

Impromptu Tensor Discussion

CSE17

MARCH 2, 2017

CROWD-SOURCED TALK

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Why tensors? Current Applications? Future Applications?

- Quantum chemistry
- Data analytics
- Statistics
- Engineering
- Health care analytics
- Sparse versus dense
- PDEs with unknowns that are tensors – operator theory
- Multi-fidelity, associated with rank, rare events – Modeling rare events

Key Kernels/Computational Bottlenecks/Data Structures

- MTTKRP
- TTM
- Matricization/unfolding
- SVD of unfolded tensor
- In-place algorithms (i.e., avoid data movement)
- Coupled tensor decomposition – bringing in different types of constraints
- Tensor contractions for dense, sparse, and block sparse
- Methods including permutational symmetry
- Data structures for sparse tensors
- Khatri-Rao product – not tensor operation but sometimes need to build it explicitly
- Need interface standardization ala BLAS
- How to optimize operations in a general framework for dense, sparse, symmetric, etc.

Needed Understanding, Algorithms, Methods

- Streaming data – network data, partial computation?
- Updating tensor decomposition
- How to choose the data layout for general sparse tensor?
- Tensor completion – how many samples do you really need?
- Sparsity-preserving computations – sparse factors
- Global optimization

Theoretical, Algorithmic, Understanding Challenges?

- Rank estimation
- Connections between tensors & deep learning (new program just started in Moscow!)
- Use of tensors inside neural networks
- Alternative decomposition algorithms – beyond ALS
- DMRG/Tensor Train in quantum – why does it work so well? How to expand to other tensor networks?
- Theoretical framework to understand how to do the quantization
- Visualization of factorizations?
- Also, how to identify what the components mean, choosing constraints, etc. Maybe a generic framework.
- Which model to choose for which application? Choose based on fit? Based on interpretability?

What Training for Tensors?

- Are there things we can do to cross pollinate between tensor contraction and tensor decomposition folks?
 - Dimensions, contractions, ranks
 - Explicit labeling of modes/Einstein notation
 - Explicit translation paper? Workshop? (NSF workshop in May??)
- Need listing of existing books and survey papers
- Need better Wikipedia articles!
 - “Tensor” is polymorphic
- Recommended coursework
 - Numerical linear algebra
 - Optimization
 - Differential geometry
 - Selected topics in biomedical data processing – subspaces with interpretation
- TensorFlow tutorials for MD arrays