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**HW V: Random graphs** (due before Mar 14th at 8:00)

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1. Let  $G$  be a random  $G_{n,p}$  graph. Determine  $p_n^*$  (which may be a function of  $n$ ) such that if  $p_n = o(p_n^*)$  (i.e.,  $p_n/p_n^* \rightarrow 0$ ) then  $G$  has no triangle with probability  $1 - o(1)$  and if  $p_n = \omega(p_n^*)$  (i.e.,  $p_n/p_n^* \rightarrow \infty$ ) then  $G$  has a triangle with probability  $1 - o(1)$ . Recall that a triangle is a triple  $(u, v, w)$  of vertices such that all the edges between them are present.