

# ASYMPTOTIC DENSITY FOR EQUIVALENCE

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## Abstract

In this paper we study the asymptotic behavior of the fraction of true formulas against all formulas over  $k$  propositional variables with equivalence as the only connective in the language. We investigate the size of the tautology fraction of length  $n$  (at most  $n$ , respectively) against the number of all formulas of length  $n$  (at most  $n$ , respectively). In both cases we are interested in finding the limit of each fraction when  $n \rightarrow \infty$ .

In this paper we show that asymptotic density for the language based on equivalence does not exist but for every  $k$  there are exactly two limit points: 0 and  $1/2^{k-1}$  ( $1/2^{k-1}(4k+1)$  and  $4k/2^{k-1}(4k+1)$ , respectively for cumulation density).