Théorie des jeux pour la négociation entre la production d'énergie et les tâches informatique dans un datacenter à énergies renouvelables

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# Context

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- ⇒ IT consumes a huge amount of energy
  - sending an email with an attach file consumes as much as one low-power bulb of high power for one hour
- $\Rightarrow$  Data Centers in the US consumed 91 billions of kWh in 2013
- $\Rightarrow$  Data Centers in Europe consumed 56 billions of kWh in 2013

 increasing the energy efficiency of data-centers  supplying data-centers with only green energy

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 increasing the energy efficiency of data-centers  supplying data-centers with only green energy

## DATAZERO : an innovative data-center model



## DATAZERO : an innovative data-center model



Adapting the IT load to the available power & Adapting the power to the incoming IT load



while using a mix of only green energy sources (without grid power usage)



### **DATAZERO : the big picture**



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## Outline

- 1. Context
- 2. Negotiation between ITDM and PDM Context and overview of the problem
- 3. Pareto front
- 4. SAN and GAN : Turn based approaches
- 5. SCHEDULING BASED NEGOTIATION (SAN) Formulation Example
- 6. GAME BASED NEGOTIATION (GAN)
  - Model Negotiation Model Algorithm ITDM Formulation PDM Formulation Example
- 7. EXPERIMENT

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# **Negotiation between ITDM and PDM**

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## Context and overview of the problem

#### **Problem statement**



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- Ability to evaluate power plan impact
- Internal objective (utility)
- Black box functions  $\mathbb{R}^T \to \mathbb{R}$
- Computationally expensive



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- Each DM has one or more objectives to satisfy
- Objectives may differ between DM
  - QoS related for ITDM, environmental impact for PDM

#### Managing different objectives

3 options studied :

- ► Finding a set of good solutions (set of possible trade-offs) (Pareto-based approach)
- Maximizing the weighted sum of the utilities, under the constraint of a distance between the two resulting profiles (SAN approach)
- Playing a game between the PDM and the ITDM so that each one maximizes its profit (GAN approach)

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# **Pareto front**

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#### Multi-Objective Evolutionary Algorithms

- Well studied area, various approaches
- Focused on SPEA2 (genetic algorithm). Maximization of the hypervolume of solutions

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# SAN and GAN : Turn based approaches

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## **Overview of SAN and GAN approaches**

Main points

- Both algorithms are based on scheduling
  - DMs generate multiple scheduling solutions
  - Then we find negotiation solution from those scheduling solutions
- Both SAN and GAN negotiates in turn-based strategy
  - When ITDM runs scheduling (to follow PDM), PDM does not, and vice versa
  - We define 2 modes : "Follow PDM" mode (FLW\_PD) and "Follow ITDM" mode (FLW\_IT)
  - ► For both SAN and GAN (for the entire of the presentation), the whole system is executed under only 1 mode at a time



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# SCHEDULING BASED NEGOTIATION (SAN)

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Definitions

- ▶ The set of ITDM profiles is {*x*<sub>1</sub>, *x*<sub>2</sub>, ..., *x*<sub>m</sub>}
- The set of PDM profiles is  $\{y_1, y_2, ..., y_n\}$
- Depending on each specific context, a profile may also be named "hint" or "candidate"

2 stages

- Stage 1 : Checking for matched pair
  - Decision variable : the pair {PDM profile, ITDM profile} :

$$\{x \in \{x_1, x_2, ..., x_m\}, y \in \{y_1, y_2, ..., y_n\}\}$$

Objective : maximize sum of utility

$$\max_{\{x,y\}} (u(x) + u(y))$$
 (1)

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- Constraint :  $d(x, y) < \epsilon$ where d() is the distance between x and y
- If we can't find any matched pair, run Stage 2 : Negotiating.

Stage 2 : Negotiating :

- General mechanism
  - At a time, the whole system is executed under only 1 mode : follow ITDM (FLW\_IT) or follow PDM (FLW\_PD)
  - NM decides to switch between two modes using "verify quality of rescheduling"
  - Repeat until matched pair found
- Two modes :
  - FLW\_IT : Follow the ITDM
    - NM sends the ITDM hints to PDM
    - PDM uses an algorithm (e.g. greedy, linear program) to find multiple scheduling solutions as candidates
    - PDM evaluates quality of candidates by "weighted similarity" to hints
    - PDM selects candidates with high "weighted similarity" as its news hints and sends back to NM
  - FLW\_PD : Similar to FLW\_IT, following the PDM

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(\*) verifiy quality of rescheduling: compare "distance between the best ITDM hint and the best PDM hint" before and after rescheduling

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## Formulation

▶ Mean Square Error between profile  $x = \{x_1, ..., x_T\}$  and  $y = \{y_1, ..., y_T\}$ :

$$d(x,y) = \frac{1}{T} \sum_{i=1}^{T} (x_i - y_i)^2$$
(2)

Pearson correlation between them :

$$d(x,y) = \frac{\sqrt{\sum_{i=1}^{T} (x_i - \bar{x})^2} \sqrt{\sum_{i=1}^{T} (y_i - \bar{y})^2}}{\sum_{i=1}^{T} (x_i - \bar{x})(y_i - \bar{y})},$$
(3)

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$$w(x,Y) = \sum_{n=1}^{N} (u(x) + u(y^n)) \frac{1}{d(x,y^n)},$$
(4)

Or, if we want to adjust impact of utility and distance :

$$w(x, Y) = \sum_{n=1}^{N} \left( \alpha(u(x) + u(y^{n})) + (1 - \alpha) \frac{1}{d(x, y^{n})} \right),$$
 (5)

where  $Y = \{y^1, ..., y^n, ... y^N\}$  and  $y^n = \{y_1^n, ..., y_T^n\}$ , and the values are normalized to (0,1]

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Follow ITDM



Follow PDM



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# GAME BASED NEGOTIATION (GAN)

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# Model

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#### Model



#### Motivation

- The buying-selling nature of the system
  - ▶ Selling : PDM is selling power → controls the price
  - Buying : ITDM is buying power  $\rightarrow$  decide the order/purchase
- Advantages of pricing
  - Power source availability can be reflected in price
  - $\blacktriangleright$  Through price, pattern of order reflects pattern of PDM's desirable supply  $\rightarrow$  drive demand toward supply

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### Model

#### Preliminary

- Players are selfish
  - They try to maximize their utility
  - Each player negotiates just because he foresees some benefit
  - ► We introduce *incentive pricing mechanism* : each player tries to find offers that are attractive to the other player.
- An unexpected situation may occurred : all players can't foresee their benefit and stop negotiate without reaching any agreement.
  - From the view of the whole system, this situation is unacceptable, no transaction is done, the players obtain zero utility
  - ► If this situation occurred, we introduce *sacrifice mechanism*, in which the players gradually sacrifice their utility until they reach an agreement.

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## **Definition 1**

- ► T : Time window
- $\hat{x}, x^{IT}, x^{PD}$  are profiles

• 
$$\hat{x} = \{\hat{x}_1, \hat{x}_2, ..., \hat{x}_T\}, x^{IT} = \{x_1^{IT}, x_2^{IT}, ..., x_T^{IT}\} x^{PD} = \{x_1^{PD}, x_2^{PD}, ..., x_T^{PD}\}$$



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#### **Definition 2**

•  $\pi = \{\pi_1, \pi_2, ..., \pi_T\}, \pi^{IT} = \{\pi_1^{IT}, \pi_2^{IT}, ..., \pi_T^{IT}\}, \pi^{PD} = \{\pi_1^{PD}, \pi_2^{PD}, ..., \pi_T^{PD}\}$ 



pd sched()

pd\_est\_price() pd\_propose\_price()

## **Negotiation Model**

Turn-based play

- ► There are 3 variables :
  - ► ITDM local variable *it\_mod* = {*FLW\_IT*, *FLW\_PD*},
  - ▶ PDM local variable  $pd\_mod = \{FLW\_IT, FLW\_PD\},\$
  - global variable  $mod = \{FLW\_IT, FLW\_PD\}.$
- The mode of the system is only depended on mod. Two local variables only show the capability of the DMs.
- At a time, the system is executed under only one mode
- However, each player is selfish, he always wants the other player to follow himself, i.e., *it\_mod* = *FLW\_IT*, *pd\_mod* = *FLW\_PD*. In this situation, the negotiation can't be processed.
- Therefore
  - ▶ if ITDM is also capable of following PDM, we will set *it\_mod* = *FLW\_PD*
  - if PDM is also capable of following ITDM, we set  $pd\_mod = FLW\_l\overline{T}$

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Negotiation solution

- Stopping criteria :  $\hat{x}$  approximates both  $x^{T}$  and  $x^{PD}$
- Final solution is the last  $\hat{x}$

Incentive pricing mechanism :

ITDM follows PDM : when x<sup>PD</sup> and π<sup>PD</sup> are attractive \* : it\_cost(aspiration supply, PD incentive price) < it\_cost(order, price) :</p>

$$c(x^{PD}, \pi^{PD}) < c(\hat{x}, \pi)$$
(6)

PD follows ITDM : when ITDM's offers are attractive : pd\_revenue(aspiration order, IT incentive price) > pd\_revenue(order, price)

$$r(x^{T}, \pi^{T}) > r(\hat{x}, \pi)$$
 (7)

(\*) next page

(\*) How  $\pi^{PD}$  can be attractive to ITDM :

- ► Given :
  - Definition : x<sup>PD</sup> is the PDM's desirable supply
  - Then, the cost associated with this supply is lower than the cost associated with other supplies
- As a result
  - ► the PDM estimates the amount of cost it can reduce when it provides the ITDM with  $x^{PD}$ , instead of  $\hat{x}$ .
  - the PDM computes a  $\pi^{PD}$  such that its total utility increases

$$u(x^{PD}, \pi^{PD}) > u(\hat{x}, \pi) \tag{8}$$

How  $\pi^{T}$  can be attractive to PDM : similarly

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Sacrifice mechanism

- Unexpected situation : both ITDM and PDM are not capable of following each other, but an agreement is not reached
- Solution : ITDM gradually increases its *sacrifice variable*  $\alpha$  :

$$\alpha \leftarrow \alpha + \gamma \tag{9}$$

then the incentive pricing mechanism at ITDM becomes :

$$\boldsymbol{c}(\boldsymbol{x}^{PD}, \pi^{PD}) - \alpha < \boldsymbol{c}(\hat{\boldsymbol{x}}, \pi)$$
(10)

Similarly, incentive pricing mechanism at PDM becomes :

$$r(\boldsymbol{x}^{IT}, \pi^{IT}) + \alpha > r(\hat{\boldsymbol{x}}, \pi)$$
(11)

Note :

- At a time, the whole system is executed under only one mode : FLW\_IT or FLW\_PD
- DMs only exchange data that have been updated/modified, other data can be stored and reused



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Graphical interpretation of the algorithm



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## **ITDM Formulation**

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$$u(x,\pi) = r(x) - c(x,\pi) = \sum_{i=1}^{J} u_i(x) - \sum_{k=1}^{T} \pi_k x_k,$$
 (12)

#### where

- $r(\cdot)$  : revenue of ITDM
- $c(\cdot)$  : ITDM's payment to PDM
- ► J : the number of ITDM's jobs
- $u_i(\cdot)$ : the payment of the users' *i*-th job to ITDM

The payment from users is computed based on the Amazon EC2 pricing

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## **PDM Formulation**

$$u(x,\pi,S) = r(x,\pi) - c(x,S) = \sum_{i=1}^{T} \pi_i x_i - \sum_{j \in S} c_j^{OP}(x) c_j^{CAP}$$
(13)

where

- ►  $c_j^{OP}(\cdot)$  : operational rate of the j-th power source component
- $c_i^{CAP}(\cdot)$  : the capital cost
- S is the number of utilized power source components

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- it\_sched() : Generate  $x^{IT}$  from the scheduling solution, such that
  - Utility  $u(x^{IT}, \pi)$  is maximized
  - Revenue of x<sup>it</sup> must be larger than revenue of previous round's aspiration order x<sup>it</sup>
  - And  $x^{IT}$  has to be closer to  $x^{PD}$  than previous round's aspiration order  $\dot{x}^{IT}$

$$x^{IT} = \arg\max_{x} \ u(x,\pi) \tag{14}$$

$$s.t r(x) > r(\dot{x}^{T}) (15)$$

$$d(x, x^{PD}) < d(\dot{x}^{IT}, x^{PD})$$
(16)

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 it\_place\_order() : ITDM finds x̂ that maximizes the ITDM's utility function u(x, π)

$$\hat{x} = \arg\max_{x} u(x, \pi) \tag{17}$$

► it\_est\_price() : ITDM estimates new  $\pi^{IT}$  that is more attractive to PDM than previous round's IT incentive price  $\dot{\pi}^{IT}$ , while keeping the ITDM's total utility non-decreased :

$$\mathbf{p} = \pi^{IT} = \dot{\pi}^{IT} \tag{18}$$

while 
$$u(x^{lT}, \boldsymbol{\rho}) \ge u(\hat{x}, \pi)$$
 (19)

$$\pi^{\prime T} = \rho \tag{20}$$

$$p_i = p_i + p_i/N, \quad i = 1, ..., T$$
 (21)

where N is an integer, set through experiment parameters

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• pd\_propose\_price( $x^{PD}$ ) : the price  $\pi$  is generated such that

$$\pi_i = \frac{1}{X_i^{PD}}, \quad i = 1, ..., T$$
 (22)

where  $x_i^{PD}$  is normalized to (0,1]

pd\_est\_price() : Similar to it\_est\_price(), PDM estimates a new π<sup>PD</sup> that is more attractive to ITDM than previous round's PD incentive price π<sup>PD</sup>, while keeping PDM's utility non-decreased :

$$\rho = \pi^{PD} = \dot{\pi}^{PD} \tag{23}$$

while 
$$u(x^{PD}, p) \ge u(\hat{x}, \pi)$$
 (24)

$$\pi^{PD} = \rho \tag{25}$$

$$p_i = p_i - p_i/N, \quad i = 1, ..., T$$
 (26)

- pd\_sched() : Generate  $x^{PD}$  from the scheduling solution, such that
  - Utility  $u(x^{PD}, \pi, S)$  is maximized
  - Cost of  $x^{PD}$  must be smaller than cost of previous round's aspiration supply  $\dot{x}^{PD}$
  - New price  $\pi$  has to be closer to  $\pi^{IT}$  than the previous round's price  $\dot{\pi}$

$$x^{PD} = \arg\max_{x} \ u(x, \pi, S)$$
(27)

$$s.t \qquad c(x) < c(\dot{x}^{PD}) \qquad (28)$$

$$d(\pi, \pi^{IT}) < d(\dot{\pi}, \pi^{IT})$$
 (29)

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where  $\pi \leftarrow pd\_propose\_price(x)$ 

#### Simplified example



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# **EXPERIMENT**

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#### Real PDM & ITDM

- PDM weather information : 1 month
- Time window : 3 days or 72 hours
- Timestep : 1 hour or 3,600,000 ms
- ▶ PDM sizing : ≈1kW
- ► Run time : ≈10 minutes

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#### Distance

- Calculation : using Pearson correlation
- Distance is not always decreasing because the profiles are evaluated by both utility and distance
- Negotiation results depend a lot on the series of utilities from DMs



## Violation

- Calculation : sum of the amount that the ITDM profiles excesses PDM's profiles
- A significant reason for this result : DMs scheduling algorithms





Visit www.datazero.org for more information !!

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