

Algorithmic design of DNA nanostructures with non-planar curved helices

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Abstract. Form and function are intimately linked—a guiding principle across both biology and engineering. While evolution and human ingenuity have shaped this landscape through function-driven form selection, AI-driven generative design expands it beyond natural and intuitive geometries, enabling the exploration of structure-driven functionalities that were previously inaccessible. At the nanoscale, however, realizing such non-intuitive architectures remains a key challenge, limiting the development of multifunctional nanostructures across biology, chemistry, and materials science. To address these constraints, we introduce an algorithmic design paradigm that enables DNA helices to follow non-planar 3D trajectories, thereby supporting the structural and functional outcomes required for advanced capabilities. We implemented this paradigm in ENSnano, a software platform that integrates mathematical models to automate structural design in 3D space without the need of human intervention. This framework allows us to rapidly generate DNA nanostructures with key functional features such as curvature, encapsulation, and hierarchical organization—reminiscent of naturally occurring biological architectures. As a key application, we demonstrate an automated pathway from biological to engineered structures by designing and experimentally assembling Vault-like cages directly derived from the emPDB model of the Vault protein, marking a step forward in biomimetic DNA nanostructure design.

One-sentence summary. Algorithms enable accurate design of DNA origami nanostructures with complex 3D curvature and torsion.

Introduction

The interplay between form and function is a unifying principle across natural and engineered systems. In engineered gears, specific geometries optimize force transmission, while in architectural arches, curvature and torsion enhance structural rigidity and stability^{1,2}. Many of engineered designs draw inspiration from biology, where evolution has refined structural forms to achieve specific functional outcomes³. Advances in artificial intelligence have further expanded the exploration of form–function relationships in biology. Landmark methods such as AlphaFold for highly accurate protein structure

prediction, together with recent generative protein design approaches including diffusion-based frameworks such as RFDiffusion, now enable the rational creation of biomolecules with tailored structures and functions^{4,5}.

Translating these functional forms to the nanoscale presents a significant challenge, requiring molecular-level precision to ensure function, an essential step toward the development of smart materials, synthetic biological systems, and precision therapeutic devices. Structural DNA nanotechnology addresses this challenge by redefining nucleic acids as programmable building blocks for encoding functional shapes at the nanoscale¹.

Among self-assembly strategies, DNA origami⁶ has become the benchmark for constructing accurate nanoscale architectures. It enables precise control over geometry, site-specific chemical functionalization, and dynamic mechanical properties^{7,8,9,10}, while producing billions of copies in a single-pot reaction. In this approach, a long single-stranded DNA scaffold is folded into a target shape by hundreds of short oligonucleotides through sequence-specific base pairing. This programmable assembly method has facilitated the creation of diverse nanostructures, advancing both biological research and materials science by encoding functional form at the molecular scale^{11,12,13}.

However, current design strategies remain largely restricted to geometries composed of straight segments^{14,15,16,17} and planar arcs^{18,19}. This constraint arises from the conventional DNA origami approach, which models helices as near-rigid cylinders connected by crossovers at fixed spacing. The reliance on fixed crossover spacing cannot accommodate the non-integer helical twist of DNA^{20,21}, which is approximately 10.44 base pairs per turn^{22,23,24}. Furthermore, classical geometric approaches²⁵ often introduce unintended helical twist when mapping DNA onto non-planar curves. As a result, current frameworks support only planar arrangements of helices and break down when non-planar trajectories involving both curvature and twist are required. Yet such trajectories are essential for expanding the accessible design space, as many functional structures in biology and materials science exhibit non-planar three-dimensional curves and twisted geometries^{26,2}.

Here, we introduce an algorithm-driven design framework that enables the construction of DNA origami structures with helices arranged along non-planar trajectories in three-dimensional space. This approach allows precise crossover placement and promotes uniform strain distribution across helices while minimizing torsional stress. Our approach integrates three core elements (Fig. 1): a nucleotide positioning algorithm for non-planar 3D curves, automated computation of helix trajectories to cover target shapes, and structural optimization routines to relieve strain in the design. This algorithmic workflow—automating the most time-consuming aspects of curved DNA nanostructure design¹⁹—is fully integrated into our open-source software, ENSnano^{27,28}. Using this framework, we designed and assembled previously inaccessible nanostructures, including curved helical bundles in three-dimensional space, twist-rich hollow architectures, and nested spherical shells connected by

narrow tunnels. These structures demonstrate key functional attributes—such as mechanical robustness, molecular encapsulation, compartmentalized reactivity, and channel-like features that regulate inter-compartmental transport and flow—commonly observed in biological systems. Unlike wireframe DNA origami^{16,17}, which inherently limits addressability to the edges of the mesh, our framework generates fully covered surfaces with complete surface addressability, enabling dense and programmable functionalization across the entire nanostructure.

As a proof of concept, we designed an artificial nanostructure that reproduces the geometry and dimerization behavior of the Vault protein by generating a DNA origami nanocage whose shape is directly derived from the protein’s atomic structure deposited in the Protein Data Bank (PDB), rather than adapted to the constraints of DNA origami design. This biomimetic construct demonstrates that our framework can faithfully reproduce naturally occurring three-dimensional geometries. More broadly, it enables the rational design of bioinspired architectures that transcend the geometric constraints of conventional DNA origami.

Results

Algorithmic nucleotide positioning along arbitrary 3D curves. Mapping a DNA helix onto a non-planar 3D curve requires defining a moving frame along the curve. The classical Frenet frame approach²⁵ fails in this context, as it rotates erratically under the influence of torsion in non-planar curves, introducing unwanted twist into the mapped helix. To address this, we developed a custom algorithm that computes a lazily rotating moving frame along the curve (algorithm SA1). We then use the computed frame to map the DNA helix onto the curve using the best-known structural parameters for DNA²³ (table ST1 and fig. S1). Figure S2 illustrates the algorithm in action, while Figure S3 compares the classical Frenet frame to our approach. The comparison demonstrates that our algorithm avoids unnecessary frame rotation, producing a minimally twisted DNA helix with a more regular twist, closer to its canonical value in the straight conformation.

We validated our DNA model by simulating a nucleosome, a key example of DNA curvature in biology. In the nucleosome, the DNA helix undergoes significant bending, wrapping approximately 1.65 turns around the histone octamer to form a left-handed superhelix²⁹. Figure S4 compares crystallographic data (2CV5.PDB) with the output of our algorithm for a DNA helix wound

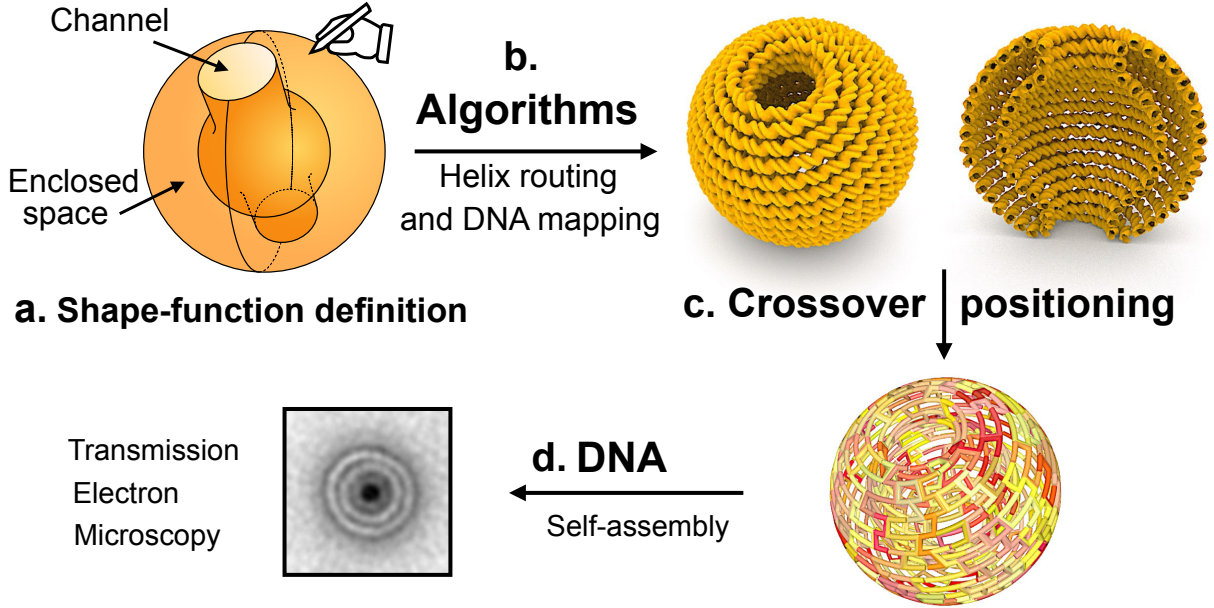


Figure 1: Algorithm-driven conceptual framework for DNA nanostructure design. (a) The target shape is defined using Bézier curves and geometric descriptors, such as the revolution surface tool. (b) The algorithm automatically computes helix trajectories that cover the target shape at an appropriate scale for the chosen scaffold strand, positioning nucleotides along their (possibly non-planar) 3D paths. A series of automated optimizations is applied to relieve structural strain. (c) The designer places scaffold and staple strand crossovers between helices. (d) Staple strand sequences are exported for assembly and imaging. Shown here is a negative-stain 2D TEM class average of the resulting self-assembled DNA nanostructure, box size is 80×80 nm.

around a nucleosome. Our model accurately reproduces nucleotide positions with an RMSD of 0.54 ± 0.23 nm, and phosphate with an RMSD of 0.44 ± 0.22 nm (figs. S5 and S6).

DNA helix bundle non-planar curvature programming. DNA helix bundles are a fundamental component of the DNA origami design toolbox. Early design strategies^{14,19} laid the groundwork for a wide range of applications, including nuclear pore complex mimics³⁰, liposome templating³¹, membrane shaping¹¹, spring-loaded nanodevices³², and targeted drug delivery systems¹³. Here we present an algorithm that enables the design of curved helix bundles in full 3D space, with continuously varying radii of curvature.

In our approach, a DNA helix bundle is defined by attaching a grid (square or honeycomb) to a Bézier curve $t \mapsto M(t)$. Each helix, located at coordinates (i, j) , follows the path $t \mapsto P_{ij}(t)$ of the grid point at coordinates (i, j) in the moving frame $F(t)$ centered on $M(t)$ (fig. S7). This construction ensures that the trajectories of the helices remain uniformly spaced along the entire length of the bundle. DNA helices are then mapped in real time onto their respective paths $P_{ij}(t)$ using the previously described DNA model. A core feature is that, since all helices in the bun-

dle evolve along the common parameter t , we introduced an adaptive 2D view of the structure in ENSnano software. In this 2D representation, the width of each nucleotide's cell is automatically adjusted based on t , ensuring that all nucleotides at the same cross-section appear vertically aligned (fig. S9). As a result, nucleotides eligible for crossovers are naturally aligned in the 2D view, eliminating the need for manual insertions or deletions. For closed curves, the rise and helicity of each DNA helix are automatically adjusted to ensure an integer number of helical turns. In practice, these adjustments are minimal (only a few %) and remain well within established precision limits. This optimization helps to evenly distribute mechanical strain along each DNA helix (figs. S10 to S13). All calculations are performed in real time, enabling the designer to interactively fine-tune the curve, either to precisely position functional groups or to ensure an exact match with the scaffold length.

Then, we proceed to position the crossovers by first placing a single crossover between adjacent helices. Next, we apply our *auto-roll* algorithm, which rotates neighboring helices to minimize crossover lengths. Once the helices are rotationally aligned, a standard scaffold and staple pattern is applied, with crossover positions visually adjusted in both 2D and 3D views of the design to optimize their length and orientation.

To explore the effectiveness of our method we designed a four-loop DNA origami structure, referred as ⌘-origami. The ⌘-origami consists of a 6-helix bundle programmed with four precise 270-degree looped bends (figs. S14 to S23). The crossover patterns were selected to minimize structural strain by 1) spacing the scaffold crossovers approximately every 100 base pairs, and 2) reducing the occurrence of double crossovers for the staples. The scaffold layout follows a “leaf” pattern (fig. S24), where each domain or “leaf” averages around 86 base pairs in length. Staples follow the classic C-shape (fig. S25), with domains typically ranging from 15 to 20 base pairs in straight regions. To accommodate curvature, staple domains on the inner side of the curve may be shortened by a full turn while those on the outer side may be extended by a full turn – adjusting lengths by approximately 8 to 12 bps depending on curvature. These modifications are guided by inspection of the 3D nucleotide mapping in the interactive 3D view. In our design, staple domains range from 7 to 30 base pairs, with staple strand lengths between 19 and 60 base pairs. Crossover lengths range from 0.65 nm and 1.7 nm according to our model. After optimizing folding conditions via agarose gel electrophoresis and negative-stain TEM (ns-TEM) particle analysis, optimal folding was achieved by mixing the scaffold with staple oligonucleotides at a 10-fold molar excess, in the presence of 20 mM MgCl₂, and following a 42-hour temperature annealing protocol (Fig. 2 and figs. S26 to S28). ns-TEM particle analysis yielded 2D class averages that closely match the intended four looped bends, each forming a precise 270-degree angle, confirming successful folding of the structure. To further assess the fidelity of curvature programming conferred by the global crossover pattern, we introduced several structural variants: (1) opening a section of the 6-helix bundle by splitting the staple strands joining the scaffold at its termini (fig. S29), and (2) splitting the vertical staples linking the top and bottom scaffold domains at the four crossover points—designated NW, SW, SE, and NE—to decouple the vertical connection (fig. S30). Each variant yielded folded structures consistent with the degrees of freedom introduced by the respective modifications, with shape outcomes analogous to those achievable by a flexible plumbing pipe making four 270° turns (see section S2.8 and figs. S31 to S41).

Optimization of helix torsion and trajectories in hollow shapes. Designing DNA origami in capsule-like shapes is crucial for advancing nanotechnology, offering a protective barrier be-

tween the internal volume and the external environment. These 3D DNA nanostructures are finding applications in areas such as mimicking natural capsids for antigen presentation, virus trapping, low-volume reactors, templated assembly, molecular transport, and drug delivery^{33,13}. Optimal functionality in these applications often depends on the creation of curved 3D hollow shapes. Previous methods for designing such structures typically involved slicing them into a stack of parallel concentric circles^{19,18}. However, this approach has two main drawbacks¹⁹: First, the angles between adjacent layers are limited to the multiples of $\sim 34^\circ$, corresponding to the angle between two consecutive nucleotides. Second, the perimeter of each DNA ring must correspond to an integer number of full DNA helix turns. Moreover, this technique is only applicable to simple revolution surfaces¹⁸.

One of the most challenging steps in hollow DNA origami design is determining the trajectories of the DNA helices. A small miscalculation in helix placement or torsion can lead to significant deviations in the structure, affecting both its stability and functionality. This task involves solving a multicriteria optimization problem that determines the appropriate number of helices and the scale of the shape, ensuring that the helices are uniformly spaced (with an average interdistance of 2.65 nm^{6,34}), minimally curved or twisted, and that their total length matches the target size of the scaffold. This step was highlighted as the most time-consuming in previous approaches¹⁹. To address this, we introduce a *spiral-based* algorithm for slicing a revolution surface (possibly twisted) into curved, equally wide stripes. This method overcomes both of the aforementioned limitations of using concentric circles in two key ways, as detailed in the supplementary text (section S3). By allowing the curvature radius to vary continuously along the trajectories, our method enables a continuous range of crossover angles between adjacent helices. Moreover, since only a few long spirals (only 2 in our designs) are needed to assemble the shape, adjusting the helix parameters by a few negligible ‰ allows for continuous rescaling (figs. S42 to S44). This results in an automatic computation of the ideal scale for the target shape, optimizing the use of every single nucleotide in the scaffold. Finally, the use of spirals allows for seamless design of tubular portions with inner radii as small as 4.3 nm within a larger shape.

Our method is integrated in ENSnano software as an automatic pipeline. We proceed by specifying the surface and spirality parameters. The surface is given by its section curve, the number of twists, and its revolution radius. The spi-

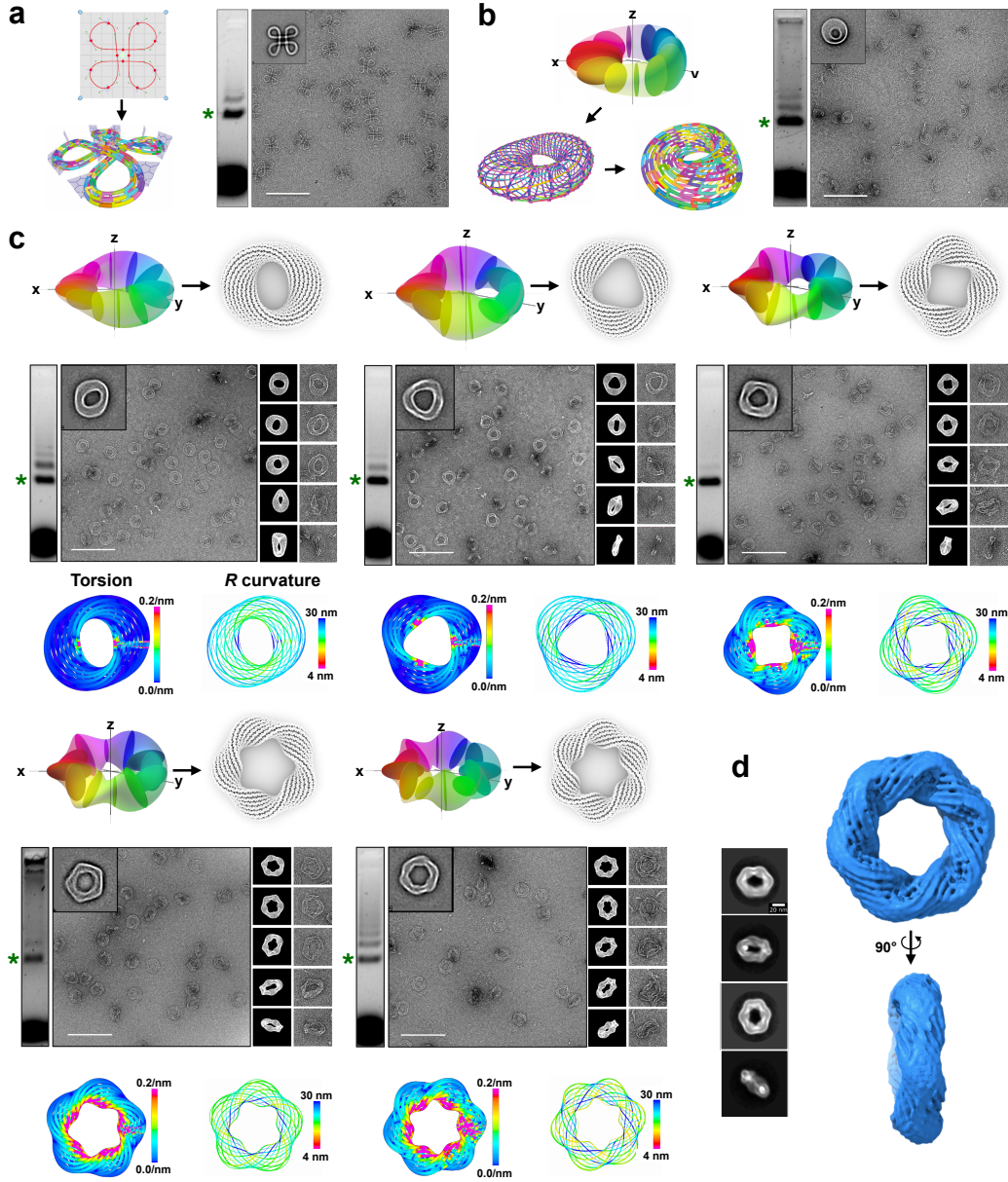


Figure 2: Spiral design algorithm for intricate hollow shapes. (a) Design workflow for a curved DNA origami composed of a 6-helix bundle with four programmed loops. In ENSnano, the bundle's Bézier path is first drawn and adjusted by the user, followed by algorithmic nucleotide mapping and crossover placement to produce the final assembly. (b) Design workflow for a half-twisted torus, defined in ENSnano as the surface generated by rotating a 2×1 ellipse by half a turn around the revolution axis. A spring-based system then optimizes helix trajectories and iteratively scales the surface until the total length matches the target scaffold length (here, 7560 bases), enabling automated nucleotide mapping and crossover placement. (c) Progressive increase in overall twisting complexity from T2 to T6, with schematic representations followed by algorithmic DNA helix routing, nucleotide mapping, and crossover placement. Below each TEM micrograph: Left: local torsion; Right: curvature radius along helices (color scales: 0 nm^{-1} [pink] to 0.2 nm^{-1} [dark blue] for torsion; and 4 nm [pink] to 30 nm [dark blue] for curvature). (d) Class averages from single particles observed by cryo-TEM and 3D reconstruction of T6 derived from 72,684 particles, with an estimated resolution of $13 \text{ \AA}$. For each structure, a 1% agarose gel (post-folding) and TEM micrographs are shown, alongside reference-free class averages from single particles (particle sets available in figs. S96, S100 to S102 and S106). White bars represent 200 nm ; box sizes for projections and class averages are $112 \times 112 \text{ nm}$ for the four-loop DNA origami and $99 \times 99 \text{ nm}$ for the Tori.

ral parameters include the number of spirals covering the surface, the *winding* parameter which dictates the rate at which the spirals coil around the surface and controls their inclination and tor-

sion (figs. S45 to S48), and the target scaffold strand length. Our algorithm calculates the spiral trajectories for the helices using a dedicated spring system which keeps them as straight and

evenly spaced as possible, minimizing their torsion along the way, as demonstrated in fig. S49. The algorithm scales the shape (section and revolution radius) until the distance between adjacent helices and the total helix length match the desired crossover distance and target scaffold length. The entire process is completed in a few seconds.

Inspired by the prevalence of twisted features in nature³⁵, we investigated the robustness of our spiral routing algorithm by designing a series of six toroidal structures referred as T1, ..., T6 with progressively increasing torsion. The surface of T k is obtained by rotating a 2-by-1 ellipse around a revolution axis while applying k half-turn twists to the section, as depicted in Fig. 2. Our algorithm generated, for each of them, a pair of spiraling helices that are evenly distributed across the surface, and whose total length precisely matches the target scaffold size (7560 nucleotides). By selecting appropriate winding parameters, we minimized the torsion of the resulting helices, yielding smooth and uniform trajectories throughout the structures (figs. S49 and S50). The resulting helices complete 7 (T5 and T6), 8 (T3 and T4), 9 (T2), and 10 coils (T1), while maintaining an interaxis spacing of $2.65\text{ nm} \pm 10\%$ relative to their counterparts.

As for the $\mathfrak{H}$ -origami, we optimized the staple and scaffold crossover placements using the 3D and 2D live-editable views provided by our algorithms (figs. S51 to S92).

We studied the assembly of T1 by combining 20 nM scaffold with a 10-fold excess of staple oligonucleotides, varying magnesium concentrations (2–30 mM) over a 42-hour folding ramp. Agarose gel electrophoresis (fig. S93) identified 12 mM as the optimal magnesium concentration. ns-TEM particle analysis yielded 2D classifications in close agreement with the T1 structure model (Fig. 2). We optimized the self-assembly protocol for each structure T2 through T6, as detailed in the supplementary text. Agarose gel electrophoresis, ns-TEM particle analysis, and 2D class averaging revealed uniform particle distribution and orientation, consistent with simulated 2D projections, and demonstrating proper folding relative to the predicted shapes (Fig. 2 and figs. S94 to S106). We further validated the T6 design using cryo-TEM imaging, generating a 3D electron density map through single-particle cryo-TEM analysis (Fig. 2 and figs. S98 and S99). The map revealed the characteristic six twists per ring, confirming the structural integrity of the design.

Algorithmic surface design with curvature inversion and tunnels. We further tested the robustness of our algorithms by designing an additional structure, double sphere DS, which explores novel architectural possibilities. This design features two nested spheres in a convex-concave configuration, interconnected by narrow channels. The resulting structure includes a hermetic compartment between the inner and outer spheres, as well as an internal open compartment regulated by tunnel diameters.

Our algorithms computed evenly spaced, spiraling helices that span this structure, which were defined as the revolution surfaces generated by rotating a $\mathbb{C}$ -shaped section around an axis. DS consists of two twisted DNA helices forming an outer sphere (41 nm diameter) connected by two 10 nm-wide channels to an inner sphere (29 nm diameter). The design was automatically adjusted to match the scaffold length (8,064 nucleotides) (Fig. 3 and figs. S107 to S113). The helices form 17 coils each. After optimizing folding conditions (see supplementary text and fig. S114), optimal assembly was achieved with 30 mM MgCl₂ over 42 hours, confirmed by agarose gel electrophoresis and ns-TEM analysis. 2D classifications revealed a homogeneous particle distribution, distinct contrast between spheres, and clear channel structures (Fig. 3 and fig. S115).

Biomimetic DNA origami design. We explored the bio-inspired applications of our algorithms, by designing a DNA origami that mimicks the shape of the vault protein, a barrel-shaped ribonucleoprotein complex found in the cytoplasm of eukaryotic cells. The vault protein can dimerize to form a closed cage^{36,37,38}. Its unique architecture and potential applications in targeted drug delivery and nanomaterial scaffolding have attracted considerable interest in nanotechnology³⁹.

To create the design, we began by modelling the cross-sectional curve of the vault protein PDB model 4V60 as a Bézier curve and applied our spiraling algorithm to generate the corresponding revolution surface. The shape was scaled automatically by a factor of 1.4 horizontally and 1.3 vertically, to match the target scaffold size of 8064 nucleotides, resulting in a structure 53 nm in width and 42 nm in height. Two inner hems were included at the top and the bottom of the structure to conceal the blunt ends of the helices and stabilize the 8.6 nm-wide tight hole at the top. The resulting two helices make 13 coils each. Additionally, the bottom of the design was equipped with six equally spaced 18-nucleotide anchor strands to facilitate homodimerization.

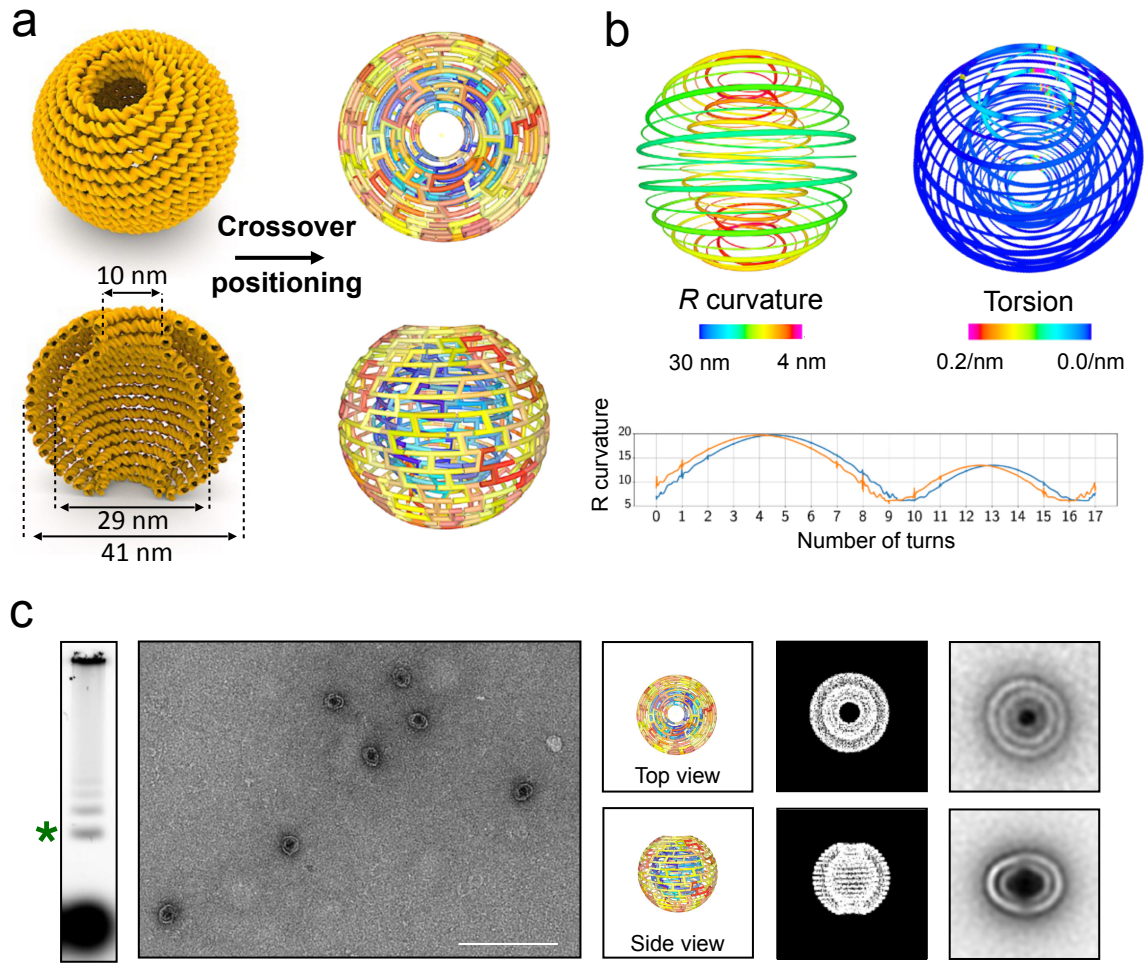


Figure 3: Spiral-based design for spherical surfaces. (a) Schematic illustration and staple design of DS. (b) Left: curvature radius along the two twisted DNA helices in DS. Right: local torsion. Color scales: 4 nm [pink] to 30 nm [dark blue] for curvature and 0 nm⁻¹ [pink] to 0.2 nm⁻¹ [dark blue] for torsion. Graphs show the evolution of curvature radius (in nm) as a function of the number of turns along each helix. (c) 1% agarose gel after folding and TEM micrographs of the purified band (green star), with representative projections from 3D PDB model and reference-free class averages from single particles (particle sets available in fig. S115). Scale bar represents 200 nm.

The resulting design, referred as vault origami (figs. S116 to S123), was then validated through direct comparison with the Vault protein model, imported in our software as an STL file generated by Chimera from the PDB file (Fig. 4).

We optimized folding of the vault monomer using agarose gel electrophoresis and ns-TEM, identifying 20 mM MgCl₂ as optimal (fig. S124). As detailed in the supplementary text and figs. S125 to S129, optimal dimerization was achieved by incubating gel-purified monomers at 37°C for 15 hours, yielding dimer structures consistent with the design, as confirmed by ns-TEM and 2D class averaging (Fig. 4 and fig. S129).

Yields. Table T1 summarizes the yields of the nanostructures presented in this work (figs. S130 and S131). The measured yields

range from 56.8% for the four-loop bundle $\mathbb{X}$ to 10.4% for the double-sphere DS. For the series of twisted tori, yields range from 53.9% to 18.6% (29.6% for the most twisted T6).

Discussion

Detailed analysis of our designs reveals that crossover spacing does not correlate with either local curvature radius or helix torsion, as shown in figs. S132 to S146 and further detailed in Supplementary Section S8. This observation highlights a critical limitation of classical rule-based design strategies^{20,19}, which rely on fixed patterning that cannot accommodate the geometric complexity of non-planar curved structures.

As DNA nanostructures evolve to encode increasingly sophisticated forms and functions, existing design constraints call for more ad-

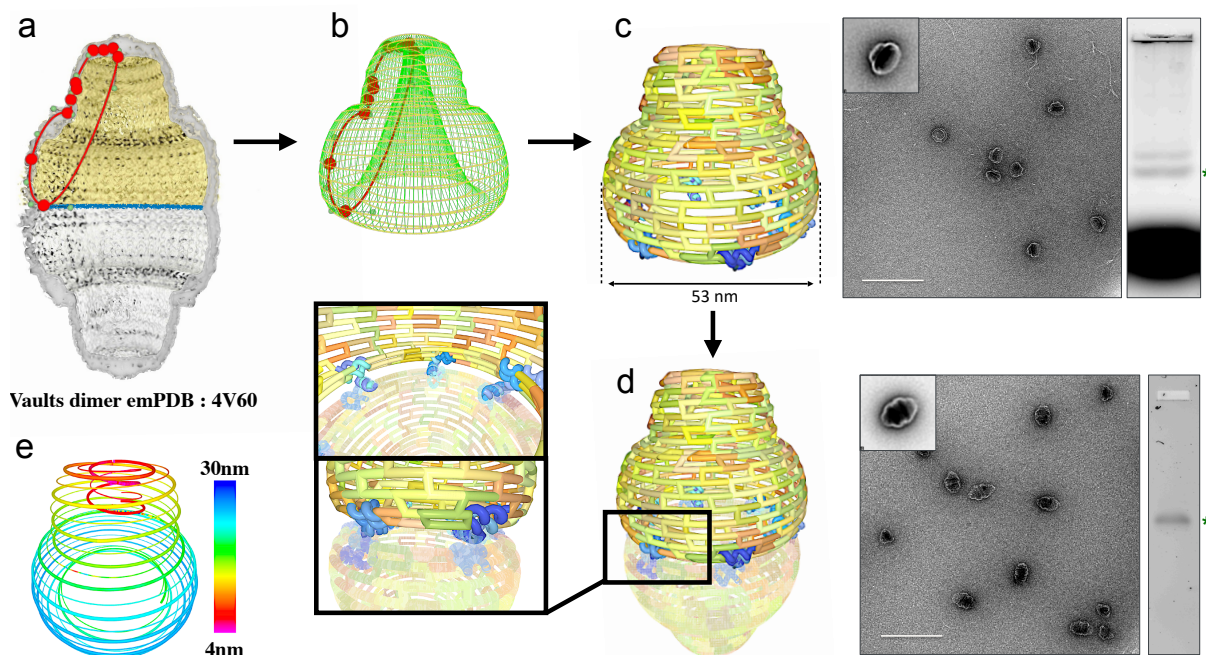


Figure 4: Bio-inspired vault protein-like design. (A) Bézier curve aligned to the cross-sectional profile of the vault protein, PDB model 4V60. (B) Spiral-based method applied to the revolution surface of the vault monomer. (C) Staple design, 1% agarose gel after folding, and TEM micrographs with reference-free class averages from single particles (particle sets available in fig. S126). (D) Schematic illustration of the dimer assembly strategy, 1% agarose gel after dimerization, and TEM micrographs with reference-free class averages from single particles (particle sets available in fig. S129). (E) Curvature radius along helices. Color scale from pink (4 nm) to dark blue (30 nm). White bars represent 200 nm.

Structure	T1	T2	T3	T4	T5	T6	DS	Vault	⌘
Yield	29.8%	39.7%	51.3%	53.9%	18.6%	29.6%	10.4%	15.6%	56.8%

Table T1: Assembly yields of all DNA origami structures.

vanced algorithmic strategies. Our algorithm-driven paradigm addresses this challenge by enabling non-planar curvature within DNA helix bundles and fully addressable single-layer architectures, without requiring human intervention, thereby supporting greater functional intricacy and the precise three-dimensional placement of functional groups. It also enhances planar designs by reducing reliance on iterative post-experimental adjustments²¹, and paves the way for the scalable assembly of larger functional structures with fewer components than multi-layered composites¹². This design framework is available through our open-source software, ENSnano⁴⁰, which integrates algorithmic control of helix geometry with intuitive 2D and 3D visualization, real-time editing, and a user-friendly interface. ENSnano is designed for continuous development, with planned extensions to support hybrid architectures—including DNA/RNA and DNA/protein systems—further bridging natural and engineered nanoscale assemblies. While the present strain-relief helix-routing algorithm

relies solely on geometric optimization, future developments could incorporate thermodynamic criteria to further improve structural stability. To facilitate such analyses, ENSnano already supports export to oxDNA, enabling molecular dynamics simulations to evaluate and refine the stability of the designed nanostructures. Finally, just as the design of a rectangle²² in caDNano allowed refine the pitch of straight helical DNA from 10–11 bp/turn to the now-standard 10.44 bp/turn, our framework provides a design environment for investigating the physical principles, structural properties, and functional behavior of curved and twisted DNA helices—both as they occur in biological systems, with implications for genome organization, gene regulation, and the structural physics of nucleic acids in health and disease, and as components of engineered nanodevices.

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Materials and Methods

Origami design The origami structures were designed using ENSnano v0.7.3 or later. ENSnano computed the DNA-helix trajectories and the corresponding three-dimensional nucleotide positions using the algorithmic design framework described in sections S1 to S3. This geometric embedding was subsequently used to place crossovers while maintaining regular staple architectures, yielding staples composed of two or three binding domains with lengths ranging from 6 to 29 nucleotides. A quick-start guide is available on the ENSnano website²⁷, and the complete design workflow for each class of origami is described step by step in sections S2.1, S3.4 and S6.1. The corresponding design parameters are summarized in section S7.

DNA strands Desalted staple strands were purchased from Integrated DNA Technologies (IDT) in water in 96-well plates at a concentration of 100 μ M each. The staple strands were pooled and diluted with water to a working concentration of 400 nM each. The different scaffolds used (M13 8064, M13 7560, M13 7249) were purchased from Tilibit Nanosystems. The scaffold (5 nM to 20 nM) and staples ten times in excess were combined in a one-pot reaction with a buffer of 5 mM Tris-HCl, pH=8.0, 1mM EDTA, different concentrations of MgCl₂ depending on the origami (12 mM to 20 mM). The thermal annealing ramp was spanned over a time-period from 3.5 hours to 63 hours. The scaffold, concentrations of the components and thermal annealing ramps used for each origami (if not otherwise noted) are described in table T2.

Agarose gel electrophoresis DNA nanostructures visualized by Electron Microscopy were purified from 1% agarose gels (0.5X TBE, 45mM Tris-borate, 1mM EDTA, pH 8.3) supplemented with 11mM MgCl₂ and 0.5mg · ml⁻¹ Sybr SAFE. Samples were migrated on the gel for 3h with a running buffer of 0.5X TBE, 11mM MgCl₂ 2.85V · cm⁻¹ at room temperature. Bands corresponding to properly folded DNA origami were excised and transferred to a DNA gel extraction spin column (Merck, France) centrifuged at 5,000 g for 5 min at 4°C.

Transmission Electron Microscopy - Negative staining Purified origami were visualized by adsorption onto glow-discharged carbon-coated grid (Quantifoil Micro tools GmbH, Germany), stained for 60 s with a 2% (w/vol) aqueous uranyl acetate (Merck, France) solution,

and then dried with ashless filter paper (VWR, France). Observations of EM grids were carried out on a JEM-1400Flash Tungsten microscope working at 120kV, equipped with a GATAN One View camera. Two-dimensional class averages were computed using EMAN2.

Cryo-EM sample preparation The purified and concentrated T6 samples were incubated 5 minutes twice to glow-discharged grids with an ultrathin carbon film supported by a 2/2 carbon film on a 200-mesh copper grid (Quantifoil Micro tools GmbH, Germany). Plunge freezing in liquid ethane was performed with a ThermoFisher Mk-IV Vitrobot with a blot time of 3 s, a blot force of 0 at 15°C and 100% humidity.

Cryo-EM image acquisition Selected grid of T6 was transferred under cryogenic conditions into the TFS Titan Krios TEM with acceleration voltage of 300 kV. Micrographs were acquired in two sessions on the Falcon4i camera under low-dose condition with a total flux of 40 e-/Å². Data were collected with underfocus values ranging from -0.7 μ m to -4.1 μ m in nominal resolution of 1.2 Å/px. Automated data acquisition was recorded into 40 individual frames. The forty-frame movies were then globally and locally (5x5 patches, 20% patch overlap) aligned to compensate for drift and beam-induced motion using program motioncor2⁴³. The resulting dose-weighted sum of aligned frames was used for subsequent image processing steps, except for estimating the contrast transfer function (CTF) parameters, which were estimated from aligned, non-dose weighted micrographs using the program ctffind4^{44,45,46}.

Cryo-EM image processing Data processing was done using SCIPION 3.0.9 package⁴⁷. 15,127 dose-weighted micrographs of T6 were used for the processing. The SPHIRE-crYOLO⁴⁸ protocol was used for particle picking from a set of 3x binned micrographs. The particles were subjected to three rounds of RELION 2D classification^{49,50,51,52} to remove falsely picked grid contaminations and damaged particles, high-quality 2D class averages were selected and duplicated particles with Xmipp3-remove duplicates^{53,54} with 80px radius, leaving a set of 142,198 particles. Relion initial model^{49,50,51,52} was used for generating the initial 3D volume. First, a 3D refinement without any symmetry (and with the initial model filtered down to 120Å) was applied, producing a 3D map at 26Å and confirming the presence of the expected D6 symmetry. Following this initial refinement, a se-

Object	Denaturation phase (15 min) (°C)	Temperature ramp	Hold temperature (°C)	Folding ramp time period (h)	Magnesium chloride concentration (mM)	Scaffold	Scaffold concentration (nM)	Staples concentration (nM)
⌘	65	60°C to 40°C: -1°C/2h	10	42	20	M13 7249	20	200
T1	65	60°C to 40°C: -1°C/2h	10	42	12	M13 7560	20	200
T2	65	1) 60°C to 55°C: -1°C/10min 2) 55°C to 25°C: -1°C/1h	25	33	18	M13 7560	20	200
T3	65	1) 60°C to 55°C: -1°C/10min 2) 55°C to 25°C: -1°C/1h	25	33	18	M13 7560	20	200
T4	65	1) 60°C to 55°C: -1°C/10min 2) 55°C to 25°C: -1°C/1h	25	33	18	M13 7560	20	200
T5	65	60°C to 40°C: -1°C/10min	10	3.5	18	M13 7560	5	50
T6	65	1) 60°C to 55°C: -1°C/10min 2) 55°C to 25°C: -1°C/1h	25	33	18	M13 7560	20	200
DS	65	60°C to 40°C: -1°C/2h	10	42	30	M13 8064	20	200
Vault	65	60°C to 40°C: -1°C/3h	10	63	20	M13 8064	20	200

Table T2: Final folding conditions for each origami.

ries of 3D refinements with progressively tightening masks and 3D classifications^{49,50,51,52} were applied to get a final set of 72,684 particles, subjected to a final 3D refinement^{49,50,51,52} with D6 symmetry, effectively reaching 13Å with a global mask.

Yield evaluation The yields of the structures were quantified by gel-band intensity analysis using ImageJ⁵⁵. Gel images were contrast-inverted, and the intensities of the DNA band corresponding to the well-folded structure, the entire gel lane, and the local background were measured. Yields were then calculated using an approach similar to those previously reported for DNA origami structures^{56,57}.

Dimerization of the Vault-like origami Each Vault-like monomer was designed to display six anchor staples at its bottom to enable dimerization. Two different versions of the 6 anchor staples A and B were designed with 18-base parts complementary to each other. The sequences of these staples are described in tables T3 and T4. The sequences annealing inside the monomers are in black, the sequences designed to be out of the monomers are in red (two T and the sequence to enable the annealing of staples A with staples B, leading to the dimerization of the vault-like origami).

The monomers of the Vault-like origami with staples A and staples B were folded according to the conditions detailed in Table T2. Then, they were purified by agarose gel electrophoresis. Finally, they were assembled in equal concentration for 15 hours at 37°C with 100 mM MgCl₂.

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- Staple no. 1: 5' TTGTTTAAACGTCACATT CATTACAAAATGAAAA TT AGTATATAGATAATTAAA 3'
- Staple no. 2: 5' TAACGAGCGTCGATTGCC TT AGTATATAGATAATTAAA 3'
- Staple no. 3: 5' CGACATTCAACCGATCACCCTCAC TT AGTATATAGATAATTAAA 3'
- Staple no. 4: 5' CGGGAACGGATAACCTCCAGTCACGACGTTGT GCCATTG TT AGTATATAGATAATTAAA 3'
- Staple no. 5: 5' CTGGTAATGGGTAAAGGTTTCTTTTTCGCA TT AGTATATAGATAATTAAA 3'
- Staple no. 6: 5' ATGCCAACGGGAAAGGCTGGCCAGCACCGTCG TT AGTATATAGATAATTAAA 3'

Table T3: Version A of the six staples enabling the dimerization.

- Staple no. 1: 5' TTTAATTATCTATATACT TT TAGCAGCAACTGAACACCCTGA 3'
- Staple no. 2: 5' TTTAATTATCTATATACT TT GTGGTGCGTTACCTGCA 3'
- Staple no. 3: 5' TTTAATTATCTATATACT TT AGGCTGCACTCCAGCCAGCTTTCGGAACCCGTCGGATTCT 3'
- Staple no. 4: 5' TTTAATTATCTATATACT TT GTTCCGGCAAACGCGGTGTGTACATCGACATAA 3'
- Staple no. 5: 5' TTTAATTATCTATATACT TT CGACTTGACCGTAATCAGTAGCGACAGAATCA 3'
- Staple no. 6: 5' TTTAATTATCTATATACT TT CTCATCCGCCG GAGCACATCCTCATAACAGCGGATCA 3'

Table T4: Version B of the staples enabling the dimerization.

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885 2, 321-328 (2013) 915 Structural Biology (GB); French École Nor-
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887 High-Throughput, High-Resolution Protocol 917 Complex System Institute (NS).
888 for Three-Dimensional Reconstruction of Sin- 918 **Author contributions:** Conceptualization: NS,
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890 A., Kruhlak, M. (eds) Nanoimaging. Meth- 920 JP, OH, DP; Algorithms: NS, NL; User Inter-
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892 mana Press, Totowa, NJ. [https://doi.org/](https://doi.org/10.1007/978-1-62703-137-0_11) 922 NS, NL, GB, JF, AM, GW; Experimental work:
893 10.1007/978-1-62703-137-0_11 923 JF, AM, AK, GW, AA; Electron microscopy: JF,
894 ⁵⁵ Abramoff, M. D., Magalhães, P. J. & Ram, S. 924 AM, AK, GW, AA; Data analysis: GB, JF, AM,
895 J. Image Processing with ImageJ. Biophotonics 925 AK, GW, AA; Visualization: JF, GB; Funding
896 International 11, 36-42 (2004) 926 acquisition: GB, NS; Project administration:
897 ⁵⁶ Huang, CM., Kucinic, A., Johnson, J.A. et 927 NS, GB; Writing – original draft: NL, JF, NS,
898 al. Integrated computer-aided engineering and 928 GB; Writing – review & editing: NS, GB, JF,
899 design for DNA assemblies. Nat. Mater. 20, 929 NL, AK, GW.
900 1264-1271 (2021) 930 **Competing interests:** The authors have no
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902 glas, Design principles for accurate folding of 932 **Code and data availability:** ENSnano source
903 DNA origami, Proc. Natl. Acad. Sci. U.S.A. 121 933 code is available in the public Github repos-
904 (48) e2406769121 (2021) 934 itory²⁸; the .ens and .xlsx files for the de-
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