gfun[listtoalgeq] - find an algebraic equation satisfied by a generating function

gfun[seriestoalgeq] - find an algebraic equation satisfied by a series

Calling Sequence

listtoalgeq (l, y(x), <[typelist]>)

seriestoalgeq (s, y(x), <[typelist]>)

Parameters

list
 s - series
 y,z - name of the unknown function and the generic variable
 [typelist] - (optional) list of generating function types

[typelist] = (opuonal) list of generating function v_{j}

Description

- The procedures **listtoalgeq** and **seriestoalgeq** compute a polynomial equation in y and x satisfied by the generating function y(x) of the expressions in l or s, this generating function being of one of the types specified by **typelist**, for example, ordinary (ogf) or exponential (egf). For a full list of available choices see <u>gftypes</u>).
- If typelist contains more than one element, these types are tried in order.
- If **typelist** is not provided, the default **optionsgf=['ogf','egf']** is used. The output is a list whose first element is the polynomial in **y**(**x**) and **x** that was found, and whose second element is the type to which it corresponds.
- In the current implementation, the maximal degree of y is 6 and the maximum degree of the coefficients is 3. This can be changed by modifying the variables <u>gfun[maxdegeqn]</u> and <u>gfun[maxdegcoeff]</u>.
- If sufficiently many terms are given, and no solution is found, then generating function does not satisfy any algebraic equation of degree less or equal to <u>gfun[maxdegeqn]</u> with coefficients of degree less or equal to <u>gfun[maxdegcoeff]</u>.

Examples

> with(gfun): l:=[1, 1, 2, 5, 14, 42, 132, 429, 1430, 4862, 16796, 58786]: listtoalgeq(l,y(x));

$$[-1 + y(x) - xy(x)^2, ogf]$$
 (2.1)

> s:=series((1-sqrt(1-4*x)),x,9);

$$s := 2x + 2x^{2} + 4x^{3} + 10x^{4} + 28x^{5} + 84x^{6} + 264x^{7} + 858x^{8} + O(x^{9})$$
(2.2)

 $s := 2x + 2x^2 + 4x^3 + 10$ > seriestoalgeq(s,y(x));

$$[4x - 2y(x) + y(x)^{2}, ogf]$$
(2.3)

See Also gfun, gfun[parameters]