



Seismic Anisotropy

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OUTLINE

- Seismic Anisotropy: many processes
- Seismic Data: Body waves, Surface waves
- Scientific Issues:
 - 3D- anisotropic structure of the Earth
 - Upper mantle LAB Oceans- continents
 - Intrinsic versus extrinsic anisotropy and attenuation
 - (-Transition zones: 410-900km)



Seismic Anisotropy is present at all scales Not a second order effect

-From microscopic scale up to macroscopic scale

-Efficient mechanisms of alignment of minerals in the crust and upper mantle:

C.P.O./ L.P.O.: Crystal/Lattice Preferred Orientation; S.P.O.: Shape preferred orientation; FINE LAYERING

ANISOTROPY is the Rule not the Exception

Apparent (observed) anisotropy: NON UNIQUE INTERPRETATION in different depth ranges of the Earth To explain seismic data: heterogeneities isotropic / anisotropic, anelasticity

Confusion: Heterogeneity \neq Anisotropy

-Homogeneous, anisotropic (Olivine aggregates)





Marmousi

Solid Earth: heterogeneous + anisotropic + anelastic

Seismic Anisotropy at all scales



PREM

PREM: radial anisotropy: up to 10%

 λ_W seismic wavelength λ_S spatial scale

(Wang et al., 2013)

Seismic Anisotropy at all scales



Intrinsic

Extrinsic

PREM

Observed (apparent) anisotropy Intrinsic versus Extrinsic anisotropy $\alpha = p\alpha^{int} + (1-p) \alpha^{ext}$

C.P.O. : Crystal Preferred Orientation (strain field)



Mapping of convection

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Christensen and Lundquist, 1982

Seismic Anisotropy at all scales



PREM

PREM: radial anisotropy: up to 10%

 λ_W seismic wavelength λ_S spatial scale

(Wang et al., 2013)

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Coherent Strain field (preferred orientation) Large-scale Seismic anisotropy $\neq 0$

Incoherent Strain field (random orientation) Large-scale Seismic anisotropy ≈ 0





Coherent Strain field

Large-scale Seismic anisotropy $\neq 0$

Incoherent Strain field

Large-scale Seismic anisotropy ≈ 0



Inner Organization

Anisotropy: Not a second order effect



ΔT Effect of Temperature Heterogeneities

Montagner & Guillot, 2002

 $\Delta \alpha$: Anisotropy Effect (CPO)

ΔT:Temperature Effect

 $\Delta \alpha \approx \Delta T$



Olivine (60%) +Opx (40%)



Montagner & Guillot, 2002

Other effects: Cracks, fluid inclusions-S.P.O.: (shape preferred orientation-stress field)

Crust (+lithosphere, asthenosphere)



(Babuska and Cara, 1991)

Inner core



(Singh et al., 2001)

FINE LAYERING: Stratification Anisotropy Mille-feuilles model (partial melting)



Radial anisotropy (Kawakatsu et al. 2009) V.T.I. Vertical Transversely Isotropic medium: 5 parameters $(A=\rho V_{PH}^2, C=\rho V_{PV}^2, F, L=V_{SV}^2, N=V_{SH}^2)$ Effective medium theory: Stratified medium (Fine Layering) Backus (1962) => Homogenization technique (Capdeville et al., 2008...)



Different processes in different layers -S.P.O. (stress) -C.P.O.(strain) Fine Layering



Mineralogy, Water and fluid content
Present day tectonic, geodynamic processes
Past processes (frozen anisotropy)
Monitoring of stress and strain fields

Separation of the different kinds of anisotropy in different layers => Different interpretations (Stratification of anisotropy in the crust & mantle)



Different processes in different layers -S.P.O. (stress) -C.P.O.(strain) Fine Layering



Mineralogy, Water and fluid content
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Stratification of anisotropy in the crust & mantle Separation of the different kinds of anisotropy in different layers => Different interpretations

DATA?



Data in Global & Regional Seismology



[www.geo.uib.no]



[drh.edm.bosai.go.jp]

Barruol et al., 2013



Different kinds of seismic data

Body waves: P-wave azimuthal variations S-wave splitting, SKS

Surface waves:

-discrepancy Rayleigh-Love (polarization anisotropy)

- -Azimuthal variations of phase (or group) velocities
- Effect on amplitudes



Animation courtesy of Ed Garnero

SKS- Splitting





Vinnik et al., 1989 Silver et al., Т

R

S-wave splitting



Savage, 1999; Fouch, 2006; Wüstefeld et al., 2009;

S-wave splitting: Updated SKS database (Becker, 2020)



Savage, 1999; Fouch, 2006; Wüstefeld et al., 2009; Becker et al., 2012; ...





Figure 2.7-1: Seismograms recorded at a distance of 110°, showing surface waves.

surface-wave tomography

Seismic data







Body waves sample deep parts of the Earth

Surface waves sample the crust and upper mantle

Surface waves

P-SV Spheroidal modes



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Surface waves are dispersive.



Example of seismogram (Rayleigh wave)



3-component Seismogram Inversion



Different approaches:

-Phase information: measurement of phase and group velocity dispersion curves of fundamental and higher modes along paths; regionalization + inversion at depth (classical technique)

-*Waveform inversion* => Adjoint Tomography, ...

Seismic Anisotropy?

Anisotropic Tomographic Technique

Forward Problem: Theory d=g(m)
 d data space: observables + C_d

SEISMIC DATA: SEISMOGRAMS

m model parameter space + C_m -

- Reference Earth model m_0 :
 - $d_0 = g(m_0)$
- Kernels ∂g/∂m

• Inverse Problem: $m-m_0 = \tilde{g}^{-1} (d-d_0)$ Barbara (next week)

Effect of anisotropy on the phase of surface waves

Effect on eigenfrequency ω_k for multiplet k={n,l,m} (Rayleigh's principle)

$$\frac{\delta\omega_{k}}{\omega_{k}} = \frac{\int_{\Omega} \varepsilon_{ij}^{*} \delta C_{ijkl} \varepsilon_{kl} d\Omega}{\int_{\Omega} \rho_{0} u_{r}^{*} u_{r} d\Omega} = \frac{\delta V}{V} \Big|_{k}$$

ε strain tensor, u displacement, δC_{ijkl} elastic tensor perturbation, V phase velocity (V_R Rayleigh; V_L Love)

Phase velocity pertubation δV(T,θ, φ,Ψ) at point r (θ,φ)
 (Smith & Dahlen, 1973; Montagner & Nataf, 1986)
 Ψ Azimuth (angle between North and wave vector)

 $\delta V(T,\theta,\phi,\Psi)/V = \alpha_0(T,\theta,\phi) + \alpha_1(T,\theta,\phi)\cos 2\Psi + \alpha_2(T,\theta,\phi)\sin 2\Psi + \alpha_3(T,\theta,\phi)\cos 4\Psi + \alpha_4(T,\theta,\phi)\sin 4\Psi$

Sensitivity Kernels of 0- Ψ , 2- Ψ , 4- Ψ azimuthal terms

13 parameters, functions of C_{iikl} (3x3x3x3) \Leftrightarrow c_{pq} (6x6)

Constant term (0Ψ -azimuthal term: α_0)

$$A = \rho V_{PH}^2 = \frac{3}{8}(C_{11} + C_{22}) + \frac{1}{4}C_{12} + \frac{1}{2}C_{66} \leftarrow C = \rho V_{PV}^2 = C_{33}$$

$$F = \frac{1}{2}(C_{13} + C_{23})$$

$$L = \rho V_{SV}^2 = \frac{1}{2}(C_{44} + C_{55}) \leftarrow N = \rho V_{SH}^2 = \frac{1}{8}(C_{11} + C_{22}) - \frac{1}{4}C_{12} + \frac{1}{2}C_{66}$$

$$\frac{2 \Psi \text{-azimuthal term:}}{\alpha_1 \cos 2\Psi} \qquad \alpha_2 \sin 2\Psi$$

$$B_c = \frac{1}{2}(C_{11} - C_{22}) \qquad B_s = C_{16} + C_{26}$$

$$G_c = \frac{1}{2}(C_{55} - C_{44}) \qquad G_s = C_{54} \leftarrow H_c = \frac{1}{2}(C_{13} - C_{23}) \qquad H_s = C_{36}$$

$$\frac{4 \Psi \text{-azimuthal term:}}{\alpha_4 \sin 4\Psi}$$

Equivalent V.T.I (Transversely Isotropic medium with vertical symmetry axis): 5 parameters



 α_3

 $E_s = \frac{1}{2}(C_{16} - C_{26})$

$$\Rightarrow E_c = \frac{1}{8}(C_{11} + C_{22}) - \frac{1}{4}C_{12} - \frac{1}{2}C_{66}$$

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Fundamental - Higher modes: Depth Sensitivity Kernels Rayleigh waves



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•Cijkl 21 elastic moduli

• $\alpha_0 = 0$ - ψ term: 5 parameters A, C, F, L, N (PREM)

VTI Model (transverse isotropy with vertical symmetry axis)

•Best resolved parameters from surface waves (among 13 parameters when including azimuthal anisotropy 2ψ –, 4ψ –terms)

 $L = \rho V_{SV}^2$ Isotropic part of V_{SV}

 $\xi = N/L = (V_{SH}/V_{SV})^2$ Radial Anisotropy

 G, Ψ_G Azimuthal Anisotropy of V_{SV} , also related to SKS splitting (when horizontal symmetry axis, vertical propagation, Montagner et al., 2000)

•Body waves (Crampin, 1984)

 $\rho V_{SV}^2 = L + G_c \cos 2 \Psi + G_s \sin 2 \Psi$

 $\rho V_{SH}^2 = N - E_c \cos 4 \Psi - E_s \sin 4 \Psi$

Geodynamic Interpretation: LPO

Tomographies of:

-S- Velocity

-Radial Anisotropy $\delta\xi = (V_{SH}^2 - V_{SV}^2)/V_{SV}^2$ -Azimuthal Anisotropy *G*

 $V_{SV} \approx V_{SV0} + \frac{1}{2}G\cos(2(\Psi - \Psi_G))$

At a given depth

Convective cell: anisotropic parameters



Imaging of famous geophysicists




Imaging of famous geophysicists





Anisotropic Imaging





Imaging of famous geophysicists



Anisotropic Imaging





Isotropic Imaging







Examples of applications of seismic anisotropy to geodynamic processes



- •Mapping of mantle convection (global scale)
- •Mapping of the LAB (Lithosphere-Asthenosphere Boundary) Lithosphere roots (oceans- continents)
- Intrinsic versus Extrinsic anisotropy and attenuation
- •Mantle Transition Zones (410-1000km depth range)

L.A.B.: Lithosphere-Asthenosphere Boundary (many different approaches and definitions)



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LAB : from seismic data



Much discrepancy between different estimates:

Global surface wave tomographies give 200-250km depth for continental roots

Mid-lithospheric Discontinuity (Yuan & Romanowicz, 2010)

From Surface wave dispersion





Other proxies from parameters obtained from anisotropy tomographic models



Data collection

Phase and group velocity dispersion curves Rayleigh and Love waves, Fundamental and higher modes (n={0,6})

IPGP(1)	44 - 315	9292†	-	-
UTRECHT(2)	35 - 175	63628	35 - 176	45179
HARVARD(3)	35 - 150	37738	35 - 150	23227
BOULDER(4)	16 - <mark>2</mark> 00	76580	16 - 150	47021
TOTAL	-	187238	-	115427

First step: Regionalization =>local dispersion velocity $V(T, \theta, \phi, \psi)$



LAB: Statistical M.C. Isotropic Inversion

Data: C_R , C_L , U_R , U_L [30-300s], Parameters: 3Vs, $2 \delta z$



First order perturbation Theory => depth distribution of Vsv, G (and ξ)



LAB from the gradient of VSV parameter



LAB from the gradient of ξ parameter (only oceans) Radial anisotropy $\xi = (V_{SH}/V_{SV})^2$



Statistical MC Isotropic Inversion

Vsv proxy (1st order Perturbation Theory)



ξ proxy (1st order Perturbation Theory)

Age Variation of LAB depth in oceanic regions

Compared with Half Space Cooling model



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Age Variation of LAB depth in oceanic regions

Compared with Plate model



Atlantic Ocean

Indian Ocean





New Discontinuity within the lithosphere

- -LAB topography derived from surface wave data on a global scale
- -The ocean lithosphere not so simple!
- For oceans, the model of formation of lithosphere must be revisited in view of results from radial and azimuthal anisotropies.
- -Existence of a strong gradient of ξ between 60-80km (related to dehydration boundary layer?) **Mid-Lithospheric Boundary**





er 2 frozen-in anisotropy

Yuan and Romanowicz, 2010

Indian Continent Motivation and Scientific Challenges

Indian continent is unique in many respects.

Indian plate moved at exceptionally high speeds of 18-20 cm/yr after its breakup from Gondwanaland ~65 Myr. Ago

Five cratons of various extension,

Ravaged by hotspots and experienced large scale magmatism.

Deccan, Rajmahal volcanic trapps

Interaction with plumes (La Réunion, Marion, Crozet and Kerguelen)?



Scientific Challenges – Debate on Indian LAB

- Super mobility due to a thin seismic lithosphere (~80-100km)) (Kumar et al., Nature, 2007)?
- In total disagreement with common consensus on cratons:
- North America (~200-250km) [Yuan and Romanowicz, 2010, ...]: stratification.
- Is the seismic discontinuity at ~100 km depth unrelated to LAB?
- Evidence for postcollisional flexuring of the Indian plate with a wavelength of ~1000 km [Kumar et al., 2013]
- > => Large topography on the LAB (Lithosphere-Asthenosphere Boundary)?
- Deep structure of the Indian continent.



Layering in the lithosphere in NA [Yuan and Romanowicz, 2010]



Unique Dataset

Stations

Earthquakes





- 29 Seismic broadband Networks (global and regional)
- Over 550 seismic stations
- Earthquakes of magnitude >5.5
- Surface wave data in the period range of 10-400s.

3-D tomography model of the Indian continent Velocity and Azimuthal Anisotropy

Z = 70 km

Z = 150 km





3-D tomography model of the Indian continent Radial Anisotropy ξ (Rayleigh – Love inversion)



Study Area: geological signature



3D-Perturbation model



3D-Perturbation model -NS



MLB-ML-LVZ: Mid-lithospheric low velocity zone

3D-Perturbation model: Indian Keel



MLB-ML-LVZ: Mid-lithospheric low velocity zone

Indian Plate LAB (Lithosphere-Asthenosphere Boundary)



Indian Plate LAB: Keel



Azimuthal anisotropy



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Azimuthal anisotropy





80°E

90°E

100°E

70°E

MLB = ML-LVZ2 different orientations of $\Psi_{\rm G}$ 90-120° 10-40° : Indian plate motion

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0

0

90

180

90

180

Discussion: Indian keel 40°

- Prominent cratonic keel present in the center of the Indian continent.
- Shape and orientation of the keel along to the direction of the plate motion.







Indian Plate LAB: Keel






Continental plates

LAB topography derived from surface wave data on a global scale and regional scale (India)

For continents: Large variability of craton thickness Stratification: MLB- ML-LVZ, low velocity zone (not present in all cratonic blocks). Relationship with MLB?

➤The model of fomation of lithosphere must be revisited in view of results from radial and azimuthal anisotropies in oceans and continents.

➢Role of the Indian Keel

➢Role of mantle upwellings in plate motion which might be as important as subducting slabs









Anisotropy and extrinsic Anelasticity (Q factor or Q⁻¹ attenuation)

Knopoff, 1964: Q? no frequency dependence



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Standard Linear Solid: τ relaxation time



Anisotropy and Anelasticity (Q factor or Q⁻¹ attenuation)

Knopoff, 1964: Q? no frequency dependence



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Anisotropy and Anelasticity

Incoherent Strain field

Large-scale Seismic anisotropy ≈ 0

But extrinsic (scattering) attenuation





1D-Layered medium



Random orientation of fast axis

-Exact numerical solution: Thomson- Haskell (*Aki & Richard*, 1980)

- Approximated analytical solution: equivalent medium (*Backus*,1962, *O'Doherty & Anstey*, 1971, *Capdeville & Marigo*, 2007)

$$Q_{app}^{-1} = \frac{E_r}{2\pi E_{tot}} \quad \checkmark U_t$$

Anisotropy and Attenuation



Different kinds Of heterogeneities $\delta \alpha / \alpha$, or $\delta \mu / \mu$, or $\delta \rho / \rho$



Example of mixing

Ricard et al. (2014) Alder et al., 2017

Anisotropy and Attenuation



Conclusions

ZLAR [VSV]

- Seismic Anisotropy can be mapped in different depth ranges

- Interpretation of seismic anisotropy is non-unique (intrinsic C.P.O. versus extrinsic anisotropy)

- Imaging of geological objects such as LAB (Lithosphere-Asthenosphere boundary)
- New findings from anisotropy : MLB
- Attenuation (extrinsic) correlated with anisotropy
- -New tools, numerical techniques and approaches are necessary in order to separate different causes of anisotropy and to model strain and stress fields





Messages of ancestors/grand-parents to kids



Athanasius Kircher, 1678

The Earth is a fascinating object

Our vision completely changed during the last centuries



- Earth science is an object-oriented discipline
- 15 orders of magnitude: upscaling-downscaling
- The fundamental laws of physics cannot explain most geological objects
- Seismic Anisotropy is a good example:
- Intrinsic anisotropy (CPO microscopic)<=>Extrinsic anisotropy (geometry, larger scale)
- Interpretation of seismic anisotropy (and attenuation) is non-unique
- Anisotropy mapped in different depth ranges => Dream: $C_{ijkl}(r,\theta,\phi)$, $Q_{ijkl}(r,\theta,\phi)$, $\eta_{ijkl}(r,\theta,\phi)$
- Multidisciplinary approach: Imaging + evolution of geological objects