

Bounded Sort Polymorphism with Elimination Constraints

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A Bit of a Dry Start, Right?

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Elder's Wisdom

'Avoid requiring something to be stated more than once; factor out the recurring pattern.'

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- ▶ higher-order functions,
- ▶ polymorphism,
- ▶ etc.

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That was before multi-sorted type theories *join the battle*.

Multi-Sorted What?

Setting:

$$t, u ::= x \mid t \ u \mid \lambda x. t \mid \Pi(x : t). u \mid \text{Type}_\ell$$

+ inductives and records (and their introduction/elimination).

where

- ▶ x is a variable
- ▶ ℓ is a universe level

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- ▶ s is a sort in \mathbb{G}
- ▶ a distinguished sort Type s.t. $\vdash \mathcal{U}_\ell^s : \mathcal{U}_{\ell+1}^{\text{Type}}$,
- ▶ predicative sorts \mathbb{G}_P ,
- ▶ impredicative sorts \mathbb{G}_I .

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- ▶ impredicative sorts \mathbb{G}_I .

By s_I impredicative, we mean:

$$\frac{\Gamma \vdash A : \mathcal{U}_\ell^s \quad \Gamma, x : A \vdash B : \mathcal{U}_{\ell'}^{s_I}}{\Gamma \vdash \Pi(x : A). B : \mathcal{U}_{\ell'}^{s_I}}$$

Ground sorts:

- ▶ Agda: $\mathbb{G}_P = \{\text{Set}, \text{Prop}\}$, $\mathbb{G}_I = \emptyset$,
- ▶ Lean: $\mathbb{G}_P = \{\text{Type}\}$, $\mathbb{G}_I = \{\text{Prop}\}$,
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Induce a small restriction: cannot create computational content from proofs.

Wet Toes in this Dry Afternoon

In practice,¹ also leads to the *dreaded* duplication:

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Inductive sum (A B : Type) : Type :=  
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Inductive sum (A B : Type) : Type :=
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Inductive sumbool (A B : Prop) : Prop :=
  | left : A → sumbool A B
  | right : B → sumbool A B.
Inductive or (A B : Prop) : Prop :=
  | introL : A → or A B
  | introR : B → or A B.
```

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Not All Heroes Wear Capes

Poiret et al. saved us from this world of suffering with `SortPoly`:

Inductive `sum@{sl sr s ; ul ur}`

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(A :  $\mathcal{U}@{sl ; ul}$ ) (B :  $\mathcal{U}@{sr ; ur}$ ) :  $\mathcal{U}@{s ; \max(ul, ur)}$  :=  
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“Universe Levels”

- ▶ **Universe level** polymorphism: Sozeau and Tabareau, 2014.

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Inductive $\text{sum}@{\text{sl} \text{ sr} \text{ s}; \text{ul} \text{ ur}}$
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| inl : $A \rightarrow \text{sum } A \text{ } B$
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“Sorts”

- ▶ **Universe level** polymorphism: Sozeau and Tabareau, 2014.
- ▶ In 2025, Poiret et al. bring *prenex* **sort** polymorphism.

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But this is not enough to avoid duplication!

A Non-Improved Situation

With unbounded sort polymorphism: cannot define *e.g.*, a generic eliminator:

```
Definition sum_elim@{sl sr s s'}
  {A : U@{sl}} {B : U@{sr}} {C : sum@{sl sr s} A B → U@{s'}}
  (u : sum@{sl sr s} A B) (f : forall (x : A), C (inl x))
  (g : forall (y : B), C (inr y)) : C u :=
  match u with
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Otherwise, setting $s := \text{Prop}$ and $s' := \text{Type}$ makes the type theory inconsistent (e.g., Hurkens). It is also the case when setting $s := \text{SProp}$.

Still need to declare the different eliminators “by hand”.

Contributions

In `SortPoly`, no principal sort assignment for e.g.:

```
Fixpoint map {A B} (f: A → B) (l: list A): list B :=  
  match l with [] ⇒ [] | a :: t ⇒ f a :: map f t end.
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We introduce a bounded sort-polymorphic type system such that it:

- ▶ allows writing the most generic terms (w.r.t. sorts),
- ▶ allows inferring the principal sort assignment,
- ▶ has relative consistency (w.r.t. `SortPoly`),
- ▶ has the *same* logical power as `SortPoly`.

The Missing Ingredient

Our proposal: interactions between sorts using *elimination constraints*.

Definition $\text{sum_elim}@\{s_l \text{ } s_r \text{ } s \text{ } s' \mid s \rightsquigarrow s'\}$

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Our proposal: interactions between sorts using *elimination constraints*.

Definition $\text{sum_elim}_{\{s_l \text{ sr } s \mid s \rightsquigarrow s'\}}$

$\{A : \mathcal{U}_{\{s_l\}}\} \{B : \mathcal{U}_{\{s_r\}}\} \{C : \text{sum}_{\{s_l \text{ sr } s\}} A B \rightarrow \mathcal{U}_{\{s'\}}\}$

$(u : \text{sum}_{\{s_l \text{ sr } s\}} A B)$

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Definition sum_elim@{sl sr s s'|s ~> s'}
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Naturally models existing systems:

- ▶ Agda: $\text{Set} \rightsquigarrow \text{Set}, \text{Set} \rightsquigarrow \text{Prop}, \text{Prop} \rightsquigarrow \text{Prop},$
- ▶ Lean: $\text{Type} \rightsquigarrow \text{Type}, \text{Type} \rightsquigarrow \text{Prop}, \text{Prop} \rightsquigarrow \text{Prop},$
- ▶ Rocq: reflexive and transitive closure of $\text{Type} \rightsquigarrow \text{Prop}, \text{Prop} \rightsquigarrow \text{SProp}.$

I Plead Guilty

Elimination constraints are not so innocent:

Lemma `guilty@{s | SProp \rightsquigarrow s} : forall {A : \mathcal{U} @{s}} (x y : A), x = y.`

Proof.

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set f : bool@{SProp}  $\rightarrow$  A :=
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```
fun b  $\Rightarrow$  match b with true  $\Rightarrow$  x | false  $\Rightarrow$  y end.
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`(* No more goals. *)`

Qed.

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\Rightarrow for the typechecking to be right, have to inherit conversion rules!

A Funny Theorem

Theorem

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Let's talk about the required conditions.

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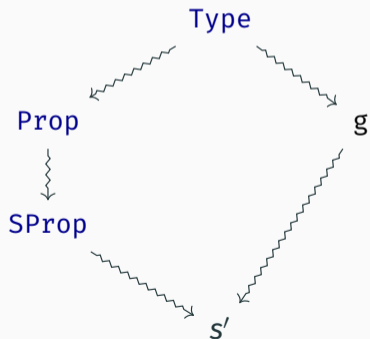
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Works, but not alone: need conditions.

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Introducing Domination (◌) (◌)

Second attempt: take minimal ground g s.t. $g \rightsquigarrow s'$.

Does not always exist!

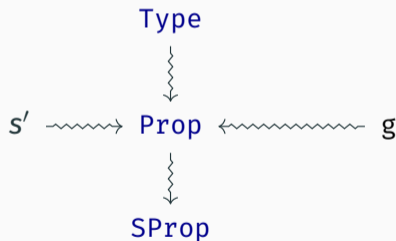
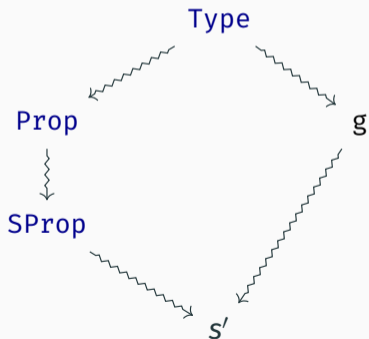


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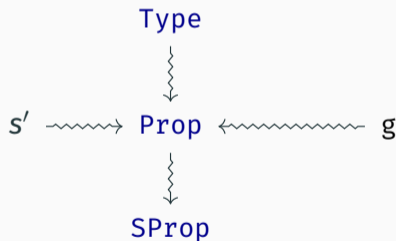
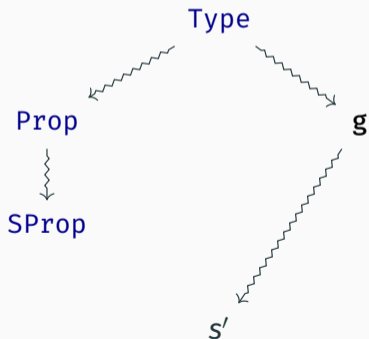


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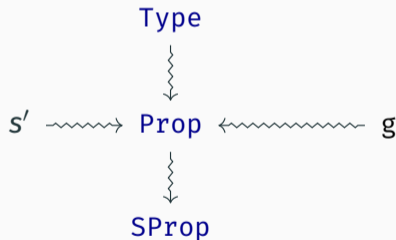
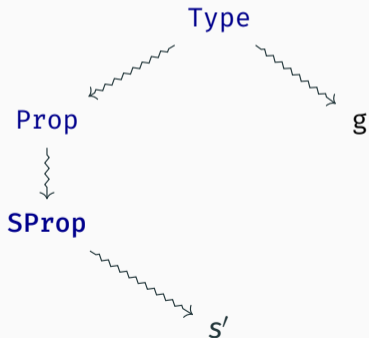


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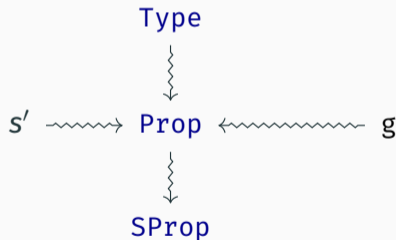
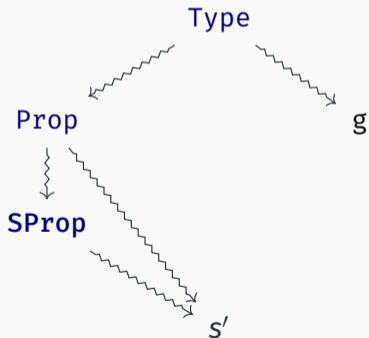


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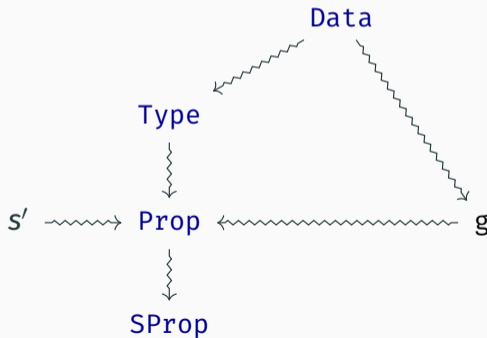
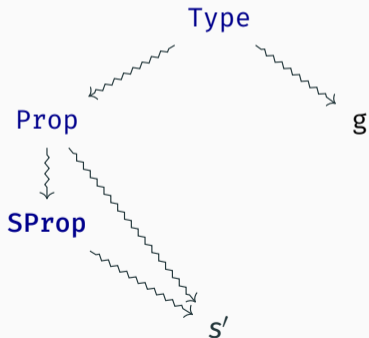


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What about strays?
have an initial sort **Data**



Let's End This Damn Proof

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For a closed $t : \perp^s$, instantiate away sort variables.

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If `SortPoly` is consistent, then there does not exist a well-typed closed term $t : \perp^s$ in $\text{SortPoly}^{\rightsquigarrow}$ for s a consistent sort.

For a closed $t : \perp^s$, instantiate away sort variables. But how?

- ▶ Ensure existence: all sort variables must be dominated.
- ▶ Take care of strays: initial sort.

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Under these conditions: instantiate by taking dominant ground sort (or initial sort if there are no dominants).

Implementation of elimination constraints in Rocq:

- ▶ ad-hoc checks for dominant sorts (amortized constant complexity),
- ▶ (current implementation restriction) manual prohibition of $SProp \rightsquigarrow s$,
- ▶ elaboration to get principal sort assignment.

Some performance regressions ($\approx 4\%$) in the monomorphic case:

- ▶ eliminability check through a graph,
- ▶ bigger structures at elaboration.



Check out the RFC!

This is Goodbye (For Now)

We have extended the type system of `SortPoly` so that our extension:

- ▶ has relative consistency w.r.t `SortPoly`,
- ▶ has the same logical power as `SortPoly`,
- ▶ has a principal sort assignment,
- ▶ has an elaboration procedure yielding the principal sort.

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Any question(s)?