

# SCALE THE WALL

Project 4

January 20, 2017

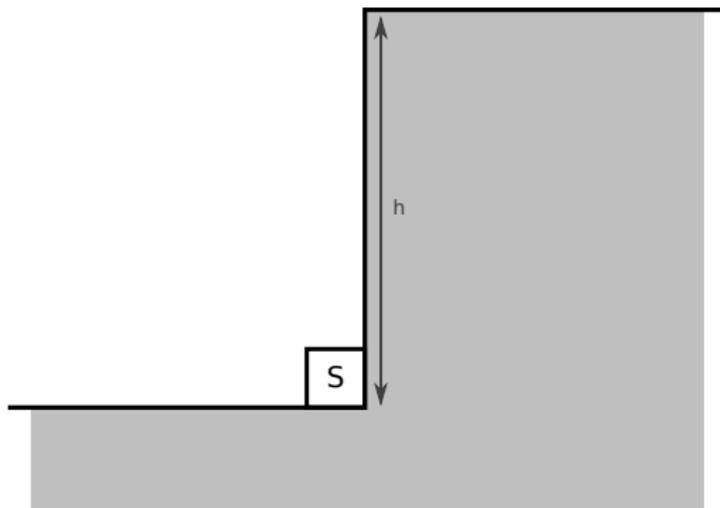
Arthur Blot, Guillaume Combette, Octave Mariotti, Etienne Moutot, Johanna Seif

# OUTLINE

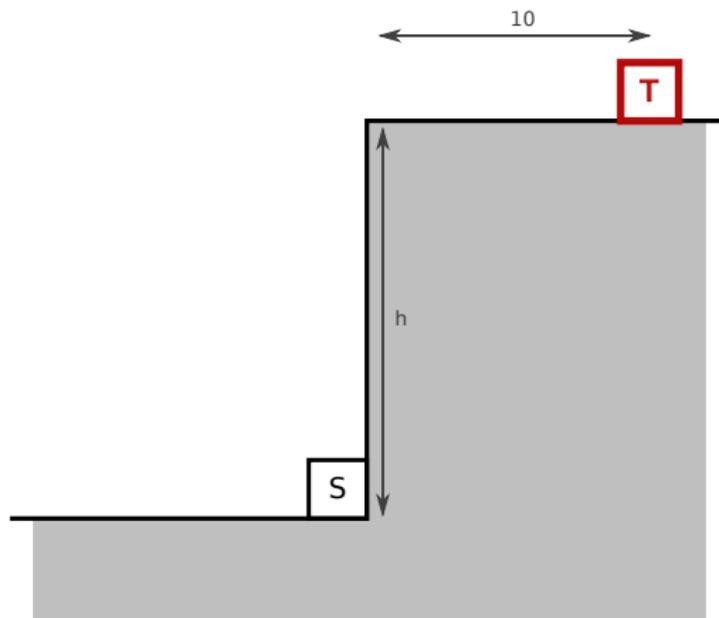
1. Impossibility Proof
2. Working Tiling for Odd Height

# IMPOSSIBILITY PROOF

# THE PROBLEM



## THE PROBLEM



## PROBLEM FORMULATION

Let  $\tau$  be a finite tileset.

The problem asks if there is a  $\tau$  such that:

$$\forall h, \forall \alpha_{\square}, (\alpha_{\square} \text{ obtained from the seed}) \implies \begin{cases} |\alpha_{\square}| \in \mathbb{N} \\ T \text{ is well placed in } \alpha_{\square} \end{cases}$$

## PROBLEM FORMULATION

To contradict it: Find a  $h$  and an assembly  $\beta_{\square}$  such that  $\beta_{\square}$  obtained from the seed and:

$$|\beta_{\square}| \notin \mathbb{N}$$

or

T is not well placed in  $\alpha_{\square}$

## PROBLEM FORMULATION

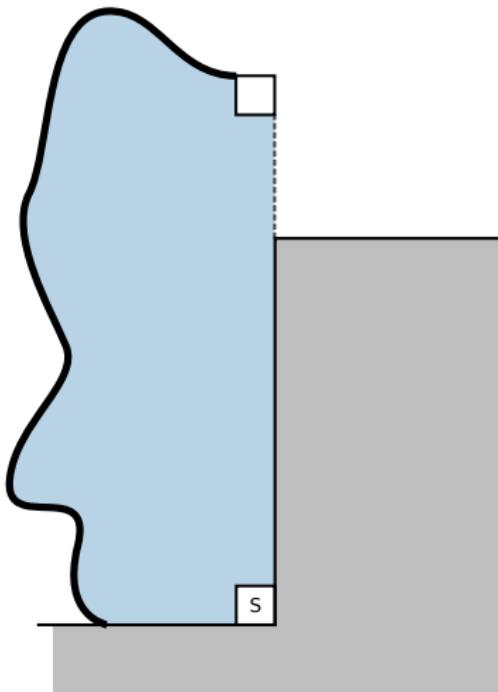
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**T is not well placed in  $\alpha_{\square}$**

# THE CONTRADICTION



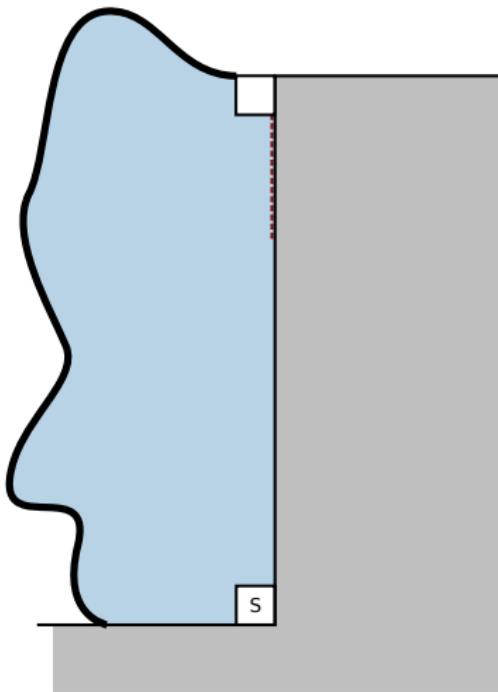
$S$  = set of all partial configurations originating from the seed.

$S' \subseteq S$  = subset of those that have not overstepped the vertical of the wall

## Claim

There exist a partial config  $c \in S'$  that is only extensible to the right (overstepping the vertical)

# THE CONTRADICTION



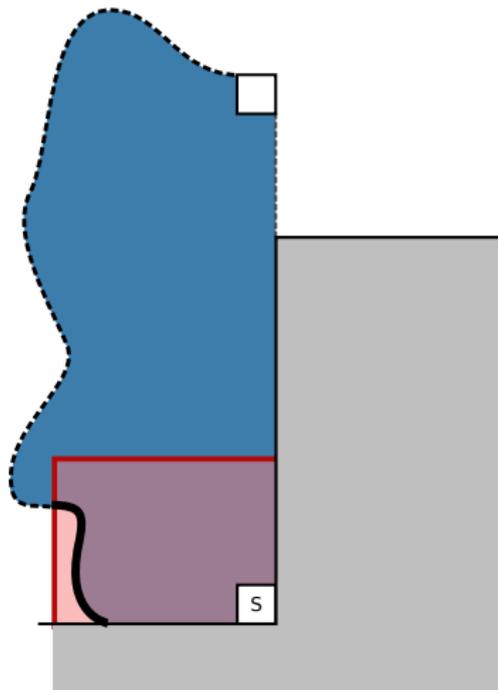
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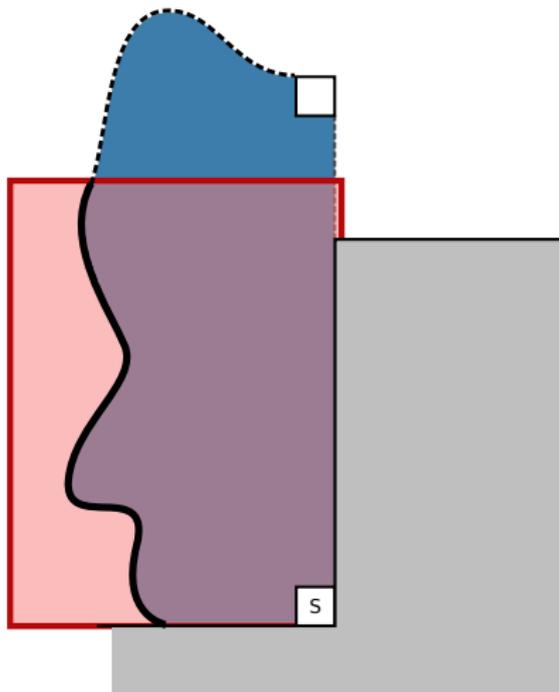
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# "COMPACTNESS"



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WORKING TILING FOR ODD HEIGHT

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Figure: The tileset

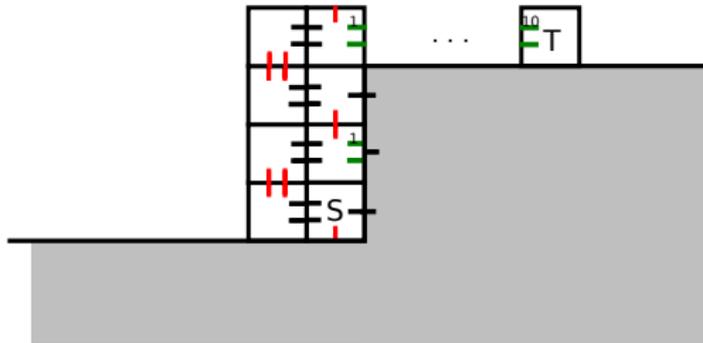


Figure: Example of tiling