# Enjoy learning data analysis, least squares, statistics, and so on. Births and Moon cycle

Frédéric Chambat, Anne-Laure Fougères, Alexandre Elyildirim, 2021, Comptes Rendus Mathématique (Académie des Sciences), to appear soon.

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Les Houches - doctoral school - 2021





- A lot of people are interested in this question
- It's about the Moon (and tides a little bit)
- A nice example of signal analysis
- An example of generalized least squares
- An introduction to statistic tests.

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A common idea is that there is more births on full moon days.

Is this idea well founded?

#### Yes... and no

Part of the room is right, but with the wrong reasons. Part of the room is not right, but with good reasons.

#### Does the moon affect births?

- Are maternity hospitals crowded on full moon days?
- Are there more births on full moon days?
- Are there many more births on full moon days?
- Are there significantly more births on full moon days?
- Is the popular belief, that there are more births on full moon days, based on observations?
- If there are more births on full moon days, can we see it in a maternity ward?

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#### 1. How, and why, do we come to study these kinds of questions?

- 2. Existing analyses about 'Lunar effects
- 3. Birth data in France over 50 years
- 4. Least squares and statistical analysis

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Do french people here recognize him?



The new wave of flying saucers (Unidentified Flying Objects)

















UFOs came on Earth mainly in the 50-70's. In 2021, nobody seems to see them anymore...



Pendulum





"Sourcier" = Dowser








Cercle zététique (skeptical association that studies paranormal phenomena)

## The prevalence of beliefs is high

- Three out of four Americans believe in at least one unfounded concept (ghosts, witches, astrology, etc.).
- Four out of ten Americans think that humans have been created in the last 10,000 years.
- ▶ 6 percent of Americans think Apollo landings on the Moon are fake. (Margot, 2015)
- ▶ 80 % of nurses, and 60 % of doctors, in emergency units, think the moon has an effect on patients.

(Daniel F. et col, 1986)

So we should like to find a way to study paranormal phenomena and extraordinary beliefs.

There is one belief that can be tested. For which there is data, accurate and in large numbers. The civil registry office and the national statistics institute (INSEE) collect birth data.

## Why should we be interested in beliefs and test them?

For brain hygiene.

« Allowing our brain to develop beliefs that contradict indisputable facts is bad brain hygiene » (Margot, 2015)

> Brush your teeth for oral hygiene. Think properly to avoid smelling bad brain.

## Misconceptions have a huge cost

Health professionals have difficulty containing a measles outbreak due to questionable beliefs about vaccine safety. Yet vaccines are widely considered to be one of the greatest public health achievements, but vaccine-preventable diseases kill people because of beliefs that are not in line with scientific evidence. In 2018 in France : 2,800 cases of measles (90 % not vaccinated), including 3 deaths.

Imminent extinction of the northern white rhino (horns), mutilation of reindeer (antlers), sharks (fins), seals (penises) etc... due to superstition of their alleged aphrodisiac character

(thanks to the inventors of molecules such as Viagra, Tadalafil...)

Many species are becoming extinct or decreasing sharply, huge population displacements will occur, due to climate sceptical beliefs.

In 2021, coronavirus antivax people have a cost : some of them will spend some time in intensive care units at hospital, other will miss work, etc.

## Probabilities and statistics

All this has to do with statistics :

- statistics are a way to thwart illusions

- statistics make it possible to analyse observations rationally.

## Statistics is not always intuitive

Which square is filled the most randomly? Left or right?





 $\mathsf{Uniform} \neq \mathsf{Random}$ 

## **Apparent Miracles**

 $\ll$  An abandoned dog 100 km away finds his home !  $\gg$ 

100,000 abandoned dogs and cats every year.

Let's say they are abandoned *averages* 100 km from home. And that they know the environment of their home about 100 m away, which means that if they get within 100 m of home, they are sure to find their master.

Suppose, as a skeptic, that an abandoned dog goes in a totally random direction ! And that 1 in 10 dogs will wander at least 100 km.

So, the expected number of dogs returning home each year is

 $(100,000/10) \times (2 \times 0.1/100)/(2\pi) = 3.$ 

This return makes the headlines in the local newspapers.

However, we can see that they are not so improbable (in France and over a year).

## Correlation and causality

60 % of deaths occur in hospitals or clinics, 25 % at home, 13 % in a retirement home. 2 % elsewhere.

Thus, hospital kills.

## Correlation and causality

Suppose we find that :

heavy coffee drinkers have more cancers than the average population. What should we conclude? Many studies have found a positive association between coffee and cigarette consumption.

An epidemiological study found an extremely strong correlation (r = 0.99) between number of cigarettes and the number of cups of coffee consumed. This correlation is not found with the tea.

- 38 % of smokers of both sexes are heavy consumers of coffee, compared to 12 % and 16 % for non-smokers, depending on gender.
- $\ll$  It must therefore be concluded that there are factors in coffee that stimulate smoking consumption, and that it is not caffeine, which would rather be tendency to limit it.  $\gg$

http://www.tabac-humain.com/wp-content/uploads/2011/07/Tabac-et-Cafe.pdf

## 2. Existing studies about 'Lunar effects'

## Meta-analysis and reviews

#### The Moon Was Full and Nothing Happened: A Review of Studies on the Moon and Human Behavior and Human Belief

by I.W. KELLY, JAMES ROTTON, and ROGER CULVER

Current Biology 18, R764-R794, September 9, 2008 (12008 Elsevier Ltd All rights reserved DOI 10.1016/j.cub.2008.07.003

#### Human Responses to the Geophysical Daily, Review Annual and Lunar Cycles

Russell G. Foster<sup>1</sup> and Till Roenneberg<sup>2</sup>

an internal ~24 hour circadian timer in anticipation of the

Table 1. Pathologies and some physiological and behavioural phenomena in humans which have been linked to the lunar cycle but which in reality occur independently of the phase of the moon.

Psychological Bulletin 1985 Vol. 97 No. 2, 286-386 Copyright 1985 by the American Psychological Association, Inc. 2011;2109(45550) 2

#### Much Ado About the Full Moon: A Meta-Analysis of Lunar-Lunacy Research

James Rotton Florida International University I. W. Kelly University of Saskatchewan Saskatoon, Saskatchewan, Canada

Data from 37 published and unpublished studies were combined in a meteanglysis that catanine bases of public of the motors, per of hang cycle, several types of hangs, including mental hospital administens, poychatre datarubances, cristi calla, buncidos, and other criminal offstess. Although a few drifte motos successful and the several several several several drifte motos successful and the several several several several trend hangs. Algebra draftes between the other (a several trend hangs. Algebra draftes) between the other (a several term data several several several several several term data several several several several several several hospital several severa

Condition/event with no consistent lunar influence	Reference
Psychosis, depression, anxiety	[67-75]
Violent behaviour/aggression	[76-80]
Seizures	[81]
Suicide	[79,82-87]
Absenteeism rates	[88]
Coronary failure	[89]
Conception (in vitro fertilization)	[90]
Birth	[91-93]
Menstruation	[94]
Surgery and survival of breast cancer	[95]
Postoperative outcome (general)	[96-98]
Renal colic	[99]
Outpatient admissions (general)	[100]
Automobile accidents	[101,102]

# For example, human copulation frequencies and lunar rhythms

# Diurnal and Weekly, But No Lunar Rhythms in Human Copulation

By John D. Palmer,<sup>1</sup> J. Richard Udry<sup>2</sup> and Naomi M. Morris<sup>3</sup>

#### ABSTRACT

Using the copulation times from 78 White married women, representing an average of 72 reporting days per woman over a 12-month period, two expected prominent copulatory rhythms were found and described quantitatively. The daily rhythm is characterized by a major evening peak, which encompasses 58% of the daily copulations, and a minor peak in the morning. The weekly rhythm describes a rather constant copulatory rate during weekdays, with a large increase on weekends. The probability of orgasm was found to be significantly greater in copulations taking place after midday. Because of the long-time speculation that the moon plays some role in the timing of human love-making, the data were examined for such a relationship. None was found.

Human Biology, 1982.

1230 copulations, 48 couples, 3rd sept. - 2nd dec. 1973 711 copulations, 30 couples, 8th juin - 5th sept. 1974



FIG. 1. The mean weekly copulation rhythm of 78 women. The curve is based on 1,941 copulatory events. Standard errors indicate the relative significance of the daily means. The Sunday rate differs significantly from that of Saturday (P = <0.01), and the Saturday rate from any weekday (P = <0.01). The numbers displayed above each mean represent the day's percentage of the week's total number of copulations.



FIG. 2A. The average solar-day pattern for weekdays during three-month studies in 1973 and 1974. The 1973 curve is based on 744 copulations; the 1974 one on 451. The major peaks in both years encompass slightly over 60 percent of the daily copulations. A second, minor peak occurs at 7 AM.





FIG. 3. The mean solar- and lunar-day patterns of copulation based on all the data collected in both studies. A total of 5,584 "copulating-couple days," and 1,941 copulations were used in the construction of each curve. Representative standard errors are given on some points to indicate relative significance, or lack thereof, between points. UT = upper transit of the moon; LT = lower transit. The solar-day pattern emphasizes the presence of a population rhythm, characterized by a prominent peak between 10 PM and 1 AM which encompasses 56 per cent of the daily copulations. There is no indication of a lunar-day rhythm.

In a further analysis, the number of copulations which took place while the moon was above the horizon (i.e., the intervals between moonrise and moonset) were compared to the number when the moon was below the horizon (the times between moonset and moonrise). The copulation numbers were found to be 7.6% greater under the former condition, but the difference was not statistically significant (p = 0.2).

Next, copulation numbers as a function of the four major phases of the moon were examined. The average rate was found to be 14.6% greater for the 5-day intervals centered on full moon, than for the same intervals centered on the nights of first quarter of the moon (the two extremes in the average-monthly pattern). The difference was not significant (p = -0.1). It should be stressed that the large-amplitude weekly rhythm present in the data, would be expected to override any relatively small correlation that might exist between copulation rates and the moon's phases.



#### Time

FIG. 4. AM and PM comparison of orgasmic success during copulation for 30 women over 711 copulations. The fraction of the copulations in which orgasm was not attained is indicated by the shaded portion of the base of each bar.

In the 1974 study, the women recorded whether they had experienced orgasm during intercourse. As a group, they failed to reach orgasm in 29.4% of their encounters. The mean-daily curve of orgasm achievement was, unsurprisingly, quite similar in appearance to that for copulation, but showed important non-uniform differences in amplitude: greater orgasmic success was attained after midday. As seen in Fig. 4, between the hours of midnight and 11 AM, 38.6% of all copulation failed to result in orgasm for the women; but between noon and midnight, the rate improved significantly ( $X^2 = 17.9$ ; p = <0.001), the failure rate fell to 23.7%.

#### Studies about births and lunar cycle

#### First method : Fourier spectrum

### Naissances, fertilité, rythmes et cycle lunaire Etude statistique sur 5 927 978 naissances

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Département de Mathématiques, Faculté des Sciences d'Orléans.

#### RÉSUMÉ

Existe-t-il une liaison entre la survenue des naissances et le cycle lunaire synodique? Certains travaux ont déjà établi l'existence d'une telle liaison. Nous avons procédé à l'étude de 5 927 978 naissances françaises comprises entre le 1<sup>er</sup> janvier 1968 et le 31 décembre 1974. Par analyse spectrale de Fourier, il est mis en évidence deux rythmes dans la survenue des naissances :

- un rythme hebdomadaire caractérisé par un nombre minimum de nouveau-nés le dimanche et maximum le mardi;

- un rythme annuel, avec un maximum de naissances en mai et un minimum en septembre-octobre.

L'étude statistique de la répartition des nouveau-nés dans le cycle lunaire révêle un plus grand nombre de naissances entre le Dernier Quartier et la Nouvelle Lune et un-moins grand nombre autour du Premier Quartier. Les écarts entre la distribution observée dans la lunaison et la distribution théorique sons isguificatifs.

#### No pic at 29.53 days in the Fourier spectrum.

(J. Gynecol. Obstet. Biol. Reprod., 1986)

Moon synodic month = 29.53 days (time delay between two Full Moons)

# The Fourier spectrum is not always the best way to detect a periodicity



A sinusoid and a comb-like signal, with a period of one month (30 days)

#### I add a gaussian (and independent) noise :



Sinusoid + noise (blue) and a comb-like signal + noise (red) (the same noise on both)

#### I will not show it entirely every time, but I consider a long signal :



Sinusoid + noise (blue) and a comb-like signal + noise (red) (the same noise on both)

Which signal appears the best on the Fourier transform?

#### Fourier spectrum :



Fourier transform of sinusoid + noise (blue) and a comb-like + noise (red)

#### In that case, it is better to stack all the months :



Stack of sinusoid (blue) and a comb-like signal + noise (red)

With a smallest noise :



Sinusoid + noise (blue) and a comb-like + noise (red)

# The sinus is visible in the Fourier spectrum, but not the comb-like signal (Why?)



In case of moderate signal/noise ratio, we should do a statistical test to say what is the probability that a given pic could be in the spectrum by chance (i.e. with a random signal).

Stack :



### With an even smallest noise :



### Fourier spectrum :



Stack :



#### With a very small noise



### Fourier spectrum :



SLACK
-------


### Second method : stack (on the supposed period)



Fig. 4. — Répartition des naissances dans le cycle lunaire synodique, Chaque point de la courbe indique le nombre moyen d'enfants nés au cours d'une journée du cycle. La moyenne, qui est de 2196,7 enfants par jour, est réprésentée par le corcle.

Stacking on a month shows 'significant variations'.

(Guillon et al., Rev. Gynecol. Obstét., 1988)

$$\frac{{\sf But ! with a } \chi^2 {\rm ~square~test:}}{\chi^2 \propto \frac{{\sf Variance}({\sf Fluctuations~in~the~lunar~month}}{{\sf Variance}({\sf Multinomial~Law})}$$

Hypothesis = the random variables (= each birth) are independent and identically distributed (iid) ( = 'strong white noise'). Wrong !  $\chi^2$  square test inadequate here.

### Third method : stack and do Student, Fischer, ANOVA, and related tests

The plot below shows the result for all 20 years, about 70 million births. The standard deviation for this set of 28 points is about 5360 and is shown as an error bar at the data point for day 15.



Most of the points lie with one standard deviation of the mean, and all but one lie within two sigmas.

Caton D.B., 2002, Personal communication .

 $\label{eq:Test statistic} \ensuremath{\mathsf{Test statistic}} \propto \frac{\mathsf{Variance}(\mathsf{Fluctuations in the lunar month})}{\mathsf{Variance}(\mathsf{Fluctuations in the lunar days})} \\ \text{Hypothesis} = \text{the random variables } (= \text{number of births/days}) \text{ are independent} \\ \text{and Gaussian. A little bit wrong on raw data, might be true after having} \\ & \mathsf{cleaned' the data.} \end{aligned}$ 

Economics and Human Biology 11 (2013) 545-550



# The lunar cycle, sunspots and the frequency of births in Germany, 1920–1989

Thomas K. Bauer<sup>a,b,c</sup>, Stefan Bender<sup>d</sup>, Jörg Heining<sup>d,\*</sup>, Christoph M. Schmidt<sup>a,b,c</sup>

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#### ARTICLE INFO

### ABSTRACT

Article history: Received 10 April 2012 Received in revised form 22 November 2012 Accepted 24 November 2012 Available online 3 December 2012

JEL classification: 112 113

Keywords: Daily frequency of births Lunar cycle Sunspots Based on multivariate linear regression models, we analyze the effect of the lunar cycle and the number of sunposts occurring on a particular day on the number of births using social security data and controlling for a number of other potential confounders. The daily numbers of births between 1920 and 1998 have been calculated from the full sample of individuals who have been registered at least once in the German social security system. While the lunar cycle does not affect the number of births, the number of sunposts is positively correlated to the number of births. The empirical results may be explained by medical technological progress making natural influences on births less important over time. This interpretation is supported by the results on the intertemporal influence of weekends and holdings on the frequency of daily births.

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61.4 million births in Germany, period 1920-1989. No link between the number of births and the lunar phases.



Figure 6: Average value for the mean detrended daily number of births along the moon cycle (in days).

Charpentier, 2008, Charpentier et Causeur, 2009 <hal-00482743>.

 $\begin{array}{l} 30 \text{ M births, from 1968 to 2005.} \\ \text{Article in 2008}: \text{ more birth between FM-1 et FM+3}: p-value = 0,02. \\ \text{Article in 2009}: \text{ more birth (+9), between FM-3 et FM+2, on 8 \% about 469} \\ \text{ lunar cycles.} \end{array}$ 

3. Birth data in France during 50 years

### Data

### Number of births per day in metropolitan France

Total number without distinctions :

- natural triggers/activated triggers (20 %) /without trigger ('déclenchement')

nor

- natural/medicalized/caesarean delivery.













### Ratio of births on Sundays to births on weekdays



And the Moon?

## The tidal force is extremely low

The inclination and intensity of this force are very low.

 $\begin{array}{l} \mbox{The difference in water level is} \\ \approx 1 \mbox{ m over } 2000 \mbox{ km} = \mbox{angle of } 5.10^{-7} \mbox{ rad} = 0.00003 \\ \mbox{ (and 10 times less on the continents).} \end{array}$  Whether the inclination of the tidal force had an effect on the initiation of childbirth, so to have a baby, all you have to do is tilt your head.

The acceleration we experience due to the lunar tidal force is  $= 10^{-7}g$ . The acceleration of an elevator is calibrated to  $10^{-1}g$ , sometimes more.

Whether the intensity of the tidal force had an effect on the initiation of childbirth, so to have a baby, all you have to do is take the elevator.

# If the attraction of the Moon and the Sun influenced the number of births, then that number should have a period of 12 h 15



Gravity measurements over time

Main tide period : 12 h 15 (and 24 h 30). + Modulation of  $0.5 \times 29.53$  days.

# And the Moon phases?



Synodic lunar month = 29.53 days (variations <  $\pm$  6h) .

# Fourier transform



Fourier Transform around 29.53 days

Main problem : low signal/noise, and FFT not the most efficient in detecting noisy non-sinusoidal signals

# If there is an effect it is not obvious at all



Birth number as a function of the moon phase angle

Average birth number every  $12^{\circ}$  ( $\approx 1 \text{ day}$ )



There are a little more births on full moon days, but :

- it's very low (16 births out of 2121, or +0.8 %).
- can this be due to chance?
- or an interaction with weekly and annual fluctuations?
- no effect of moonlight (sinus + excess in 0)

1st problem. It is necessary to compare with statistical fluctuations (= standard deviation with a statistical test)



What is the probability that the observed statistics of +16 births on FM could have been produced by chance, given the fluctuations of  $\pm$ 240 births/day in the data ?

This probability is called a p-value.

The smallest is the p-value, the smallest is the probability of being wrong if you say 'my data have not been produced by the random process'.

Calculus : take numbers fluctuating with a standard deviation of  $\pm 240$ births/day, distribute them in 30 days randomly, do it a large number of times, and determine the proportion of times the full moon is > +16 births. More simple : you know the law of your random variable, you calculate its cumulative distribution function, and then its value for the computed statistic (here 16 -> 0.07).

You find : p-value(FM) = 0.07

You can also determine the probability that one of the 30 days has > +16 births : global p-value =  $1 - (1 - 0.07)^{30} = 0.9$ 





2nd problem. An ultra-simple deterministic model of births :



 $\pm$  7 births

Deterministic fluctuations (non random fluctuations) do not respect the conditions of statistical tests.

It is therefore necessary to remove deterministic fluctuations.

4. Statistical analysis

It is therefore necessary to :

- remove deterministic fluctuations : raw data  $\longrightarrow$  residuals
- perform a statistical analysis of the residuals : residuals  $\longrightarrow$  statistical tests



### Least squares

$$n(t) = \sum_{\omega_k} \left( a_k(t) \cos\left(\omega_k t\right) + b_k(t) \sin\left(\omega_k t\right) \right) + T(t) + (1 + K(t)) \sum_{\rho=1}^{r} \alpha_{\rho} I_{\rho}(t) + \epsilon(t)$$

with :

- $\begin{array}{ll} . & \omega_k = k \times \frac{2\pi}{7 \text{ days}} & k \in \mathbb{N} \\ . & \omega_{k'} = k' \times \frac{2\pi}{365, 25 \text{ days}} & k' \in \mathbb{N} \end{array}$
- .  $\omega_{k''} = \omega_k \pm \omega_{k'}$
- . T(t) is the long-term tendency ,
- $\begin{cases} I_p(t) = 1 & \text{if } t \text{ is the particular day } p, \\ I_p(t) = 0 & \text{otherwise}, \end{cases}$
- .  $\alpha_p$  is the corresponding coefficient.
- . K(t) long-term modulation of particular days.
- . r(t) are the (Gaussian) residuals.



п

## Least squares

$$n(t) = \sum_{\omega_k} \left( a_k(t) \cos(\omega_k t) + b_k(t) \sin(\omega_k t) \right) + T(t) + (1 + K(t)) \sum_{\rho=1}^{P} \alpha_{\rho} I_{\rho}(t) + r(t)$$

$$n = g(m) + r$$

$$n \in \mathbb{R}^{18,263} = \text{data (observations)}$$
  
 $m \in \mathbb{R}^{12.3 \text{ million}} = \text{model (parameters)}$   
 $r \in \mathbb{R}^{18,263} = \text{residuals supposed random gaussian}$ 

Tarantola, A., Valette, B., Rev. Geophys. Space Phys. 20 (1982).

$$n = g(m) + r$$

Find *m* that minimises :

$$||r||^{2} = r^{T}C_{n}^{-1}r = (n - g(m))^{T}C_{n}^{-1}(n - g(m))?$$

Underdetermined !

Better find the smallest m too :

 $||r||^{2} + ||m||^{2} = r^{T}C_{n}^{-1}r + m^{T}C_{m}^{-1}m = (n - g(m))^{T}C_{n}^{-1}(n - g(m)) + m^{T}C_{m}^{-1}m$ 

We know how to find a minimum. For example with Newton iterative scheme on the derivative :

$$\hat{m}_{k+1} = C_m G_k^T \left( C_n + G_k C_m G_k^T \right)^{-1} \left( n - g(\hat{m}_k) + G_k \hat{m}_k \right)$$
with  $G_k = \frac{\partial g}{\partial m}(\hat{m}_k)$ .

Decomposition of the signal

$$n(t) = \sum_{\omega_k} \left( a_k(t) \cos(\omega_k t) + b_k(t) \sin(\omega_k t) \right) + T(t) + (1 + K(t)) \sum_{p=1}^{P} \alpha_p I_p(t) + r(t)$$







Histogramms of raw data and of residuals



# Particular days in the year?

$$n(t) = \sum_{\omega_k} \left( a_k(t) \cos(\omega_k t) + b_k(t) \sin(\omega_k t) \right) + T(t) + (1 + K(t)) \sum_{\rho=1}^{P} \alpha_\rho \, I_P(t) + r(t)$$

# Particular days and holidays in the year

N°	Day	Event	Average deficit
			of birth
Fixed date holidays			
1	January 1	New year	-466
2	May 1	Labour day	-389
3	May 8	Surrender of Germany	-457
4	July 14	National Day	-393
5	August 15	Assumption	-340
6	November 1	All Saints	-356
7	November 11	Armistice	-372
8	December 25	Christmas	-491 (-23 %)
Mobile holidays			
9		Easter Monday	-364
10		Ascension Thursday	-391
11		Whit Monday	-388
Other particular days			
12	January 2	New Year's Next day	-115
13	December 22	J-3 before Christmas	-64
14	December 23	J-2 before Christmas	-107
15	December 24	Christmas Eve	-214
16	December 31	New Year's Eve	-149
17	Extra long weekend	Monday or Friday	-71
18	Friday 13	Superstition	-43
19	February 29	Leap day	-117
20	February 14	Valentine's Day	+23
21	Last Sunday in March	Switch to summer time	-59 (- <mark>3 %</mark> )
22	Last Sunday in October	Switch to winter time	+38 (+2 %)

p-values : all  $< 1.5 \times 10^{-6}$  except Switch to winter time  $= 6 \times 10^{-4}$  and Valentine's day = 2 %. bigskip Superstition may affect the number of births since a deficit of birth appears in some days when the medical staff is a priori as numerous as the other days (Friday 13, Leap day)

### Paraskevidékatriaphobie (\*)



Operating rooms, Médipole, Villeurbanne, 2019

(\*) Phobia for the friday the 13th.



Birth residulas as a function of the lunar phase


Significant excess of births at FM and FM+1

Global test (test if all means = 0)

Test statistic : 
$$S = \frac{\text{variance between lunar days}}{\text{variance inside lunar days}} \approx 2.46$$
  
p-value(global) =  
Fischer cum. distrib. function (x = 2.46, deg. freedom = 30 and 18233) =  
=  $1.5 \times 10^{-5}$ 



#### Full moon day (test if mean(FM)=0)

Test statistic :  $S = \frac{\text{mean}(FM)}{\text{standard deviation}(FM)} \approx 4.42$ 



Correction for multiple testing also called Family-Wise Error Rate

Probability than one mean over 30 has a statistic  $\geq$  4.42 :

Corrected p-value(FM) =  $1 - (1 - \text{pvalue})^{30}$ =  $4 \times 10^{-4}$ 



Corrected p-values are all greater than 80 % except three : p-value(FM) =  $4 \times 10^{-4}$ , p-value(FM+1) =  $4 \times 10^{-3}$ , and p-value(FM+11) =  $2 \times 10^{-2}$ .

It is very unlikely that the excess at FM and FM+1 is due to the random fluctuations of the number of births throughout days.

# Isolated special days? (outliers)



# Isolated special days ('outliers')

Day	Event	Diff. of birth
Wednesday, July 16, 1969	Launch of Apollo 11	+216
Sunday, May 4, 1975	Extra long week-end	-205
Friday, July 15, 1977	Extra long week-end	-222
	between July 14th and the weekend	
Tuesday June 30, 1987	First day of summer holidays	+288
	the next day	
Friday, January 6, 1989	Weekend vigil	+254
	(return from vacation on the 5th)	
Friday, December 27, 1991	Weekend vigil in Christmas time	+185
Thursday, October 17, 1996	Public Service Strike	-199
Wednesday, August 11, 1999	Solar Eclipse	-237
Friday, December 31, 1999	Millennium New Year's Eve	-213
Monday, March 19, 2001	Midwives' Strike the next day	+203
Tuesday, March 20, 2001	Start of midwives strike movement	-339
Saturday, July 14, 2007	National holiday after a Friday 13	+263

Table – Days for which the residuals were greater than 3 standard deviations after a first application of the least squares program and for which we found an event that could influence the number of births on that day. In a second least squares step, we corrected the 12 data corresponding to these dates by the values indicated in the second column of the table. The residuals corresponding to the sum of the two stages of the least squares.

Individual p-values all  $< 6.10^{-5}$ .

Corrected, for multiple testing, p-values are smaller than 1 % only for the five days when Diff. > 237.

## Observation time and size required

- With the raw data, the probability that the peak of births on the FM day is due to chance is 7 %. It's too big to conclude that it's significant.
- To fall to a probability of 0.001, always at the rate of 2000 births per day, it would take 200 years to observe !
- By processing the data well (residuals), it only takes 40 years.
- This increase in the number of births at the FM (+8 births for an average of 2121) is therefore totally undetectable in a maternity ward (10 births/day), or in a city, even over a lifetime !
- A belief that is not based on any observation.

# Conclusions

- Significant variations in the number of births during the year  $(\pm 20 \%)$
- Significant decrease during week-ends and holidays (-20 %)
- Slight increase on FM and FM+1 days (+0.4 %)
- No significant variation on the other days of the lunar month; so lunar light doesn't seem to be a triggering factor.
- Neither is the attraction, otherwise the period would be 12 h 15.
- This increase is totally undetectable unless you have a lot of data and do a lot of statistical work.
- The number of medical staff affects the number of births
- Medical staff believes in the lunar effect
- Some maternity hospitals have (might have) more staff on full moon days !?

The excess of births at the FM might be a self-fulfilling prophecy.

Staff belief ⇒ more staff at the FM ⇒ more births.

Self-fulfilling prophecies are everywhere :

. Teachers towards the students

(information received  $\rightarrow$  differentiated expectations and attention),

. Economic agents (announce a price increase, stock market...),

. War or peace (hostility or supposed kindness of the other),

. Placebo/nocebo effect...

## Thanks!

