it becomes negative indicating that the water is in a supercooled state. When the temperature reaches $-7$°C the water abruptly starts to freeze into ice. It takes roughly 1000 s for all the water to turn into ice, after which the cooling resumes.

As explained above, only a (large) fraction $\phi$ of the ether is used as a cooling fluid. This fraction can be computed by fitting the first regime in which liquid water cools down to $-7$°C, which yields $\phi \approx 78% \pm 5\%$, meaning that 22% ± 5% of the ether is lost.

Interestingly, one can predict the duration of the freezing plateau, $\Delta t$, from the latent heat of vaporization of ether $L_v$, the mass of water, $m_{w,0}$, and its latent heat of fusion, $L_f$. Indeed, after the freezing has started, the energy provided by the evaporation of ether is used to turn the liquid water into ice and (taking into account the temperature difference between the supercooled water, $T_s = -7$°C, and the freezing temperature $T_f = 0$°C) energy conservation reads
The water rapidly cools down into a supercooled state before it freezes (at $t = 240 \pm 5$ s). The cooling resumes once the liquid water has entirely turned to ice (at $t = 1100 \pm 100$ s). The solid red line corresponds to the solution of the governing Eq. (4).

\[
\frac{\partial m_e}{\partial t} = m_W L_f + C(T_s - T_f),
\]

which yields: $\Delta t = 780 \pm 100$ s. Again, the predicted duration agrees well with the experimental data since the duration of the freezing plateau is $1100 - 240 = 860 \pm 100$ s.

3. Discussion

Finally, we need to mention that the final regime in which the ice cools down is not very well predicted by the governing equation. According to our simplified model, there should be a clear kink in the temperature and a sharper initial decrease. Indeed, the heat capacity of ice is typically half that of liquid water while its thermal conductivity is 3–4 times higher. The characteristic cooling time of ice should therefore be much shorter (6–8 times) than that of liquid water, which is in clear contradiction with the experimental data. The origin of this discrepancy can be attributed to the formation of frost (condensed from the humidity of the ambient air) on the paper towel, drastically reducing the effectiveness of the evaporative cooling.

IV. CONCLUSION

This paper shows that the complex balance between evaporative cooling and conduction heating of a system in an asymmetric air flow can actually be very well approximated by an elementary model, involving very few parameters. Provided the evaporating liquid does not contribute significantly to the heat capacity of the system, we can model the whole system as a solid object in an environment at constant temperature, with the cooling simply derived from its small mass loss. This model was verified with a very simple experimental setup, further showing the robustness of the model.

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