

CRITICAL POINT THEORY FOR LAGRANGIAN SYSTEMS

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ERRATA CORRIGE

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- The last part of the proof of Lemma 2.1.2 (page 33) contains a silly mistake: the set $\mathbf{E}_{\mathcal{K}}^{\leq -c_P}$ is clearly not a direct sum of eigenspaces of \mathcal{K} , it is rather a cone. The paragraph

“Notice that $\mathbf{E}_{\mathcal{K}}^{\leq -c_P}$ is the direct sum [...] is finite dimensional.”

should be replaced with the following:

“Assume by contradiction that there exists a linearly independent infinite sequence $\{\mathbf{v}_n \mid n \in \mathbb{N}\}$ contained in $\mathbf{E}_{\mathcal{B}}^- \cap \mathbf{E}_{\mathcal{D}}^+$. Let \mathbf{E}_0 [resp. \mathbf{E}_1] be the direct sum of the eigenspaces of K corresponding to the eigenvalues less than or equal to $-c_P$ [resp. greater than $-c_P$], and let $\pi : \mathbf{E} \rightarrow \mathbf{E}_0$ be the orthogonal projection. Since K is compact, \mathbf{E}_0 is finite dimensional. Therefore, we can find $n_1, \dots, n_k \in \mathbb{N}$ and $\lambda_1, \dots, \lambda_k \in \mathbb{R}$ such that

$$\pi(\mathbf{v}_{n_k+1}) = \lambda_1 \pi(\mathbf{v}_{n_1}) + \dots + \lambda_k \pi(\mathbf{v}_{n_k}).$$

Notice that

$$\mathbf{v}_{n_k+1} \neq \lambda_1 \mathbf{v}_{n_1} + \dots + \lambda_k \mathbf{v}_{n_k},$$

since the sequence $\{\mathbf{v}_n \mid n \in \mathbb{N}\}$ is linearly independent. Thus, the vector

$$\mathbf{v} := \mathbf{v}_{n_k+1} - \lambda_1 \mathbf{v}_{n_1} - \dots - \lambda_k \mathbf{v}_{n_k}$$

is nonzero and contained in $\mathbf{E}_{\mathcal{B}}^- \cap \mathbf{E}_{\mathcal{D}}^+ \cap \mathbf{E}_1$. This is a contradiction, since $\mathbf{E}_{\mathcal{K}}^{\leq -c_P} \cap \mathbf{E}_1 = \{\mathbf{0}\}$.”

Date: May 25, 2012.

If you find further inaccuracies, please send me an e-mail to marco.mazzucchelli@ens-lyon.fr.