

TP 3h Résonance

Introduction :

$$\frac{d^2x}{dt^2} + B \frac{dx}{dt} + \omega_0^2 x = E(t)$$

$$B = \left| \frac{2\gamma}{\omega_0} \right|$$

$$m \frac{d^2x}{dt^2} + 2\gamma \frac{dx}{dt} + kx = A \sin \omega t \quad \left| \gamma' = \frac{\gamma}{m} \right|$$

$$\omega_0' = \sqrt{\omega_0^2 - \gamma'^2}$$

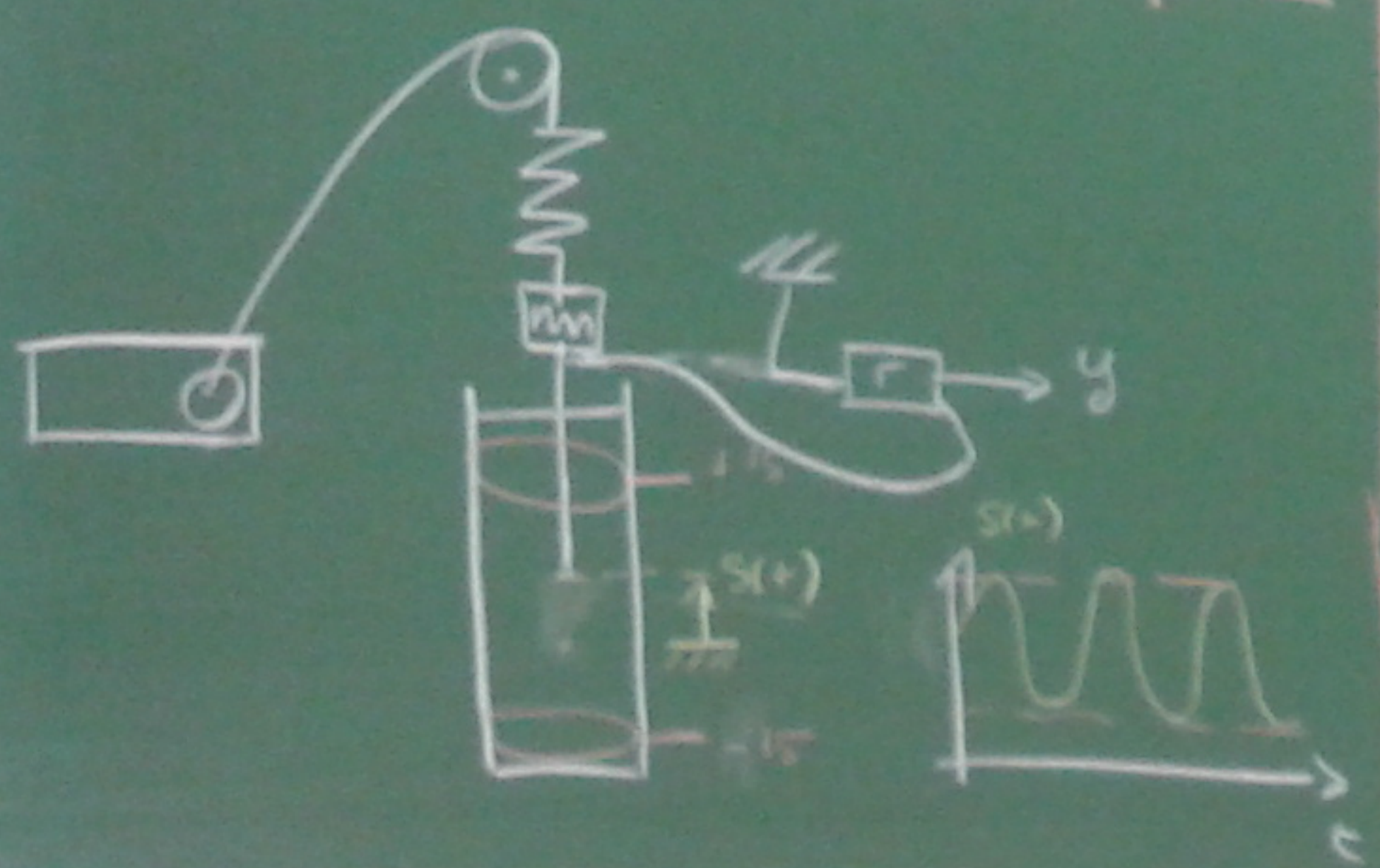
$$\omega_0 =$$

$$\omega_0' =$$

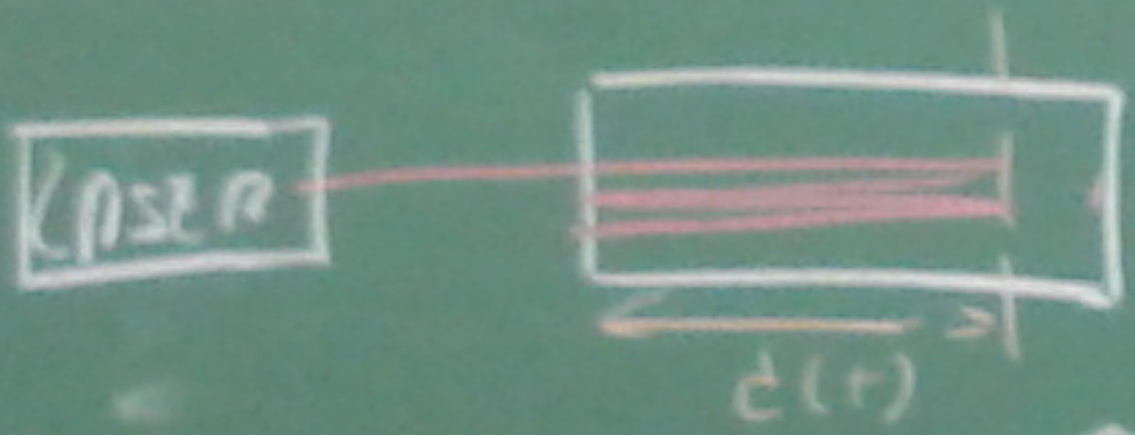
$$\gamma' =$$

I La Résonance : Instrument de mesure

a) Étude d'un système mécanique

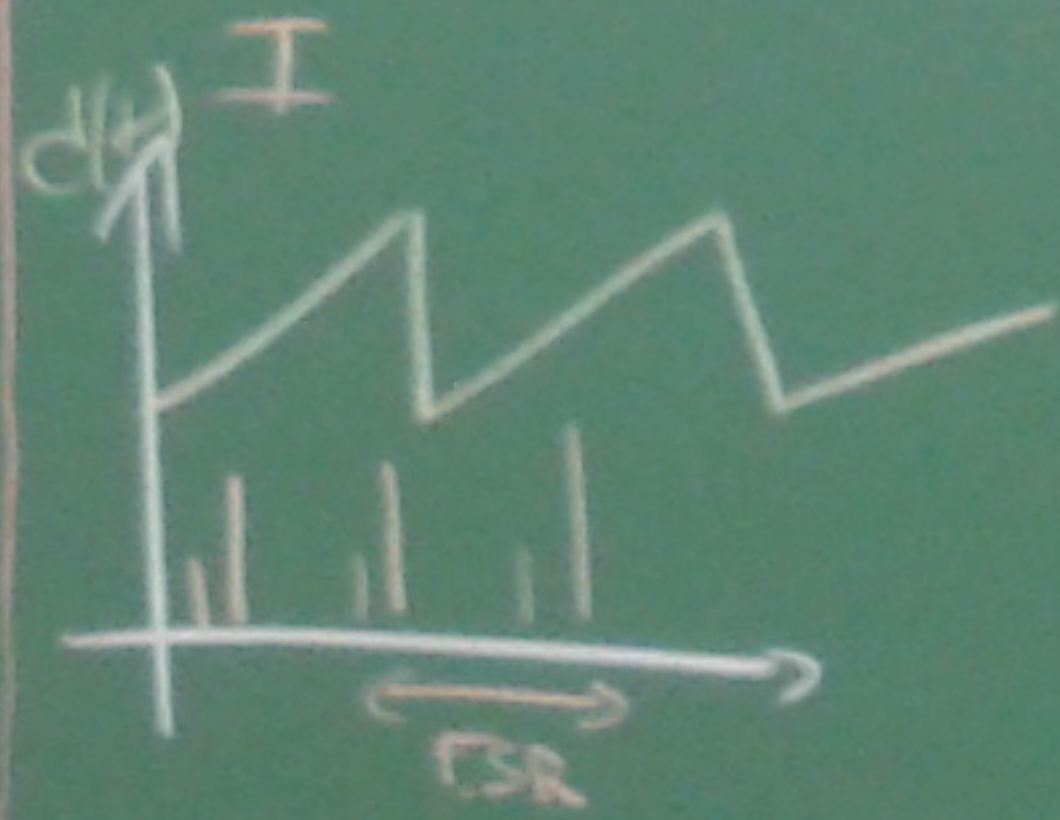


b) Résonance optique



$$I = \frac{1}{1 + T^2 - 2T \cos \theta}$$

$$\theta = \frac{8\pi d}{\lambda} \quad I_{max} \leftrightarrow d = \frac{\lambda}{4}$$

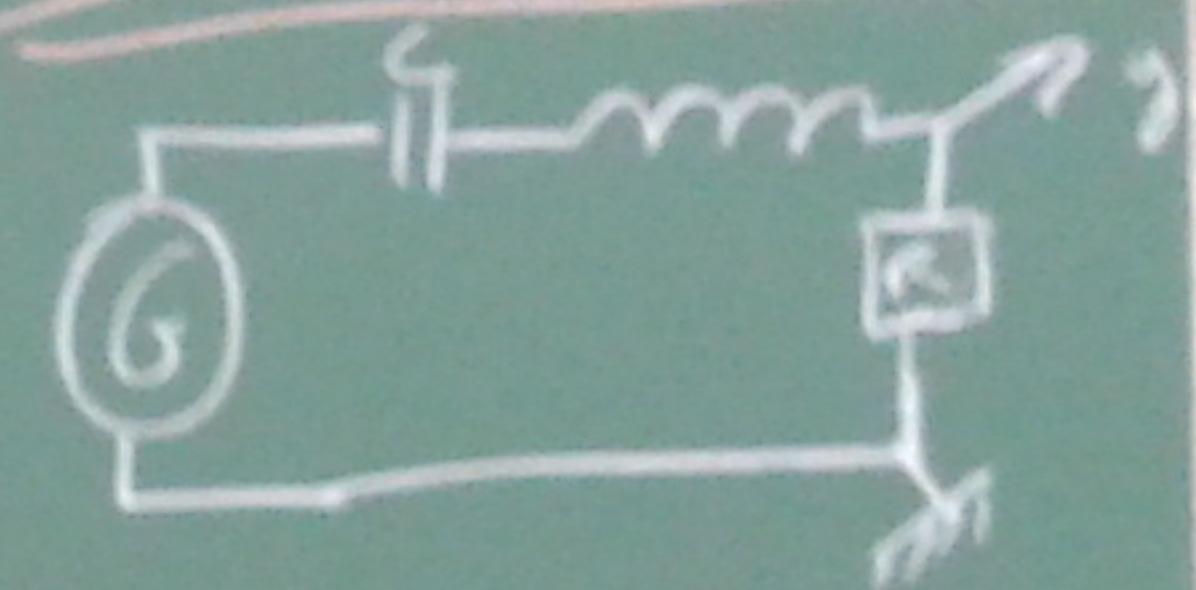


$$FSR \rightarrow 2GHz$$

$$\Delta t =$$

$$\Delta v =$$

C) Mesure d'une



$$I = \frac{U_e}{R \left(1 + jQ \left(\frac{\omega}{\omega_0} - \frac{\omega_0}{\omega} \right) \right)}$$

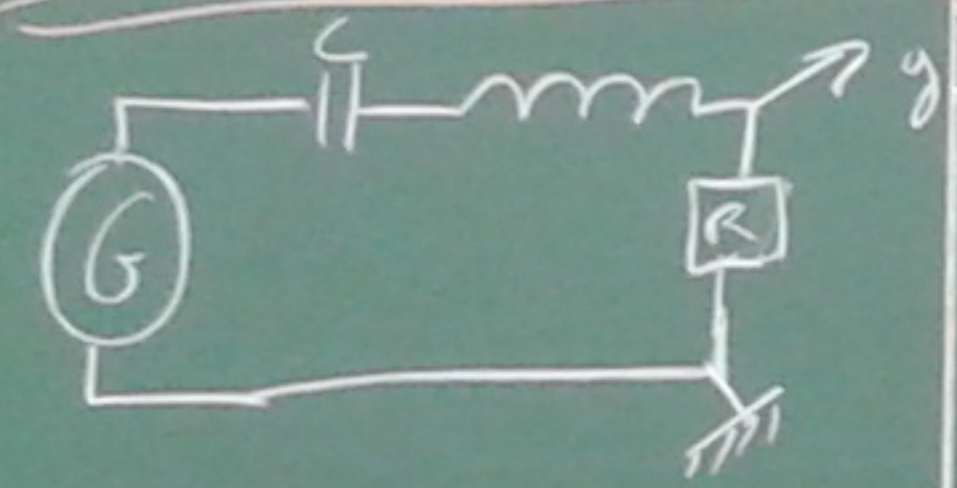
II La Résonance

a) Un phénomène

Cas du haut parleur



c) Mesure d'une Inductance



$$C = 0,101 \mu F$$

$$R = 124,1 k\Omega$$

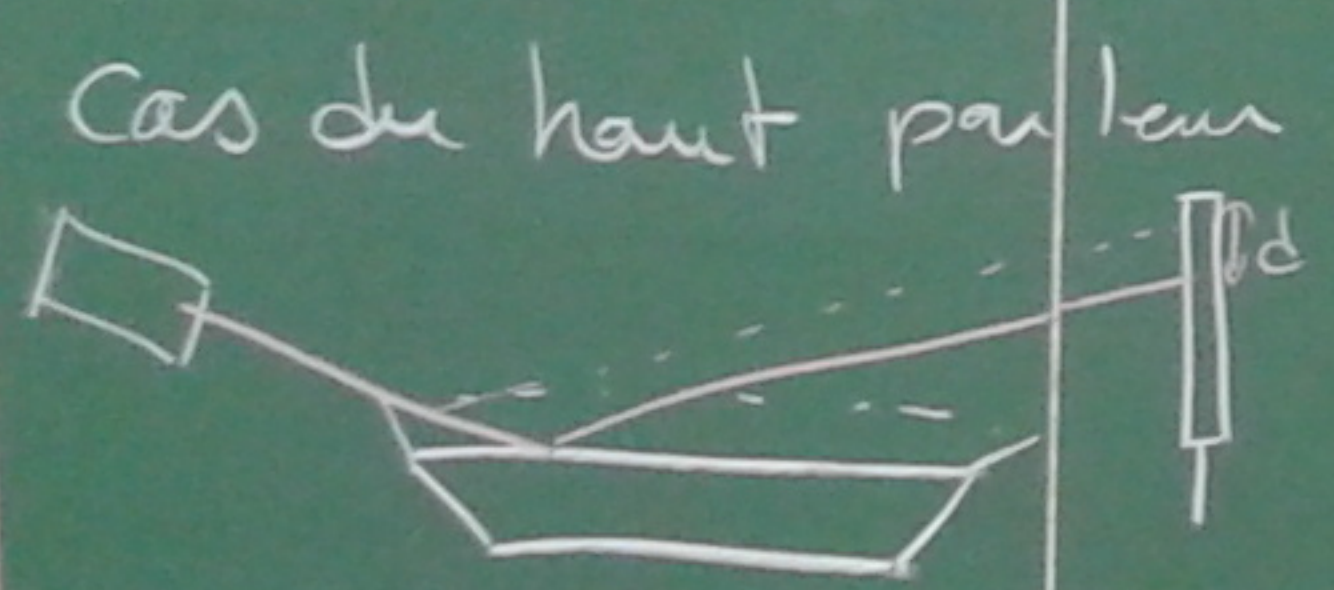
$$I = \frac{U_e}{R(1 + jQ(\frac{\omega}{\omega_0} - \frac{\omega_0}{\omega}))}$$

$$f_0 = \frac{1}{2\pi\sqrt{LC}}$$

$$L = \frac{1}{4\pi^2 f_0^2 C}$$

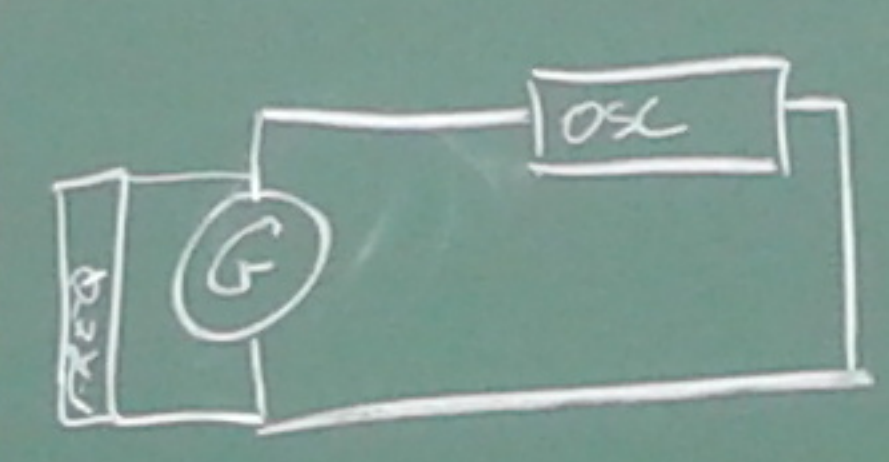
II La Maîtrise de la Résonance un enjeu majeur

a) Un phénomène gênant

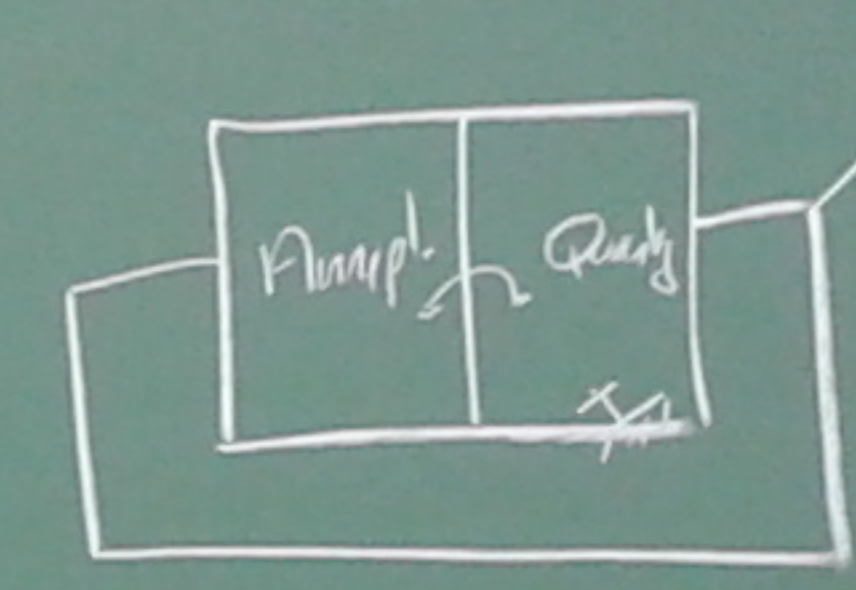


$$f_0 =$$

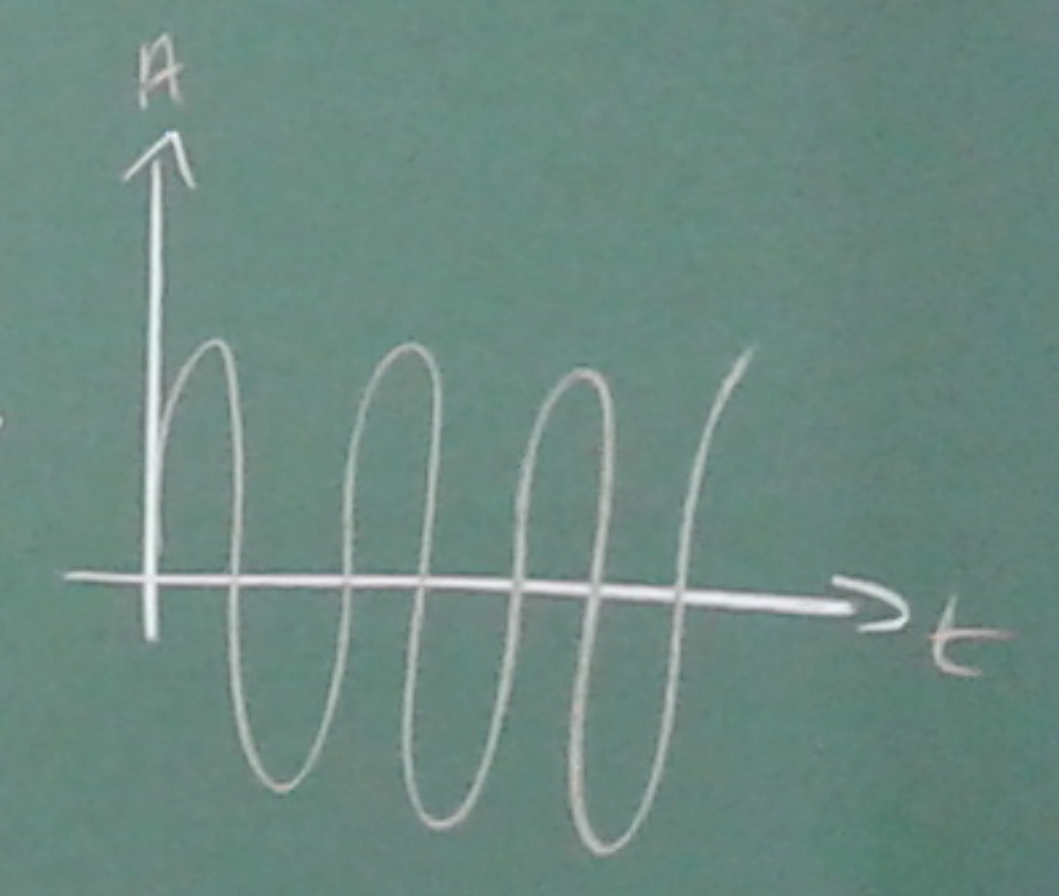
b) Fabrication d'une horloge



Boucle ouverte

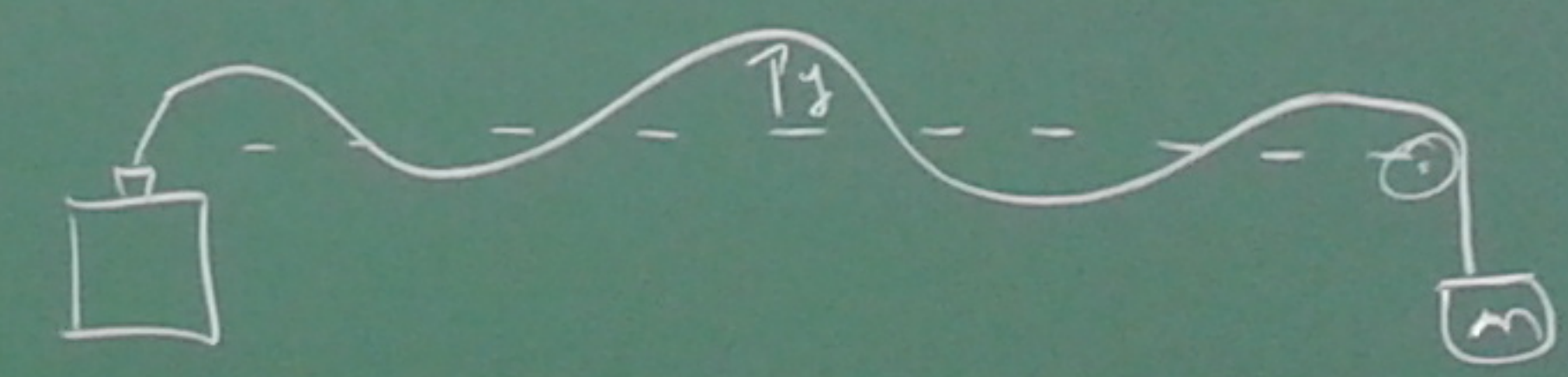


Boucle Fermée



c) Application musicale

$$L = 19 \mu m$$



$$C = \sqrt{\frac{T}{\mu}}$$

$$\mu = (1,29 \pm 0,13) 10^{-3} kg/m$$

$$\frac{d^2 y}{dx^2} - \frac{1}{c^2} \frac{d^2 y}{dt^2} = A \sin(\omega t)$$

$$\omega_n = \frac{n\pi c}{L}$$

$$y = C \cos(\omega t) \frac{\sin(\frac{\omega}{c}(L-x))}{\sin(\frac{\omega L}{c})}$$