

0.5  $\mu\text{m}$

Gelatin :

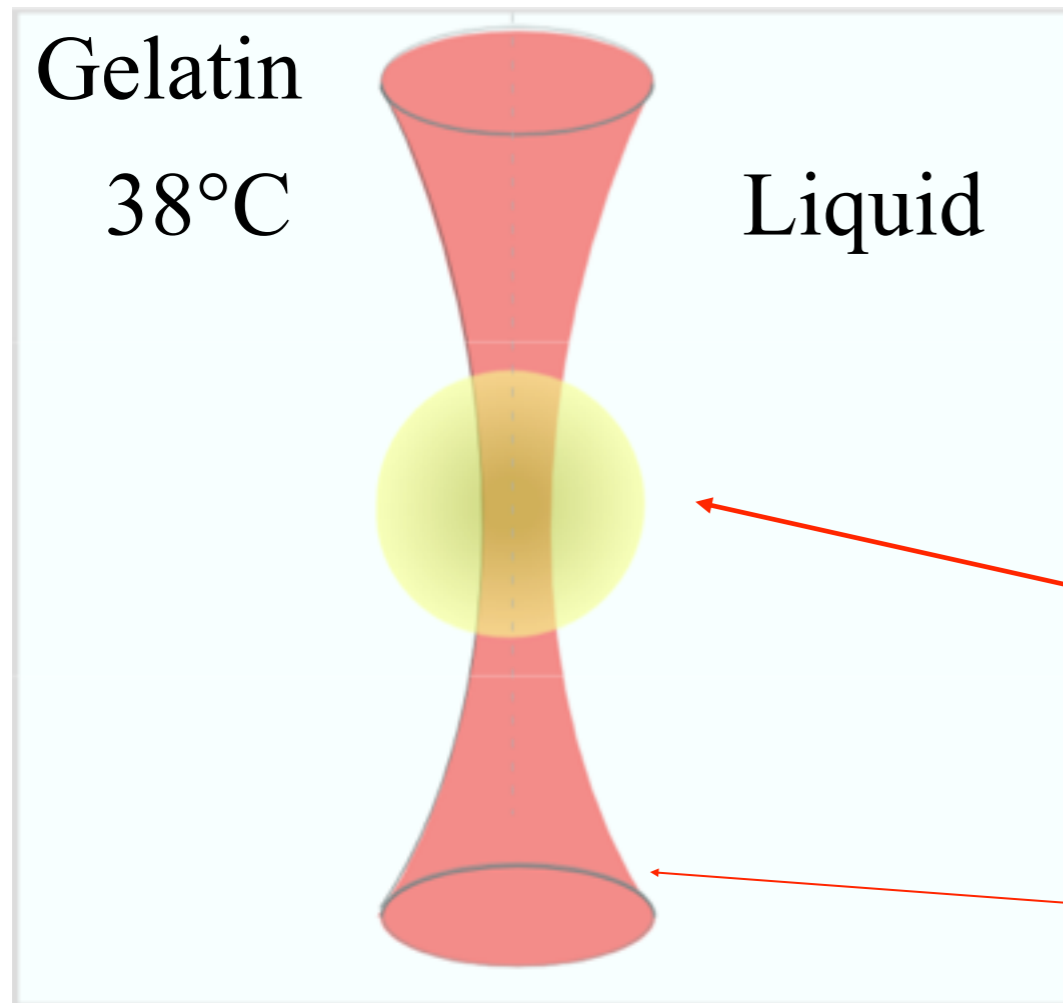
liquid for  $T_m > 32^\circ\text{C}$

solid for  $T_g < 28^\circ\text{C}$

In our experiment we use

10%wt concentration in water

For  $T < T_g$  gelatin presents : aging and memory effects  
at 10%wt concentration after a cooling at  $26^\circ\text{C}$  it takes  $\sim 2\text{h}$  to solidify



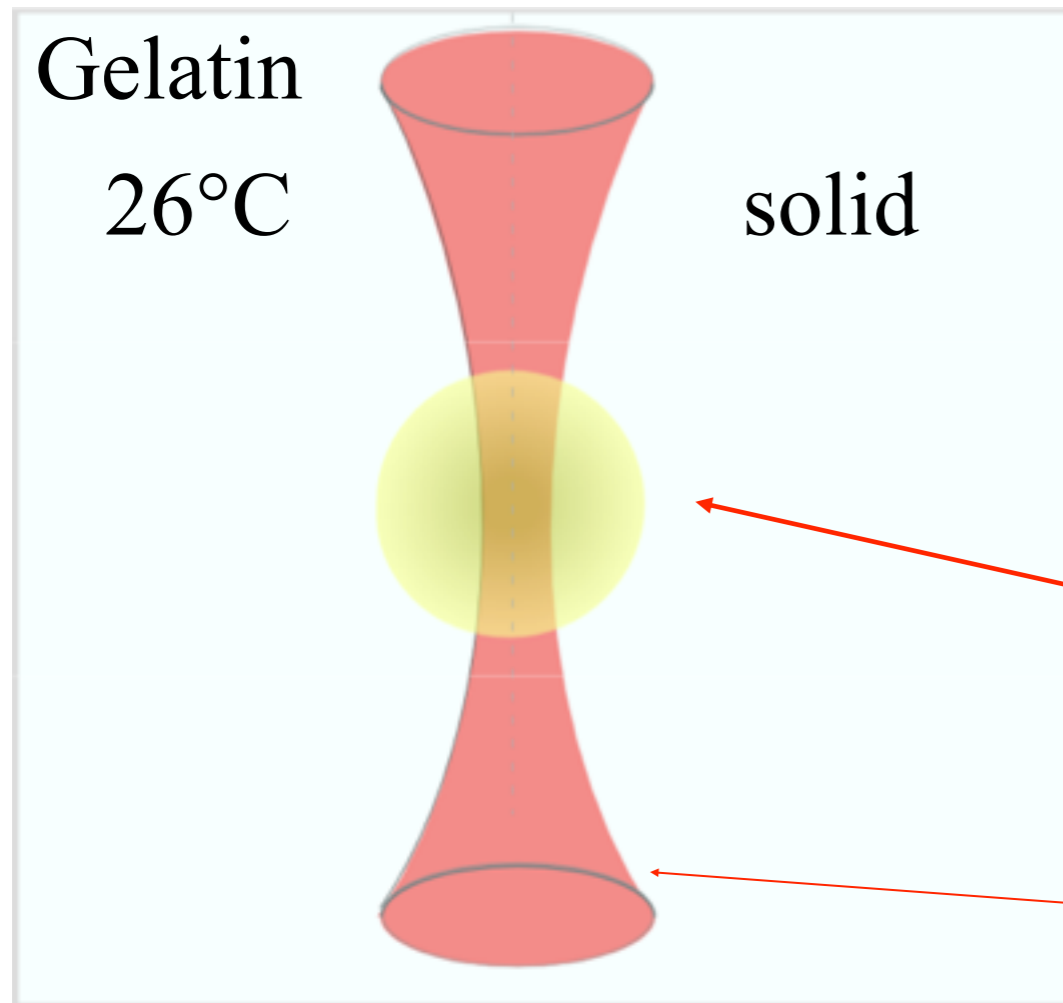
Gelatin :  
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Trapped glass particle  $R=1\mu\text{m}$

Trapping laser

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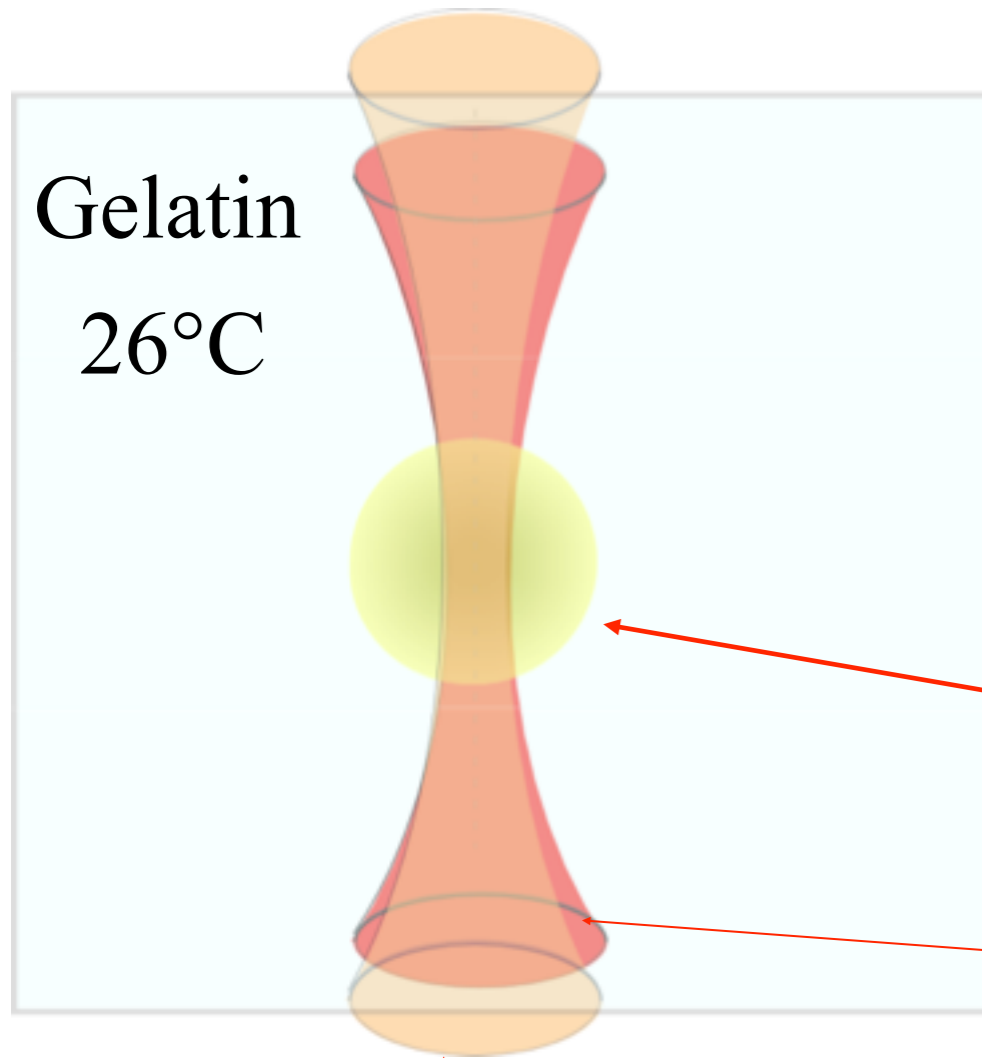
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# Gelatin liquid-solid transition (heating)

Gelatin  
26°C



Trapped glass particle  $R=1\mu\text{m}$

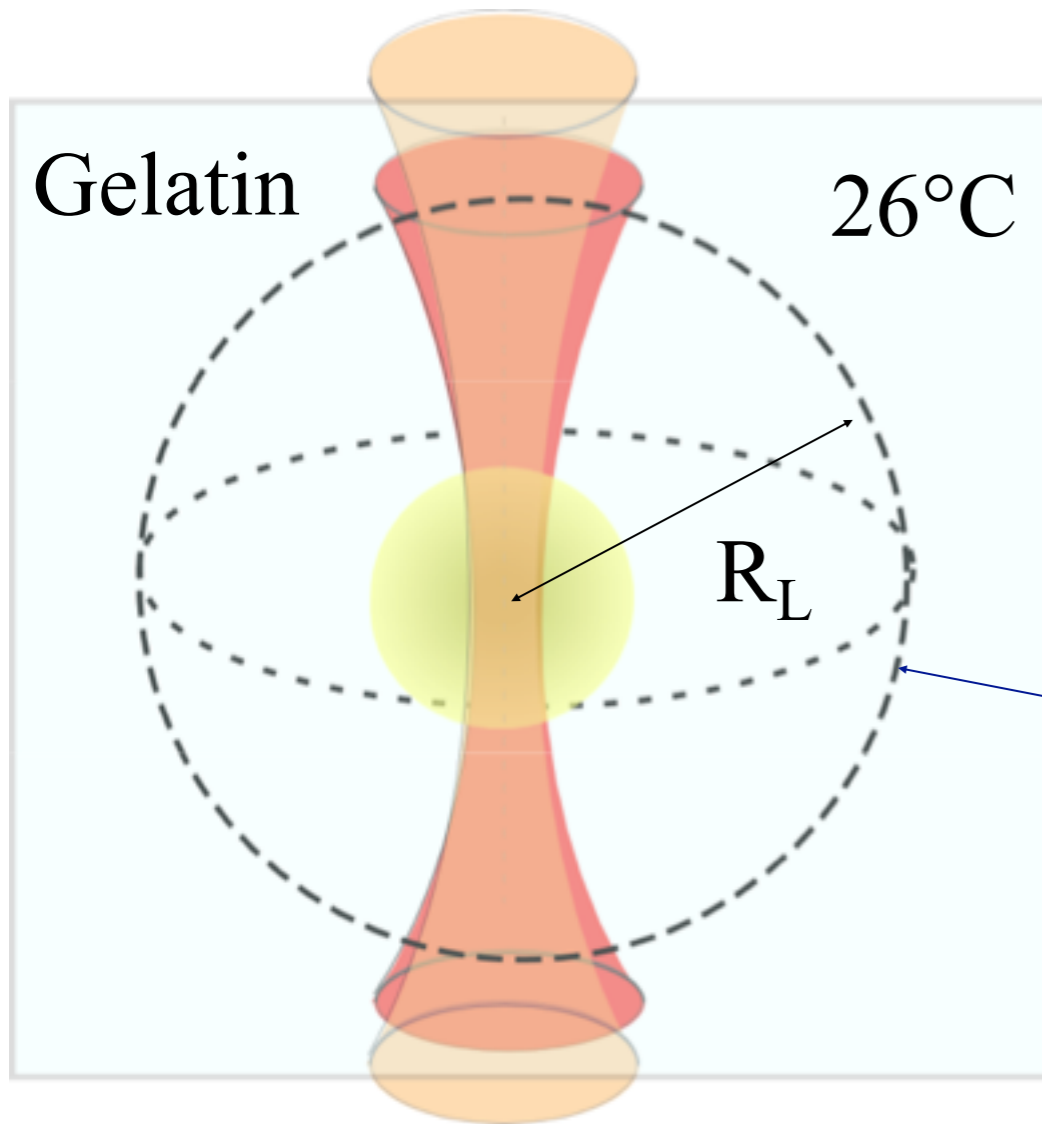
Trapping laser

Infrared Laser switched on for a few minutes

Gelatin :  
liquid for  $T_m > 32^\circ\text{C}$   
solid for  $T_g < 28^\circ\text{C}$



# Gelatin liquid-solid transition (heating)

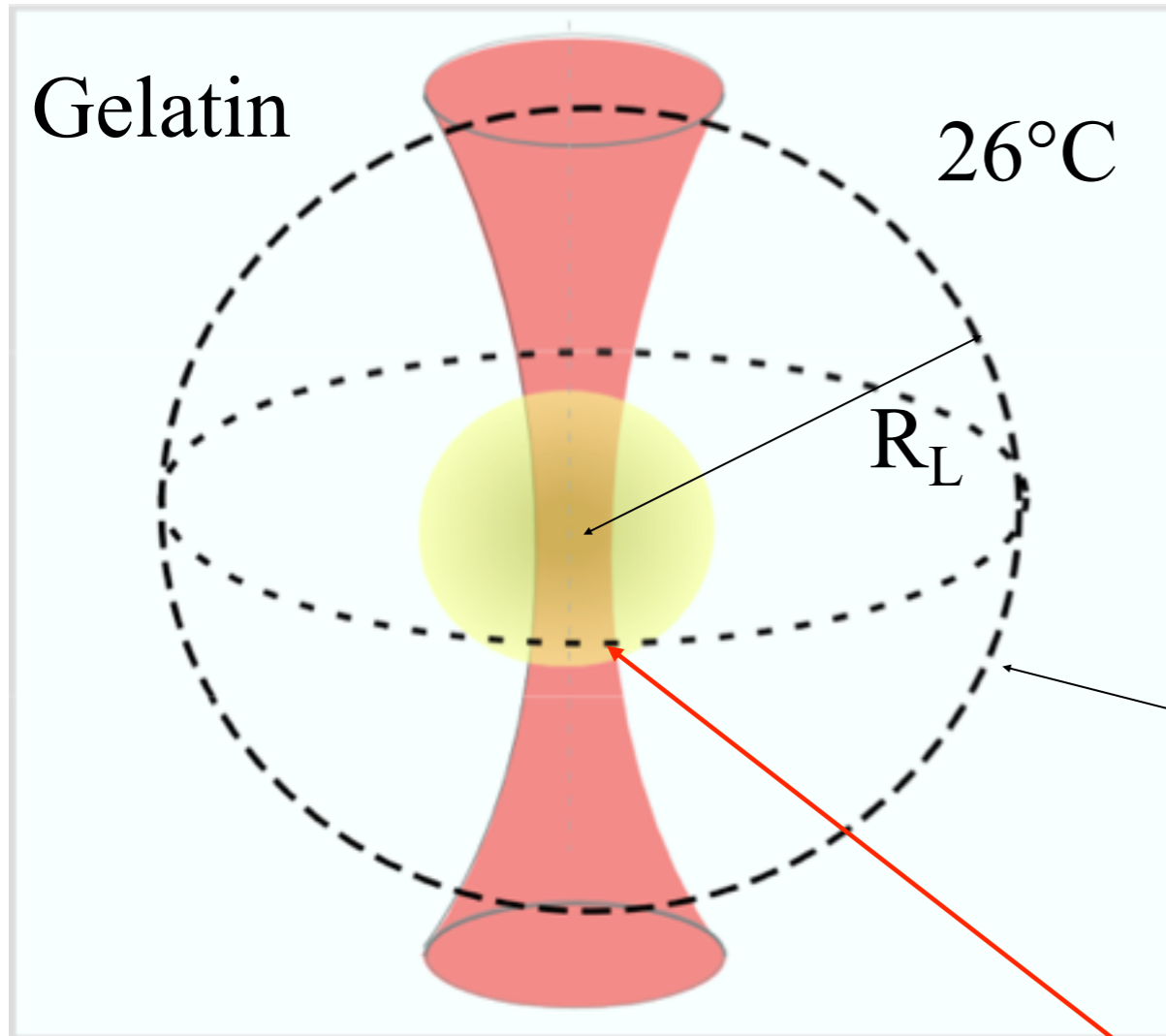


The temperature around the focus grows till 38°C and the gel melts

A drop of liquid of radius  $R_L=5 \mu\text{m}$  is formed

Infrared Laser switched on for a few minutes

# Gelatin liquid-solid transition (quench)



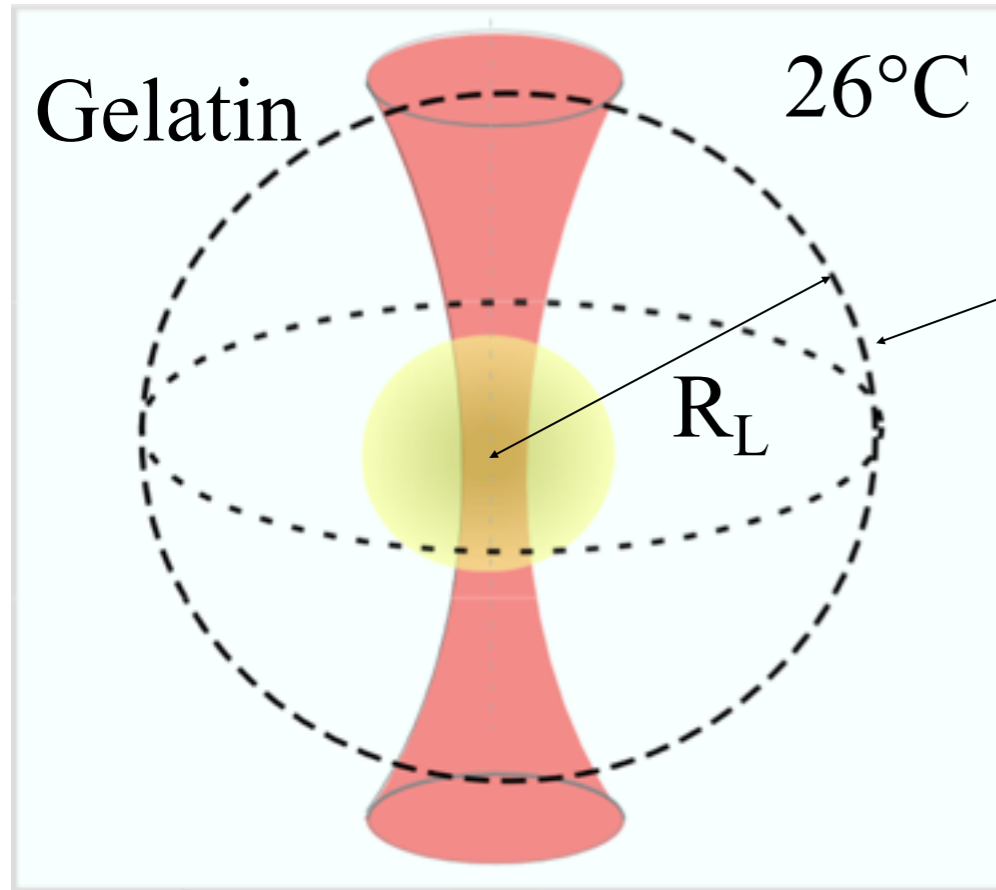
The infrared laser is switched off  
and  
the liquid drop cools very fast

At  $t=1\text{ms}$  after the switch off  
we obtain:

A drop of an unstable liquid  
at 26°C inside a stable solid

Trapped glass particle  $R=1\mu\text{m}$

# Gelatin liquid-solid transition (quench)



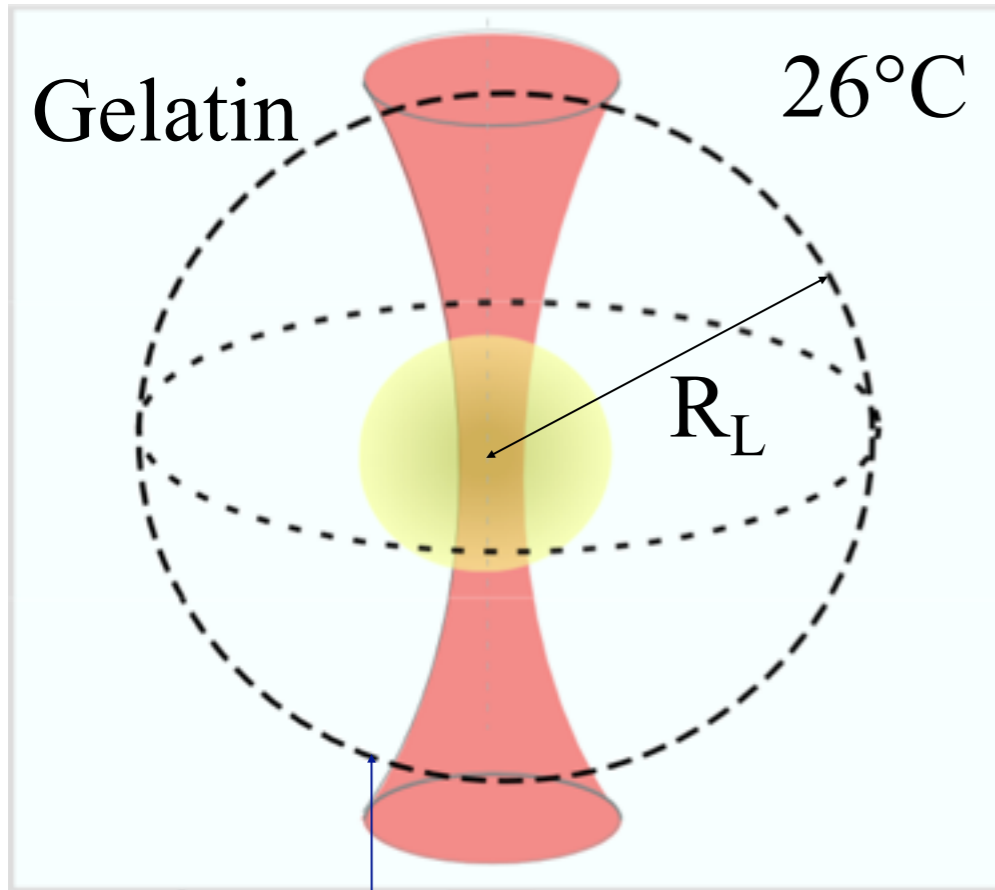
Drop of an unstable liquid at 26°C inside a stable solid

What happens ?

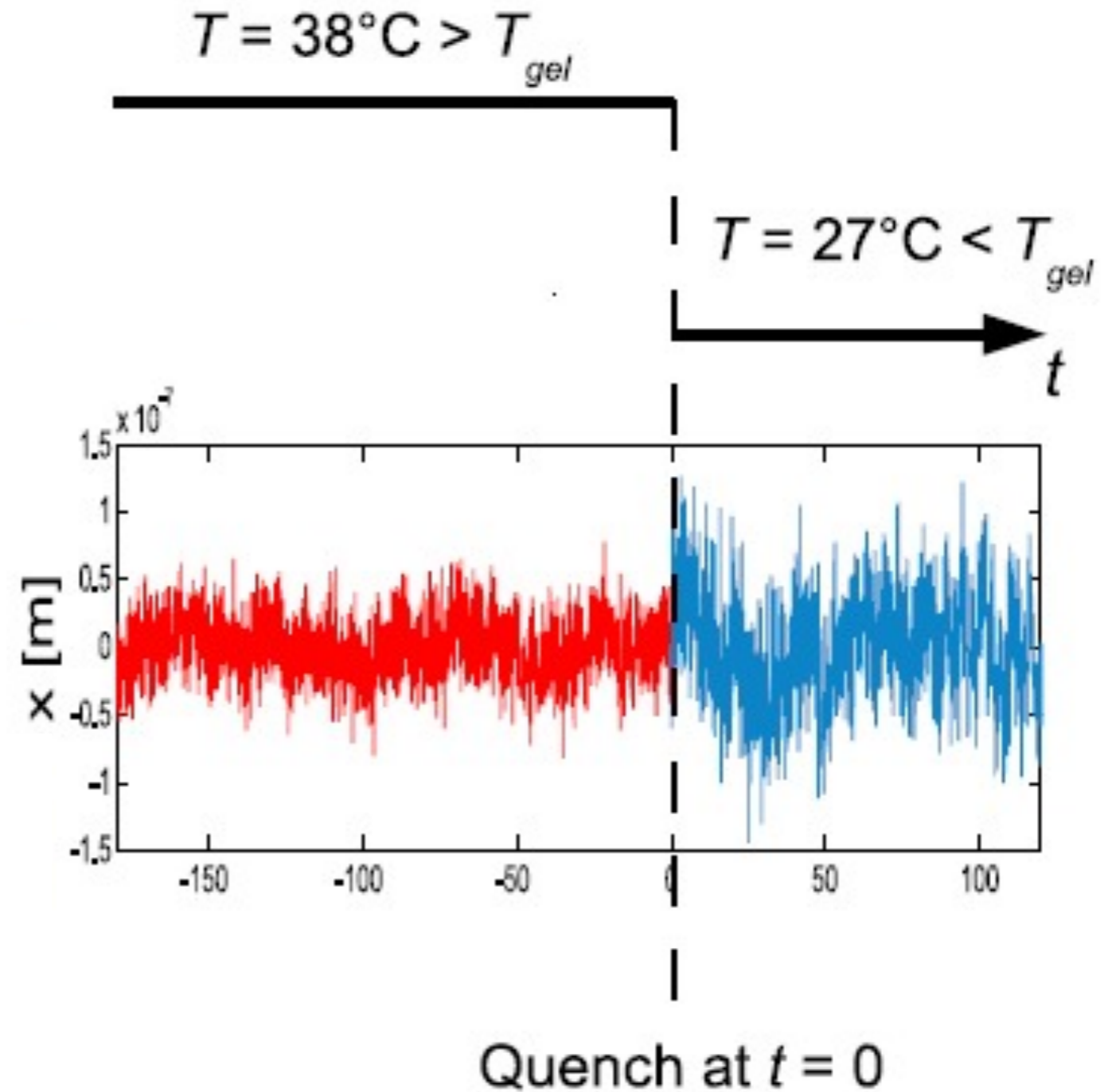
How long does it take to solidify ?

Does the transition start from the frontier ?

What is the nature of the bead fluctuations inside the drop ?



Drop of the unstable liquid at 26°C inside the stable solid

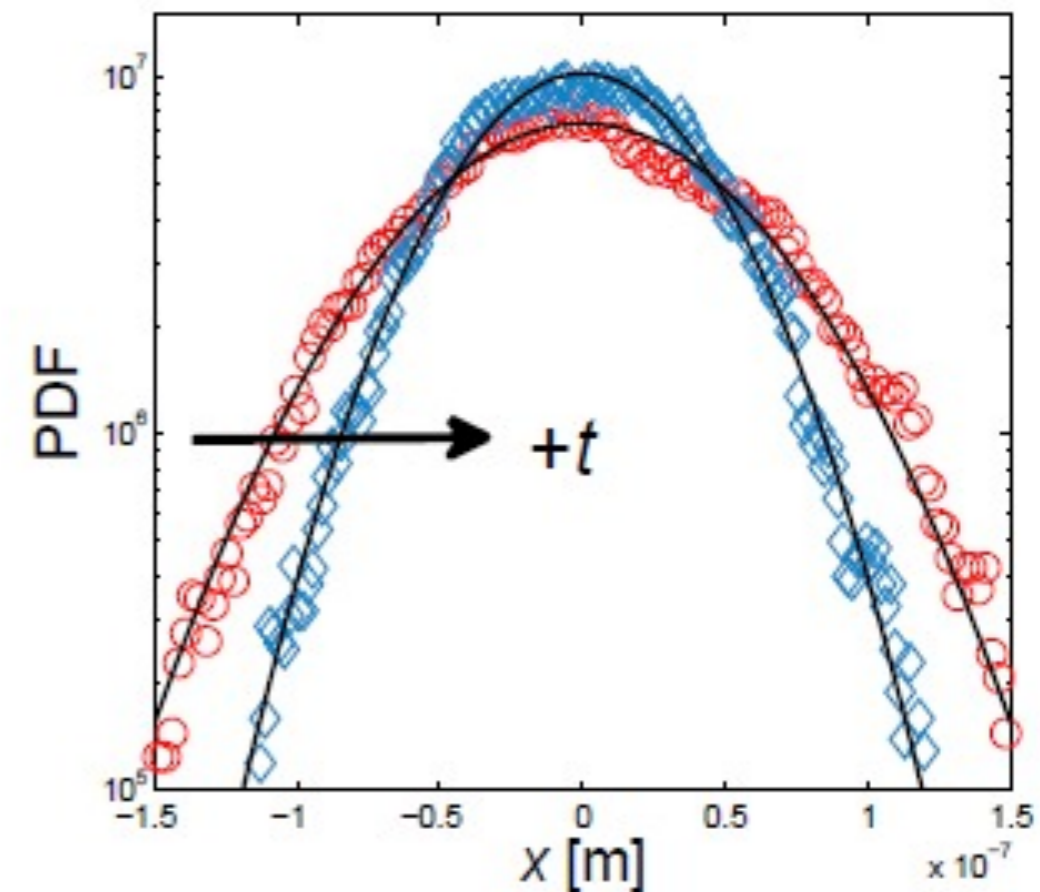
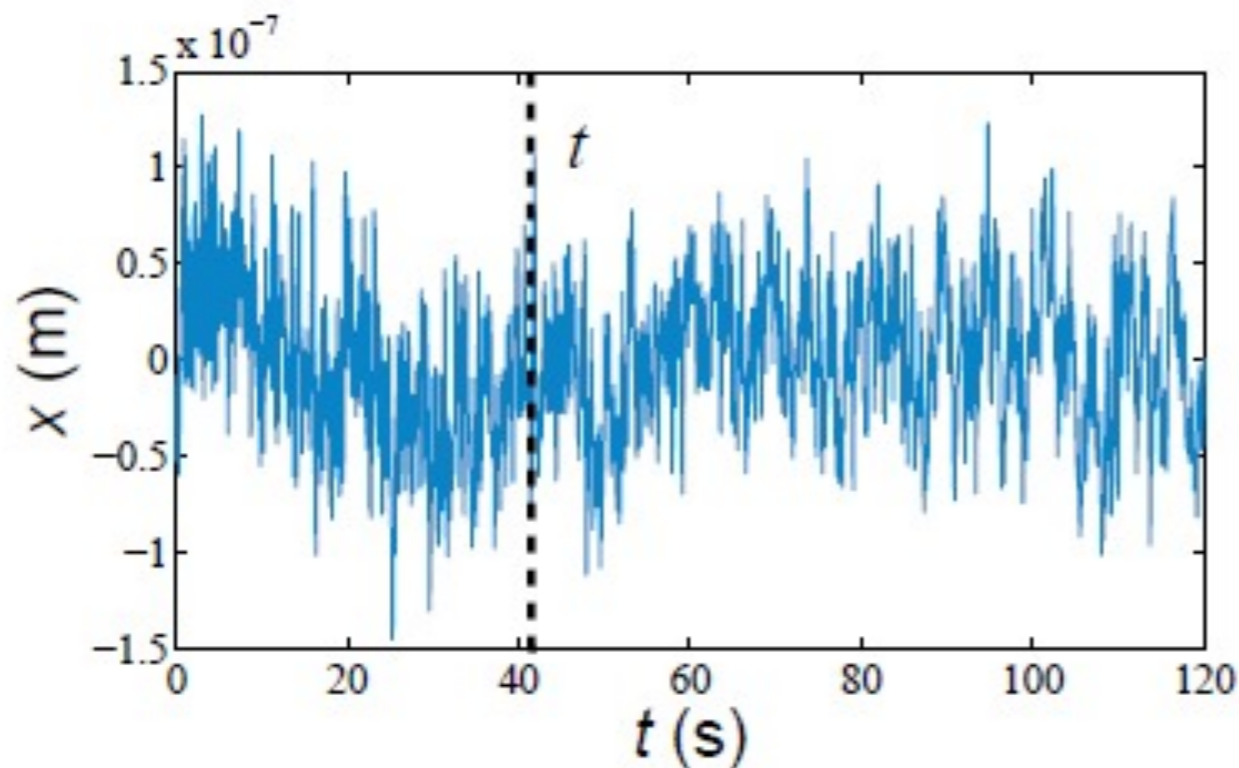




## Particle motion during the gelation process

Probing nonequilibrium particle dynamics through the **variance**  $\sigma_x^2$  of its position  $x$  [Gomez-Solano et al., arXiv:1102.4750]:

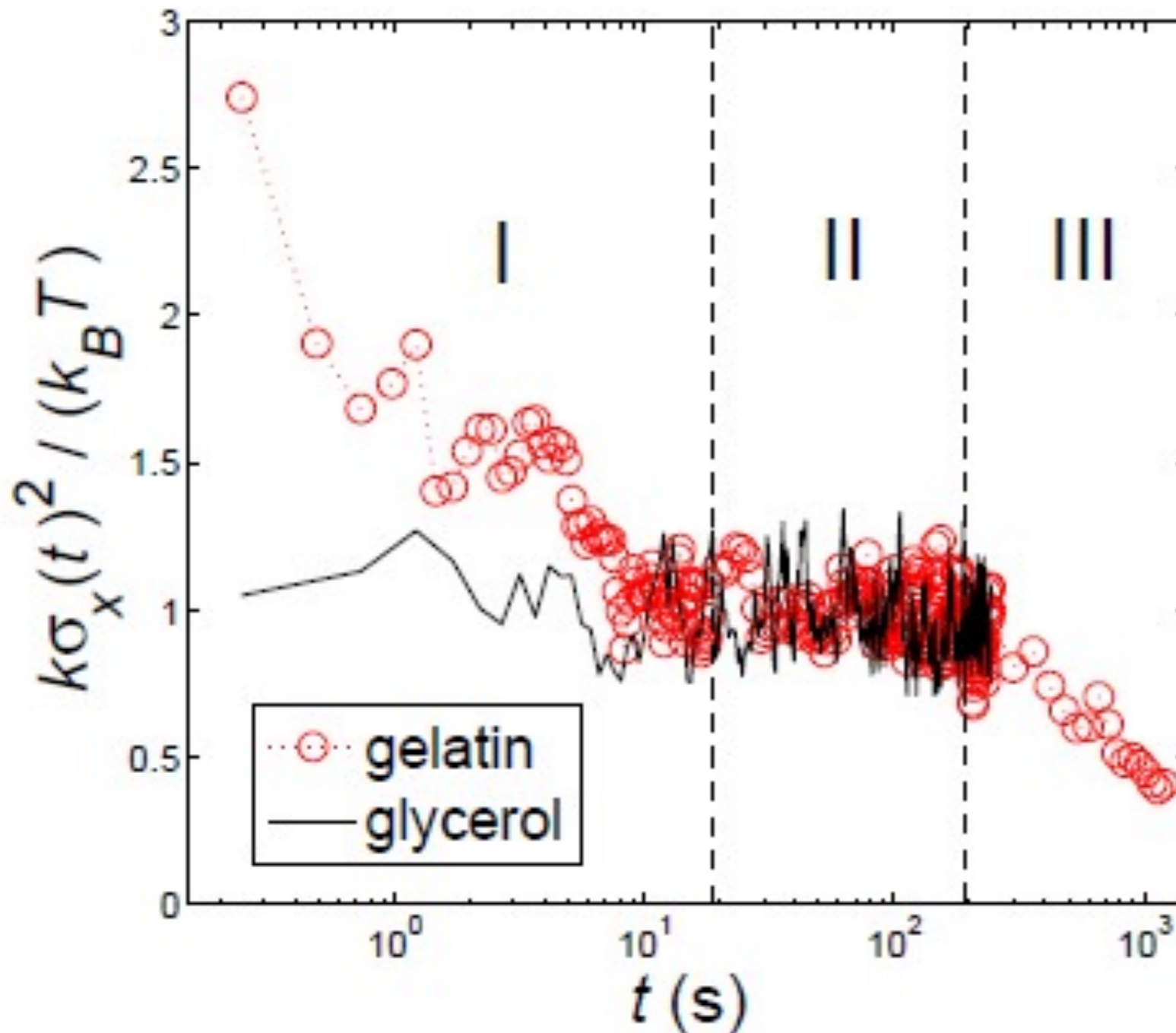
- ▶ Nonstationarity:  $\sigma_x(t)$  computed at each  $t$  over an ensemble of independent quenches.
- ▶ Fluctuations of  $x$  are Gaussian for all  $t \geq 0$ .



The measured  $\sigma^2(t)$  is compared to the equilibrium value  $\sigma_{eq}^2$  of the trap

From equipartition

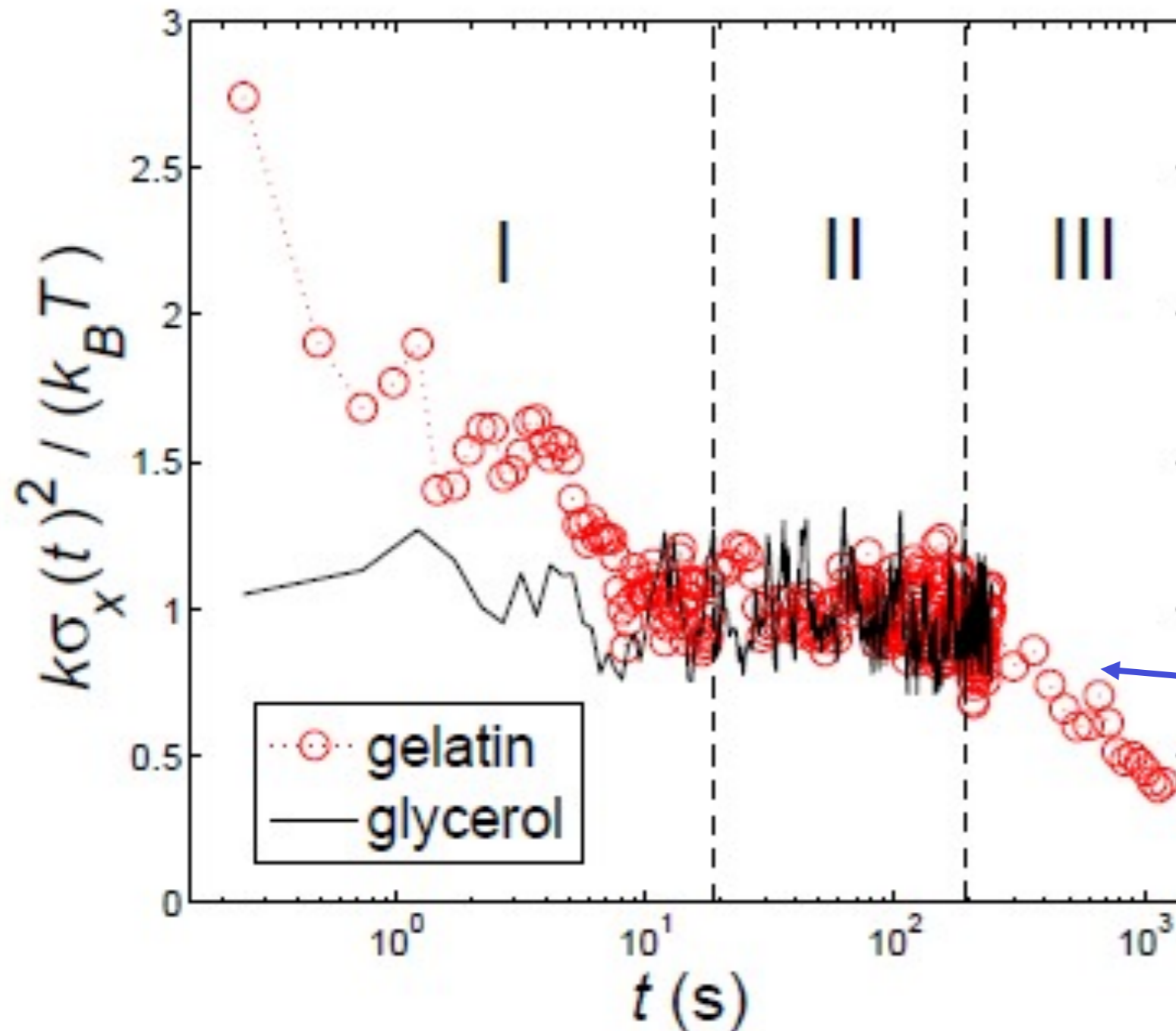
$$\sigma_{eq}^2 = \frac{k_B T}{k}$$



The measured  $\sigma^2(t)$  is compared to the equilibrium value  $\sigma_{eq}^2$  of the trap

From equipartition

$$\sigma_{eq}^2 = \frac{k_B T}{k}$$



$$\sigma^2(t) = \frac{k_B T}{(k + \tilde{k}_{gel})}$$

Motion of a Brownian particle trapped by a laser Beam

Viscoelastic Langevin dynamics

$$\int_{-\infty}^t \Gamma(t - t', t_w) \dot{x}(t') dt' + k (x - x_o) = \xi(t),$$

The applied oscillating force  $f_o(t) = k x_o(t)$

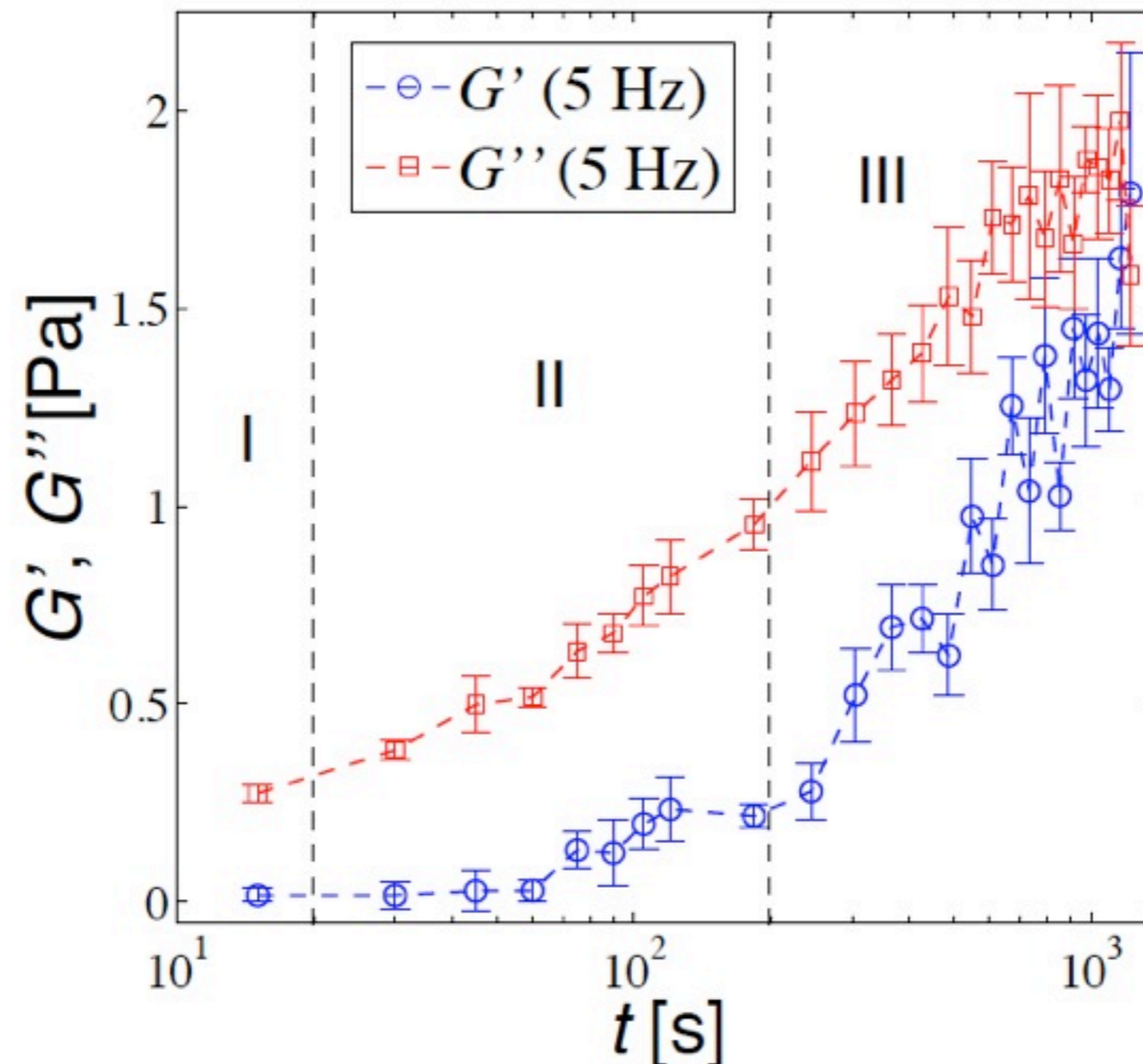
The linear response  $\hat{\chi}(\omega, t_w) = \frac{\hat{x}(\omega, t_w)}{\hat{f}_o(\omega)}$

$G'(\omega, t_w) \ 6 \ \pi \ r = \text{Re} \left[ \frac{1}{\chi(\omega, t_w)} \right] - k$  Elastic modulus

$G''(\omega, t_w) \ 6 \ \pi \ r = \text{Im} \left[ \frac{1}{\chi(\omega, t_w)} \right] / \omega$  Viscosity

## Time evolution of the viscous and elastic modulus

- I. Pure viscous
- II. Negligible elasticity
- III. Logarithmic growth of  $G'$  et  $G''$



$$\Delta U_\tau(t_w) - W_\tau = Q_\tau(t_w),$$

For  $F = 0$  :  $W_\tau = 0$  and

$$\Delta U_\tau(t_w) = Q_\tau(t_w)$$

$$\Delta U_\tau(t_w) = \frac{1}{2}k(x(t_w + \tau)^2 - x(t_w)^2) + \int_{t_w}^{t_w + \tau} \dot{x}(t)(K_t * x)(t, t_w)dt,$$

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Gel elasticity

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for  $t_w < 200s$



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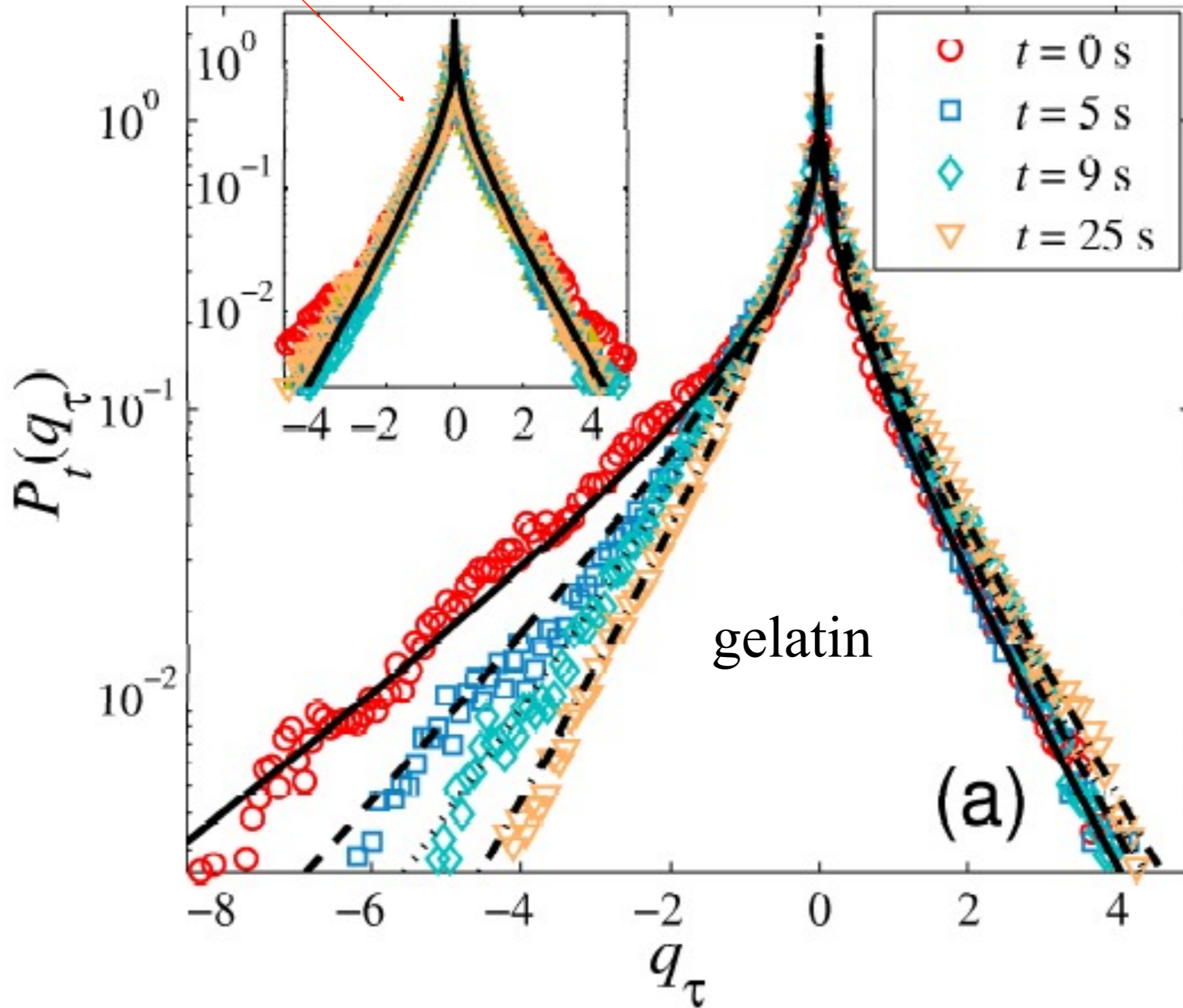
for  $t_w < 200s$

For  $t_w < 200s$ ,  $Q_{\tau}$  can be computed from  $\Delta U_{\tau}$ .

# Energy PDF

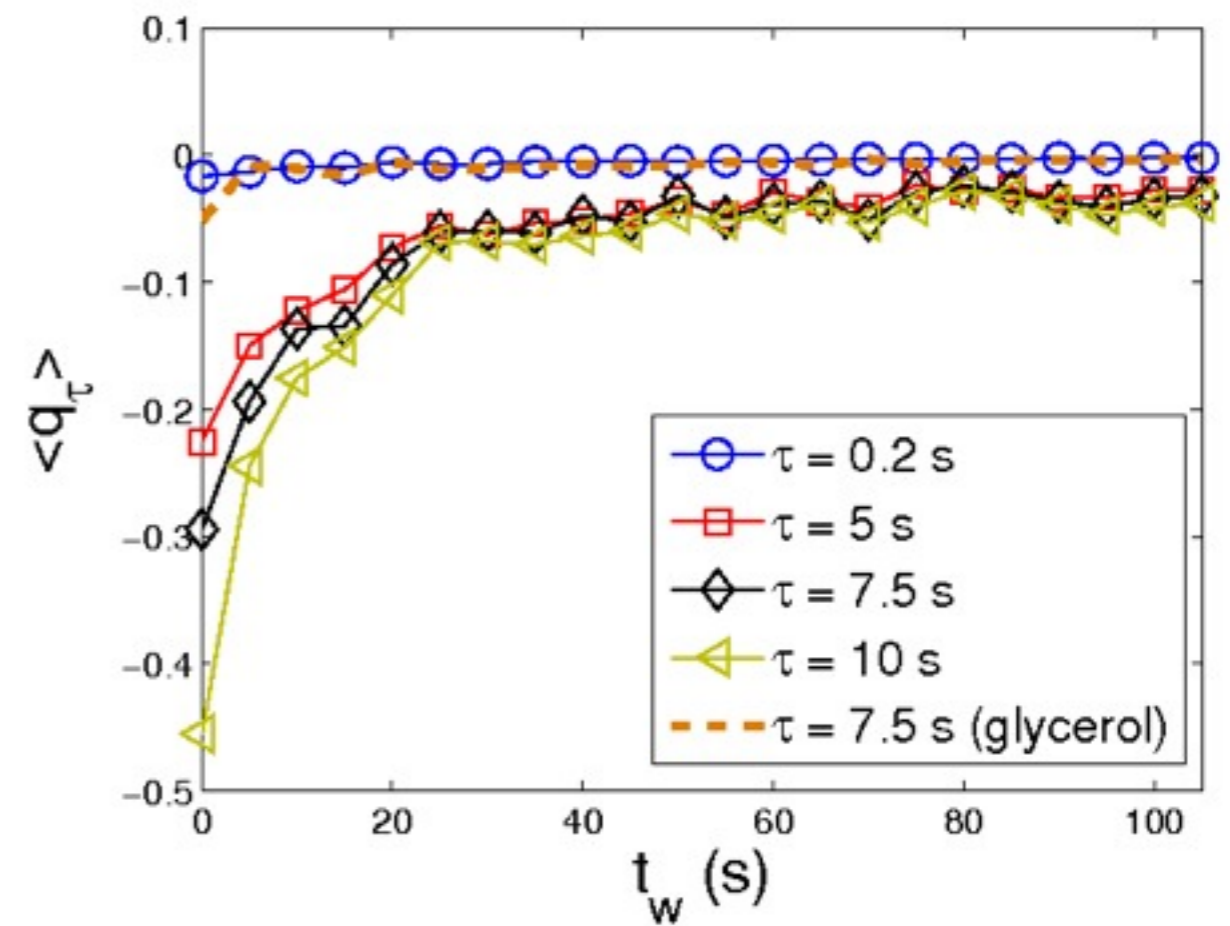
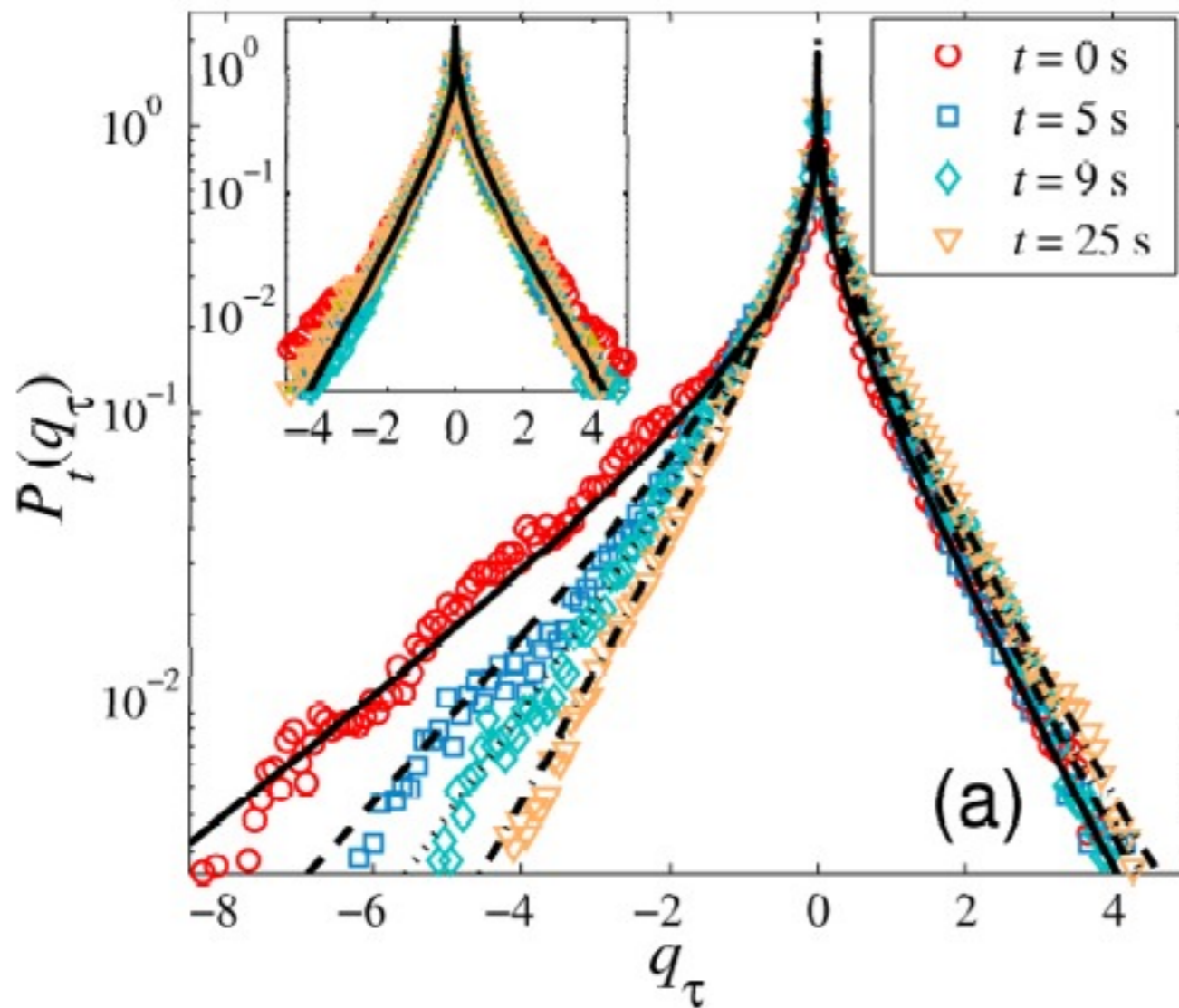
glicerol

$$q_\tau = \frac{Q_\tau}{k_B T}$$

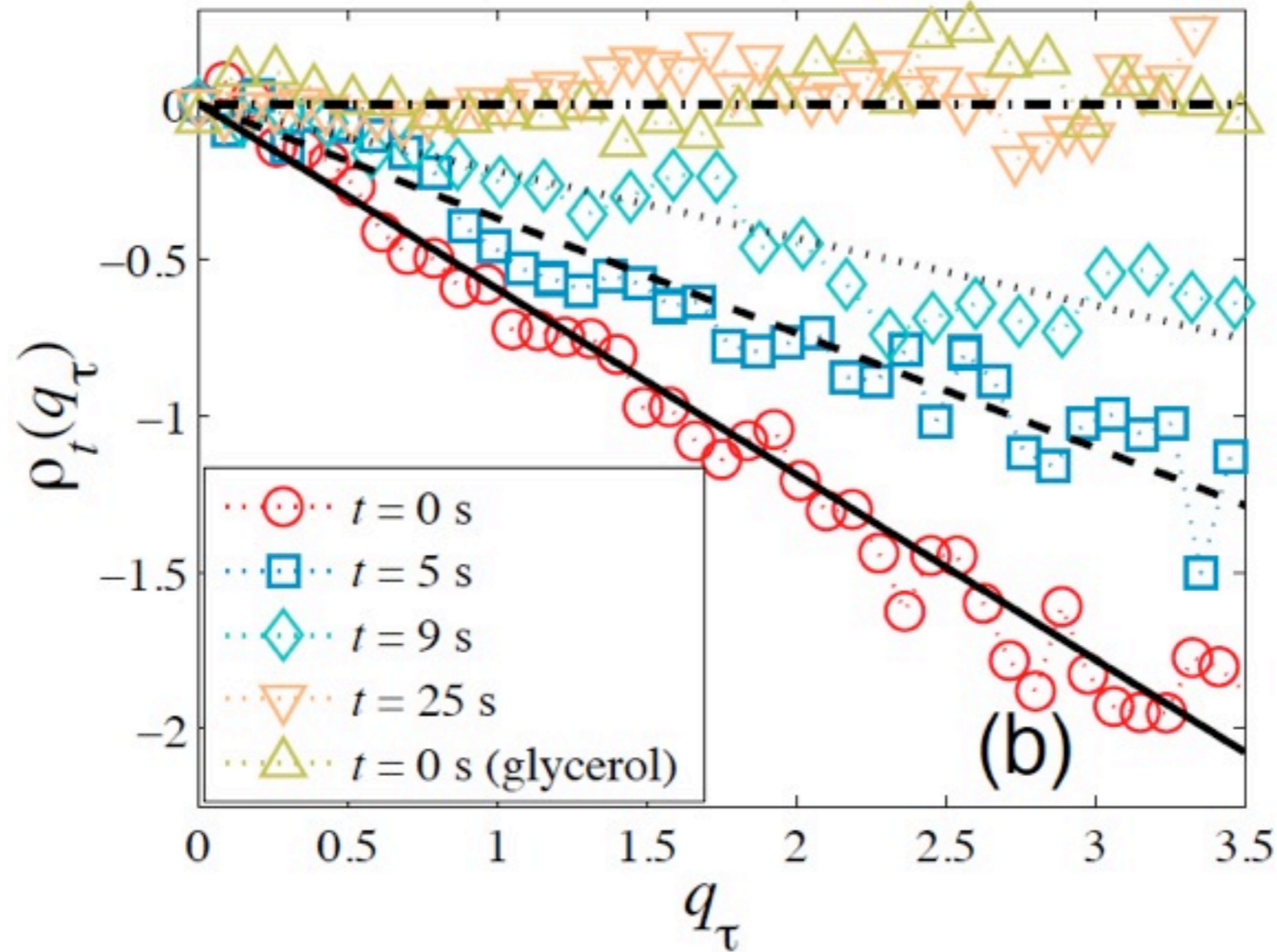


(a)

$$q_\tau = \frac{Q_\tau}{k_B T}$$



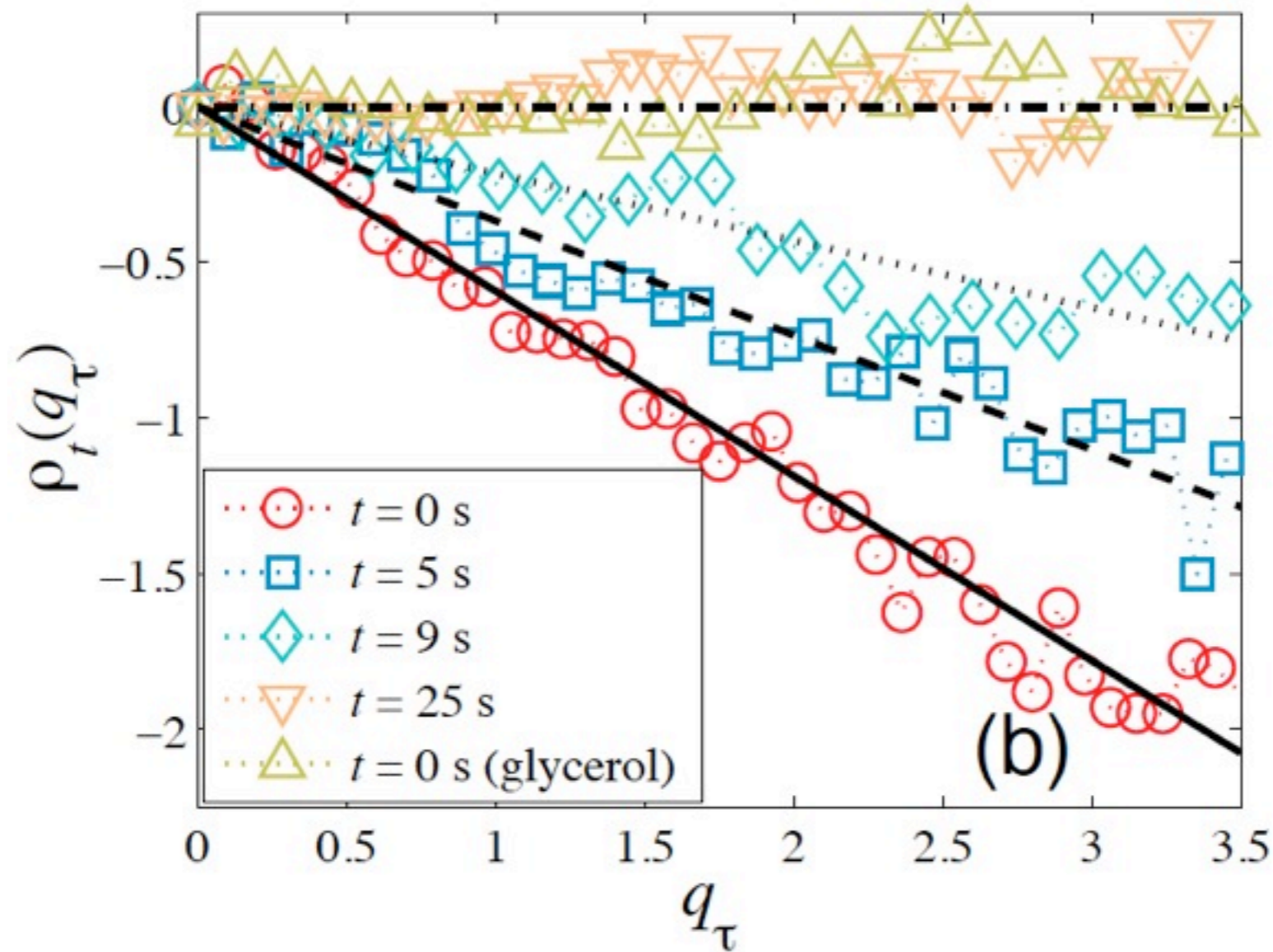
Mean heat



FT fixes the symmetries of the PDF

$$\rho(q_\tau) = \log \frac{P(q_\tau)}{P(-q_\tau)}$$

$$\rho(\tau) = \Delta \beta_{t,\tau} q_\tau \text{ for } \tau \rightarrow \infty$$



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What is the value ?

# Data analysis

Using the experimental observation that  $P(x)$  are Gaussian  
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$$P_t(q_\tau) = \frac{A_{t,\tau}}{\pi} K_0 \left( B_{t,\tau} |q_\tau| \right) \exp \left( -\frac{\Delta_{t,\tau} A_{t,\tau}}{2} q_\tau \right),$$

where  $K_0$  is the zeroth-order modified Bessel function of the second kind,

$$\Delta_{t,\tau} = \frac{\sigma_x(t)}{\sigma_x(t+\tau)} - \frac{\sigma_x(t+\tau)}{\sigma_x(t)}, \quad A_{t,\tau} = \frac{k_B T}{k \sigma_x(t) \sigma_x(t+\tau)} \quad \text{and} \quad B_{t,\tau} = A_{t,\tau} \sqrt{1 + \Delta_{t,\tau}^2 / 4}$$

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from which

$$\Delta \beta_{t,\tau} = \frac{k_B T}{k} \left[ \frac{1}{\sigma_x(t+\tau)^2} - \frac{1}{\sigma_x(t)^2} \right].$$

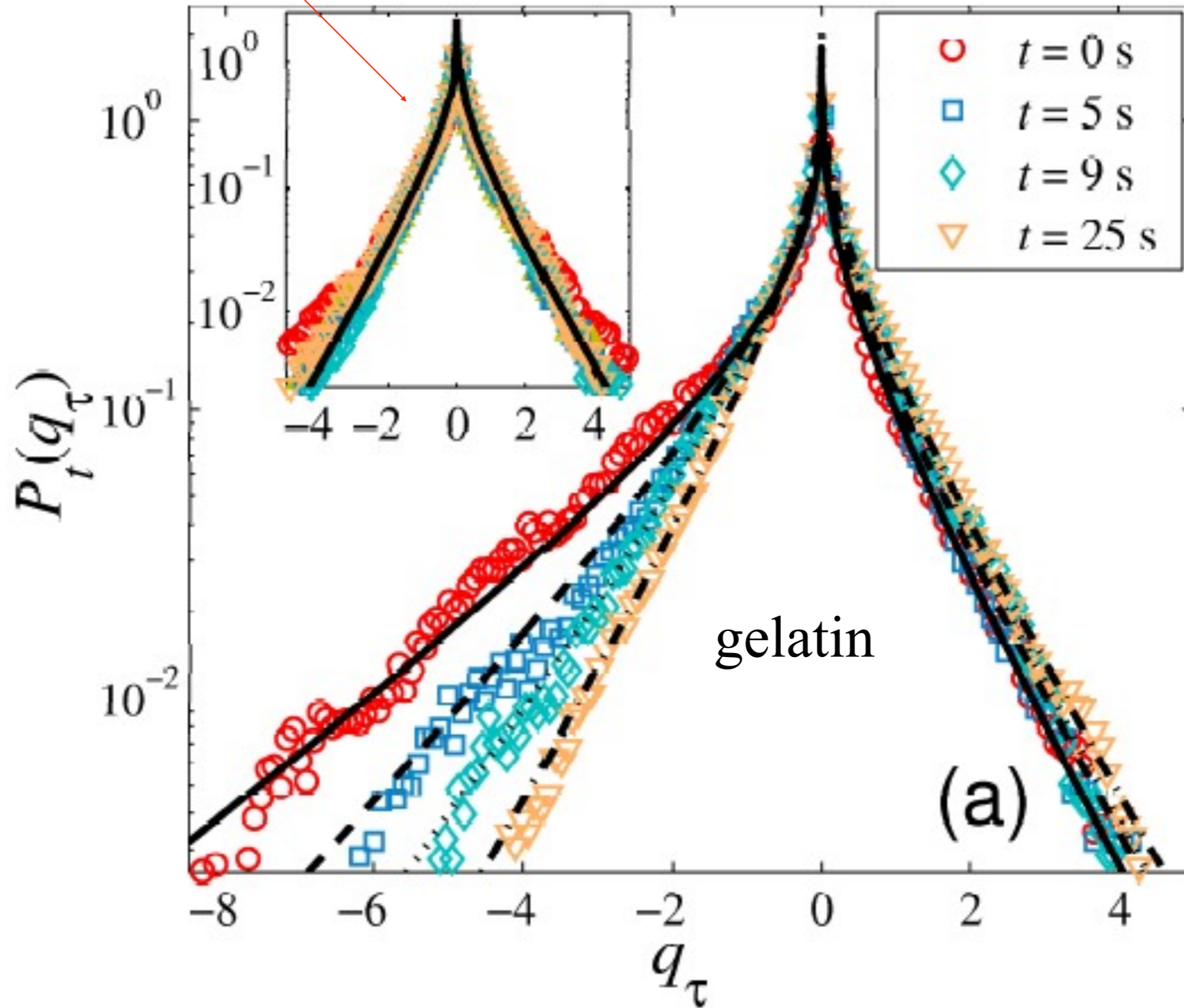
Hence, the linearity of  $\rho_t(q_\tau)$  is analytically satisfied



# Energy PDF

glicerol

$$q_\tau = \frac{Q_\tau}{k_B T}$$



(a)

Using an equipartition-like relation :  $k_B T_{eff}(t) = k \sigma_x(t)^2$

$$\Delta\beta_{t,\tau} = \left[ 1/T_{eff}(t + \tau) - 1/T_{eff}(t) \right] T,$$

Similar relations have been theoretically derived :

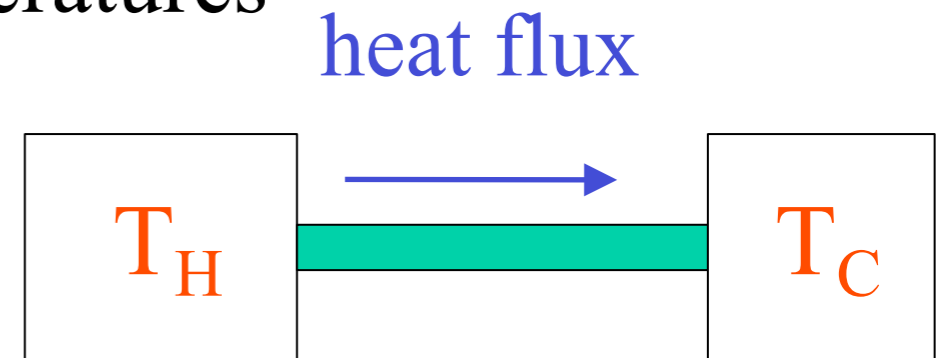
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A) In the **stationary case** for the heat flux between two reservoirs at different temperatures

$$\ln \frac{P(Q_\tau)}{P(-Q_\tau)} = \left( \frac{1}{T_C} - \frac{1}{T_H} \right) \frac{Q_\tau}{k_B}$$



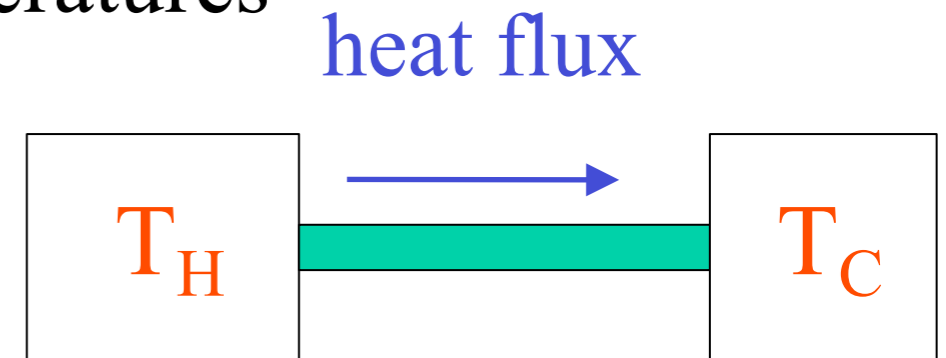
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- B) In the **non-stationary** case during the aging of spin glasses

A. Crisanti and F. Ritort, Europhys. Lett. **66**, 253 (2004).

From Fluctuation Theorem

$$\Delta S_{\tau} = -k_B \Delta \beta_{t,\tau} q_{t,\tau}$$

is the entropy production rate of the relaxation process

Comparing this result with numerical data of aging spin-glasses

*Aging can be interpreted as an heat transfer (cooling)  
of the slow modes towards the heat bath*

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## Conclusions

The liquid-solid transition is studied inside a drop of liquid after a very fast quench.

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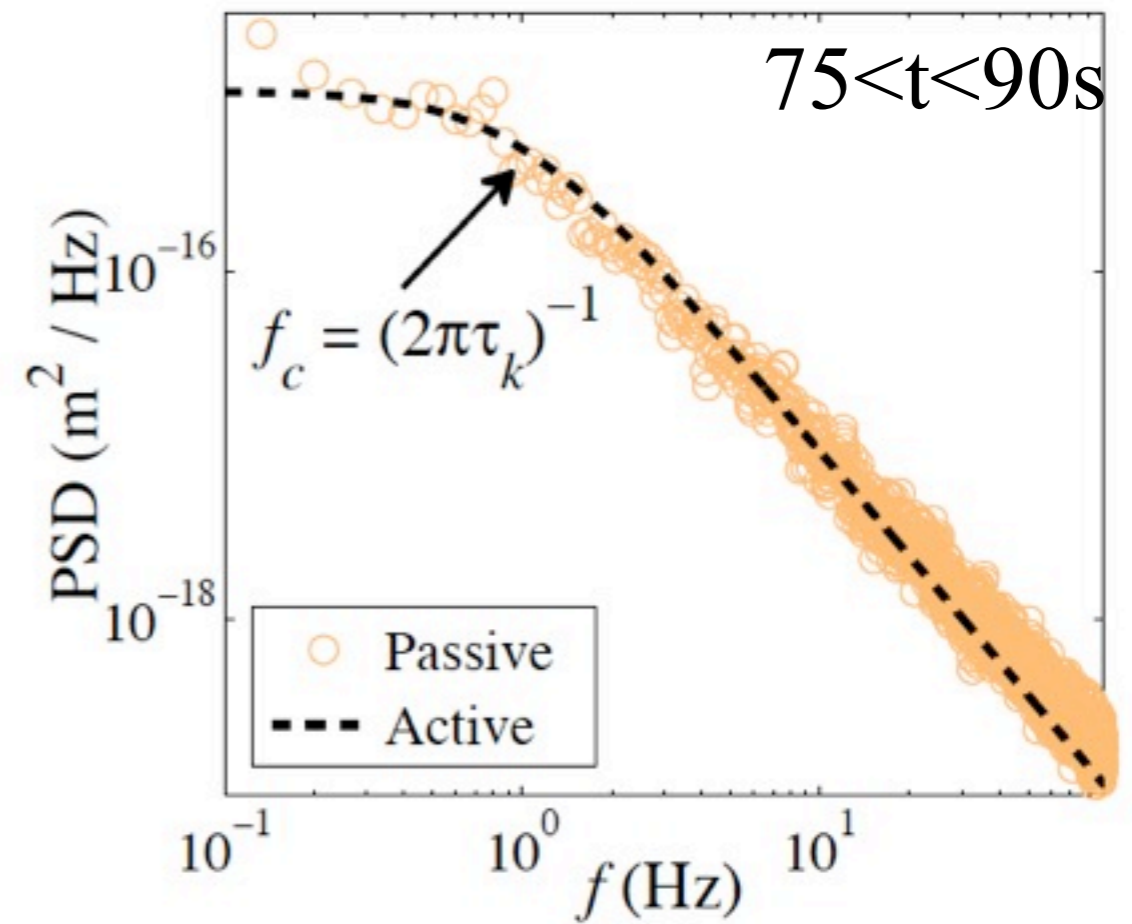
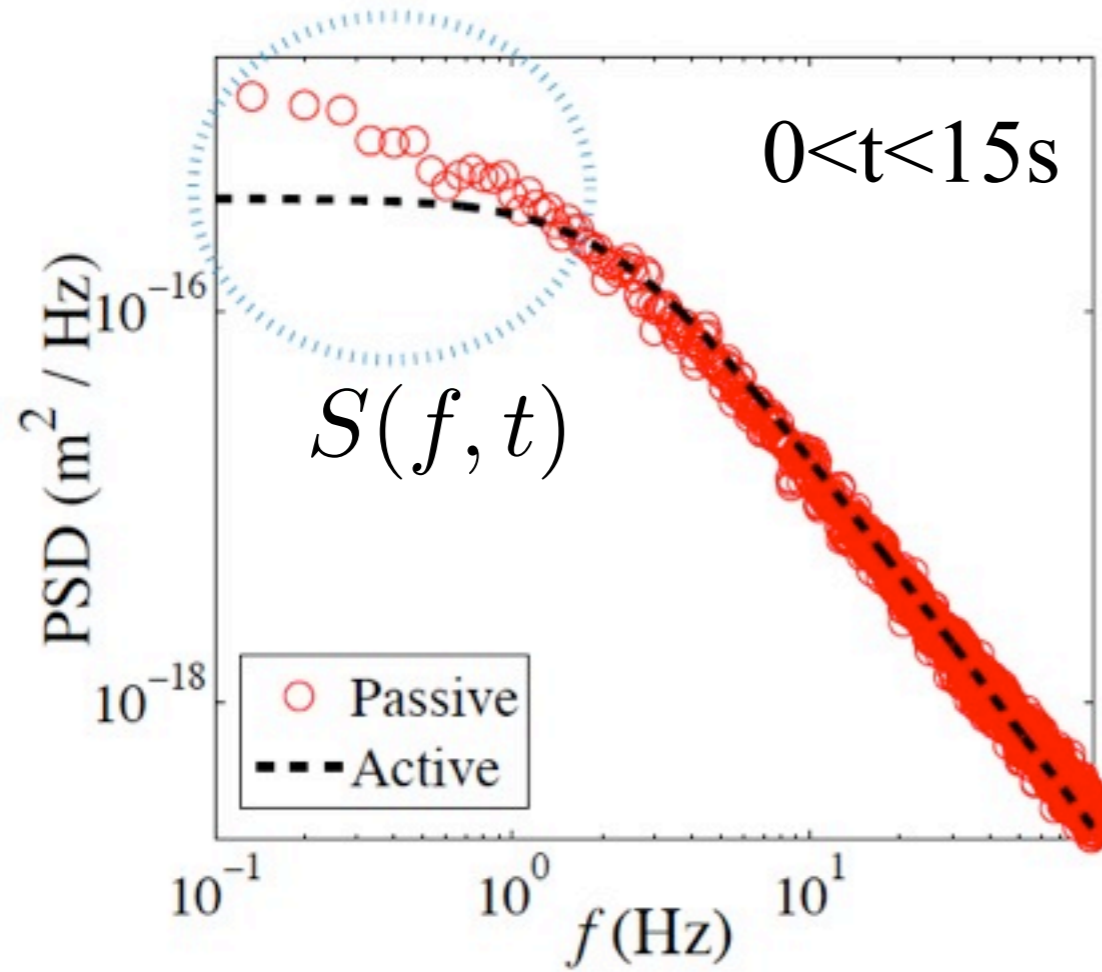
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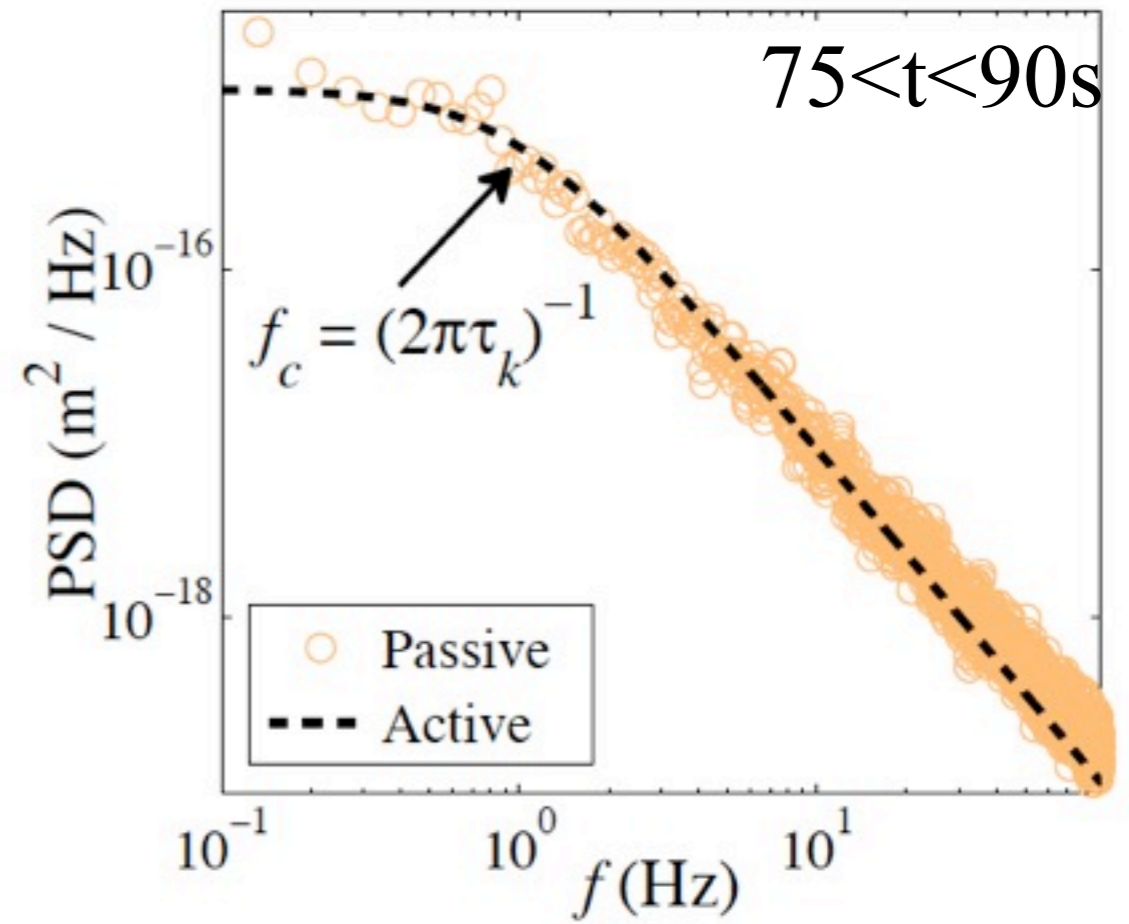
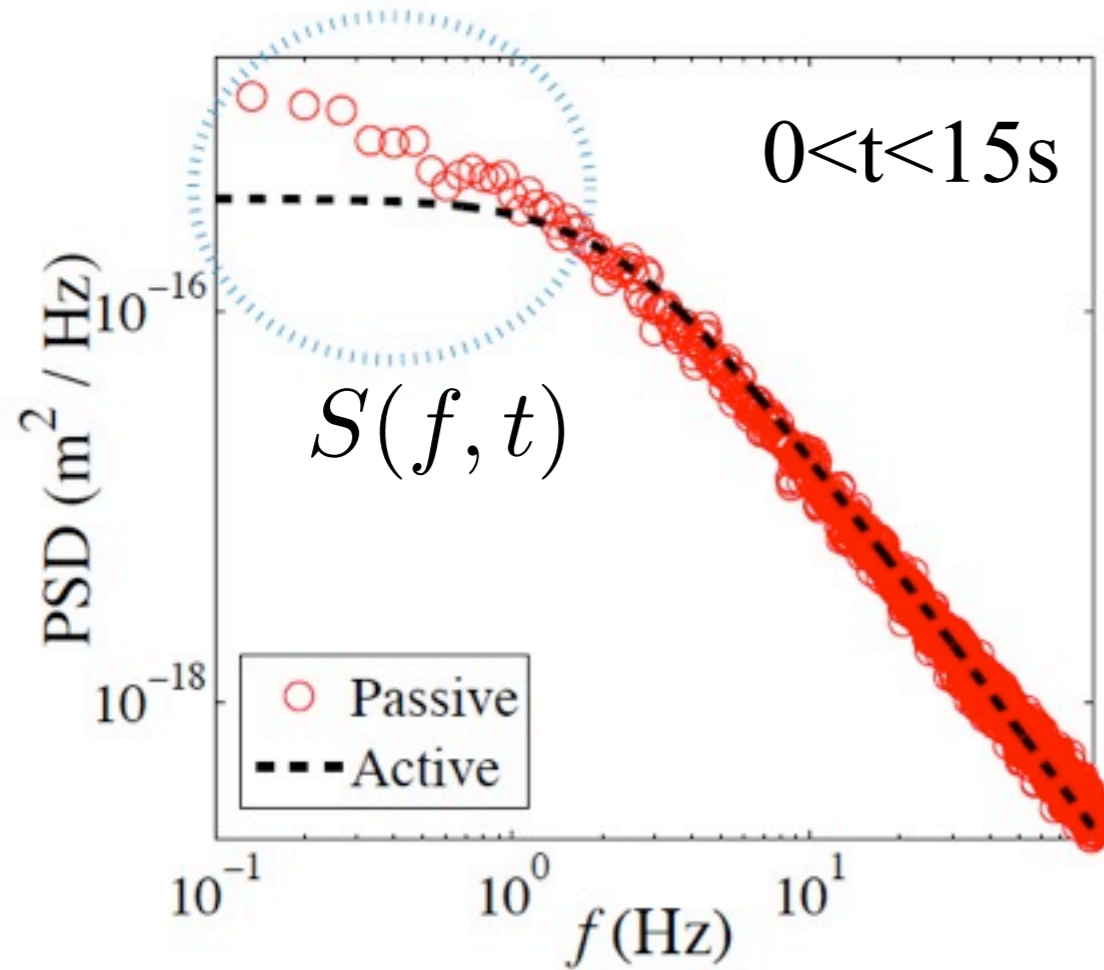
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- a) The fluctuations of heat are asymmetric, i.e. the dynamics transfer heat towards the bath
- b) The Fluctuation Theorem is satisfied in a non-stationary regime
- c) The Fluctuation Dissipation Theorem is violated



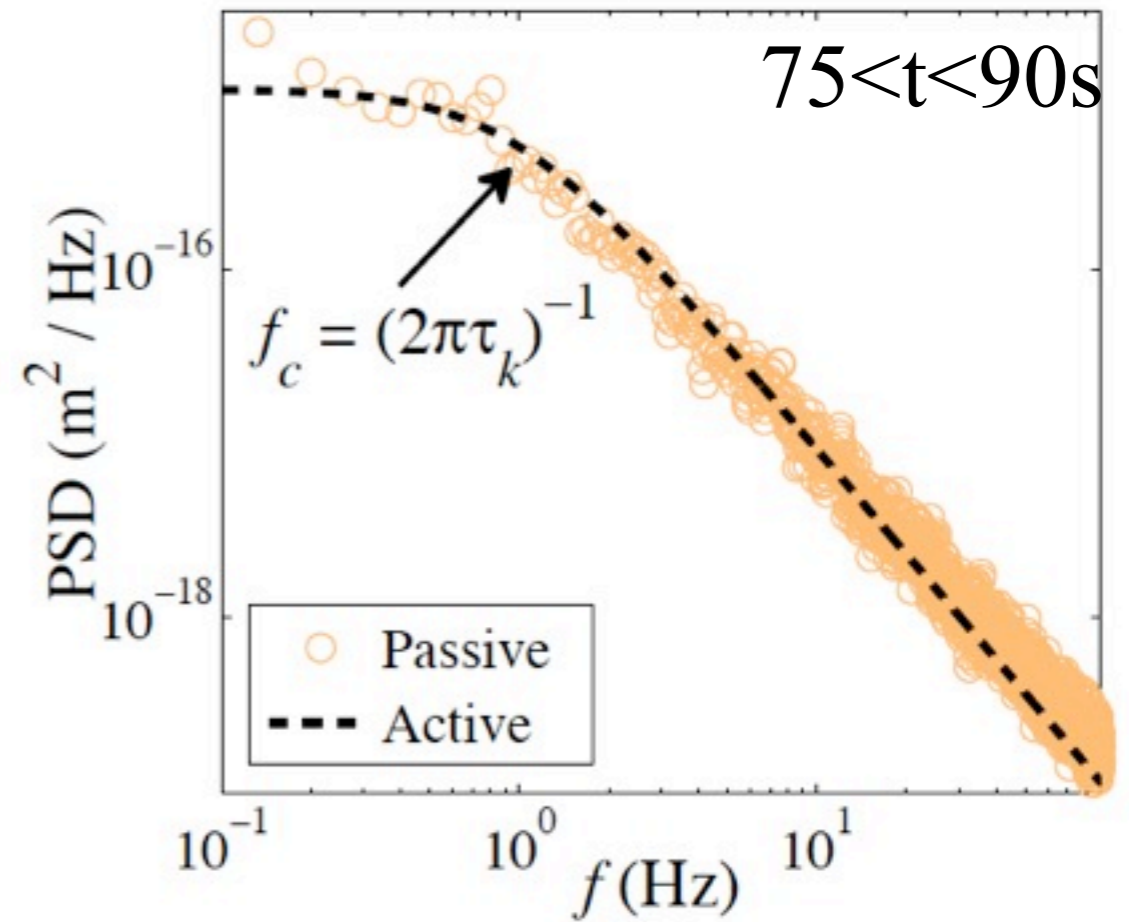
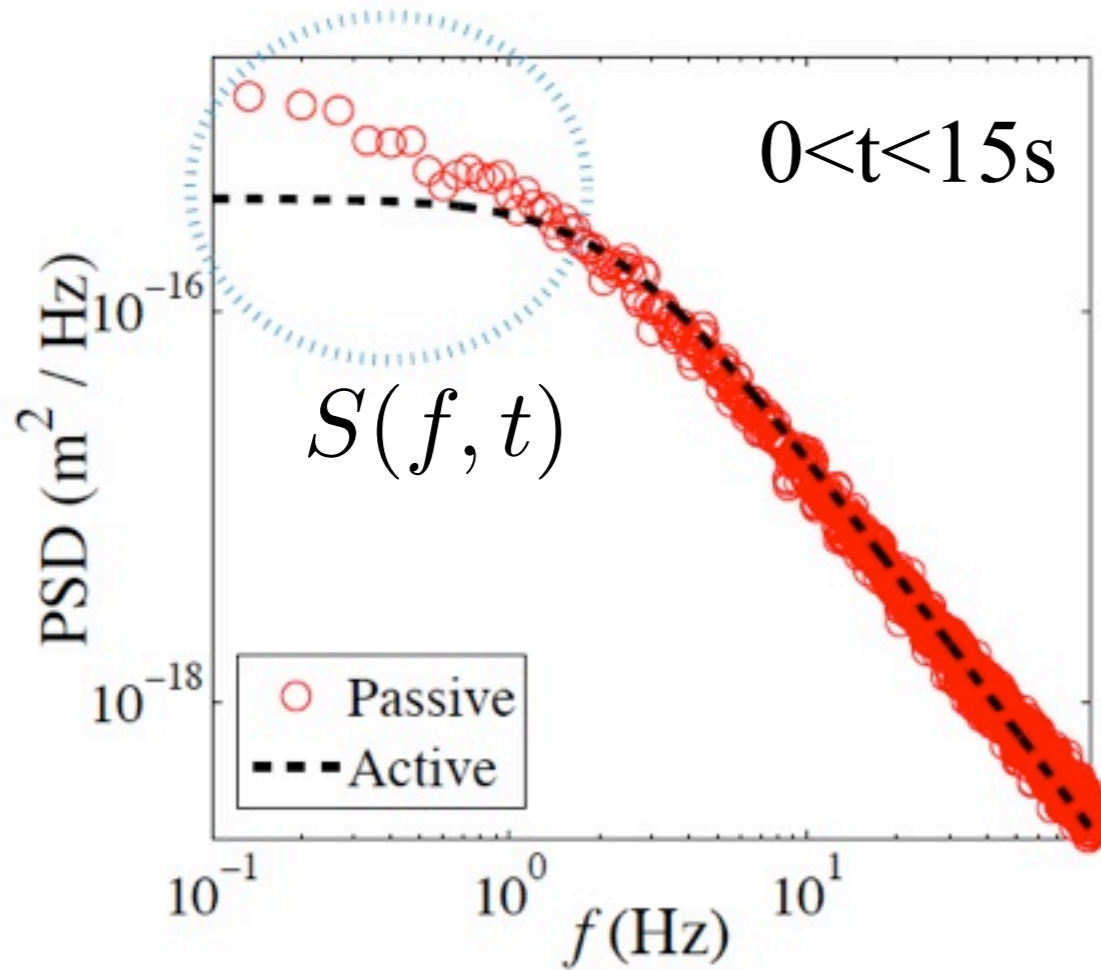




FDT

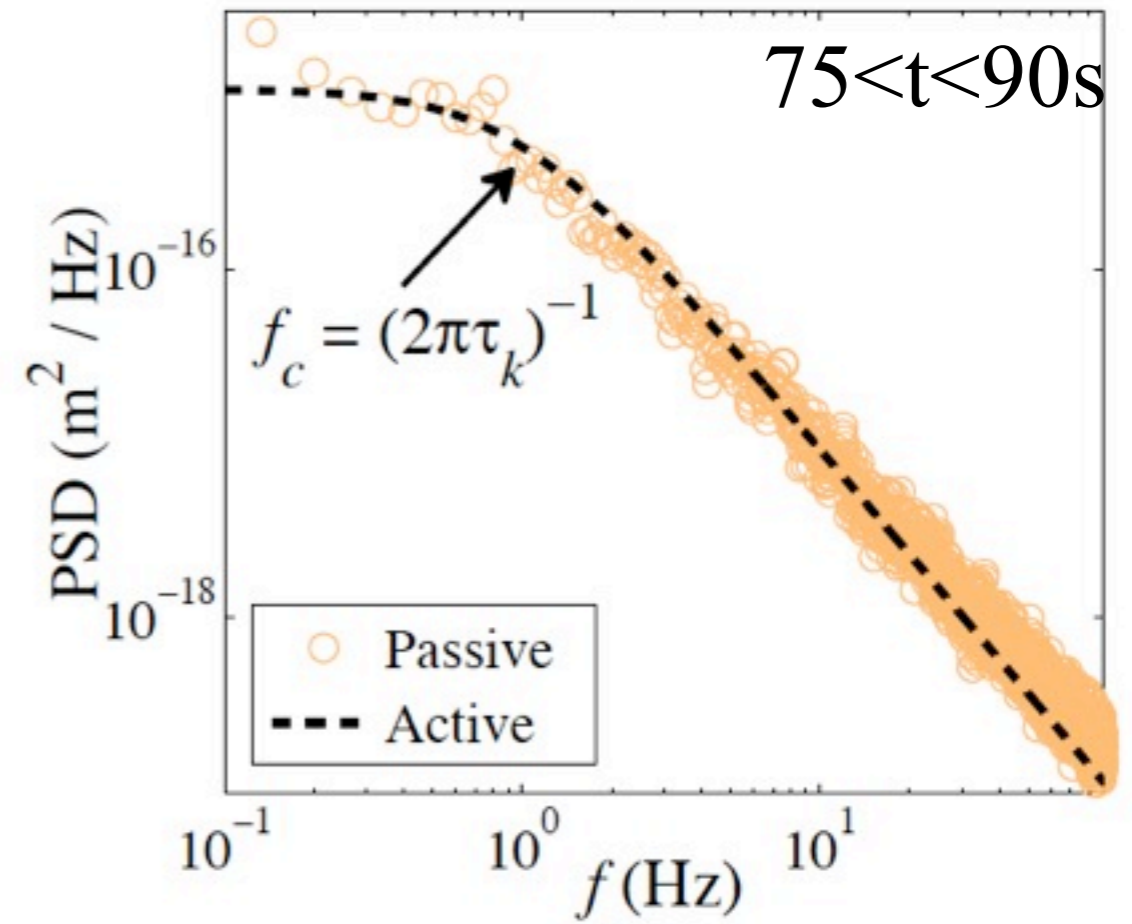
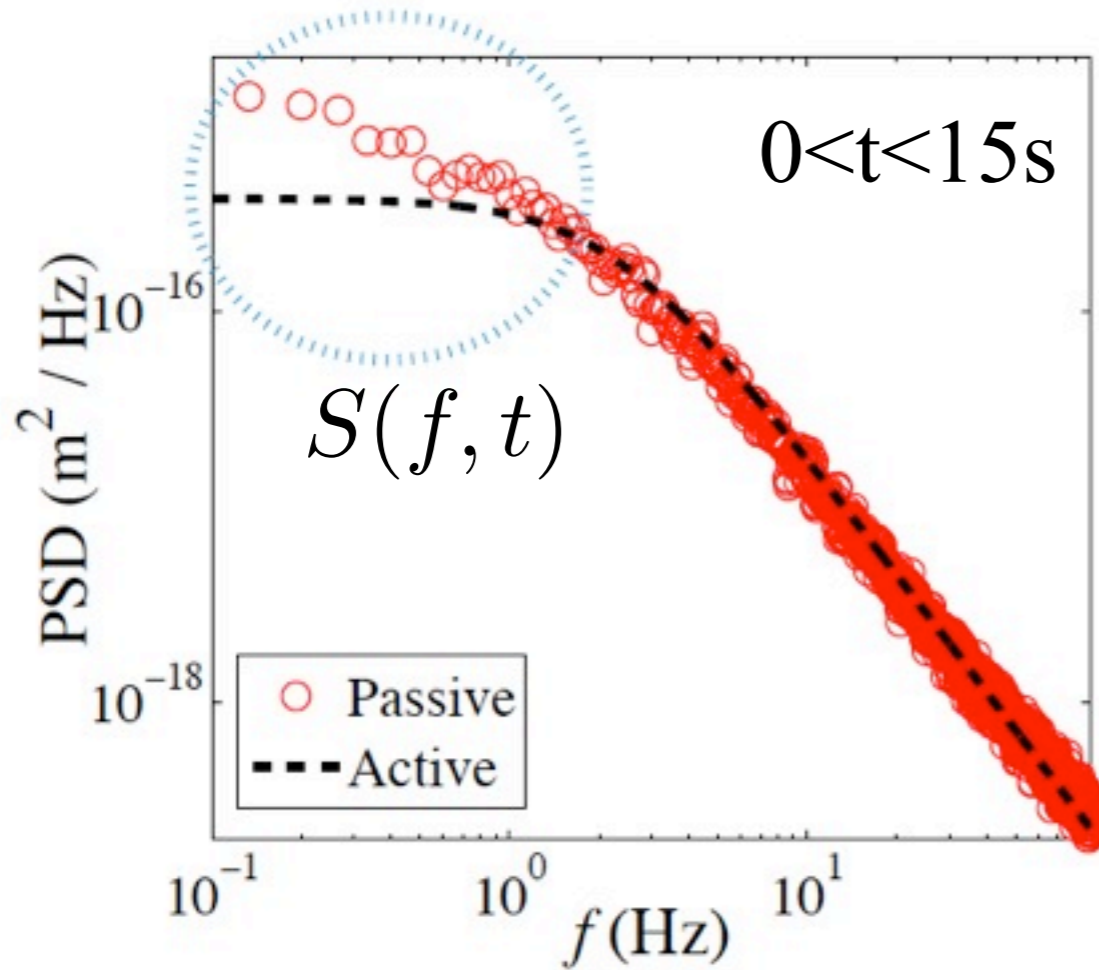
in equilibrium

$$S(f, t) = \frac{2k_B T}{\pi f} \text{Im}[R(f, t)]$$

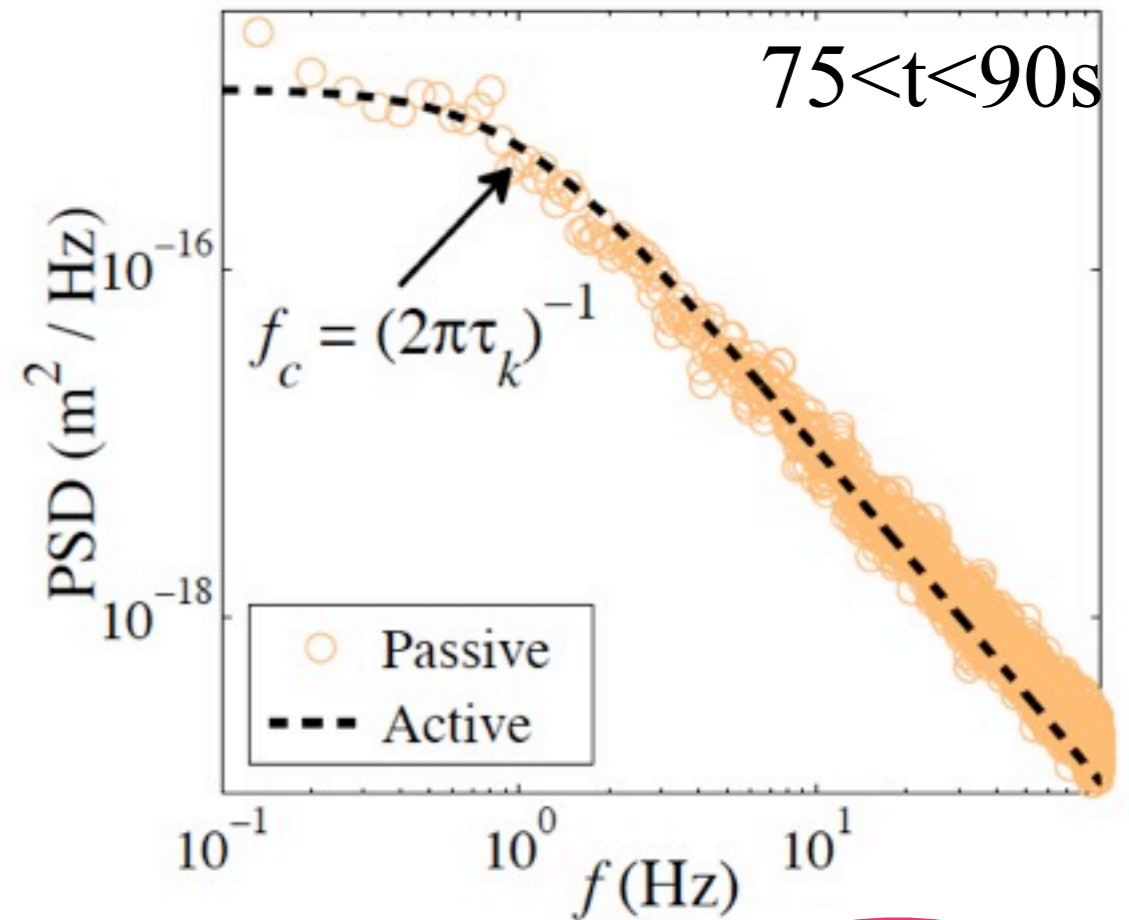
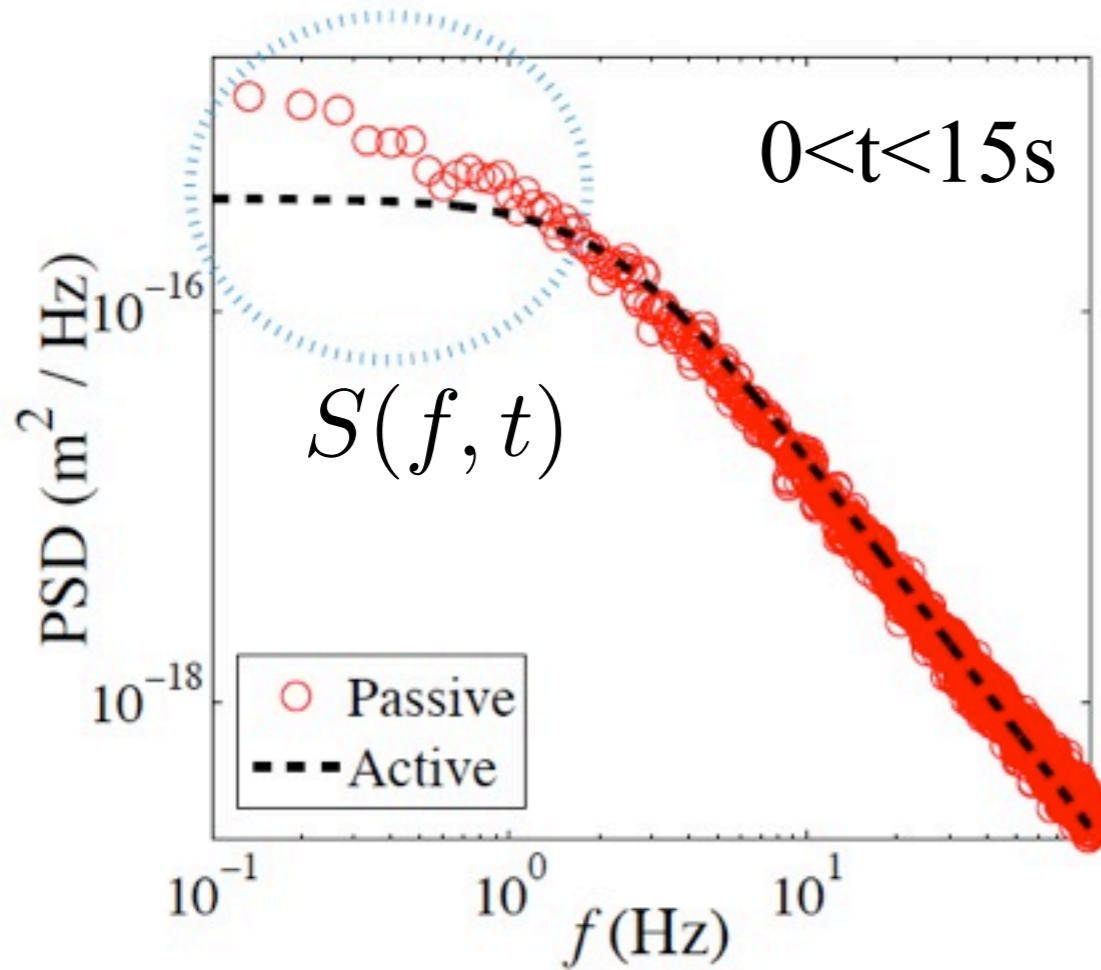


$$S(f, t) \neq \frac{2k_B T}{\pi f} \text{Im}[R(f, t)] \quad \text{out of equilibrium}$$

FDT is violated in our experiment

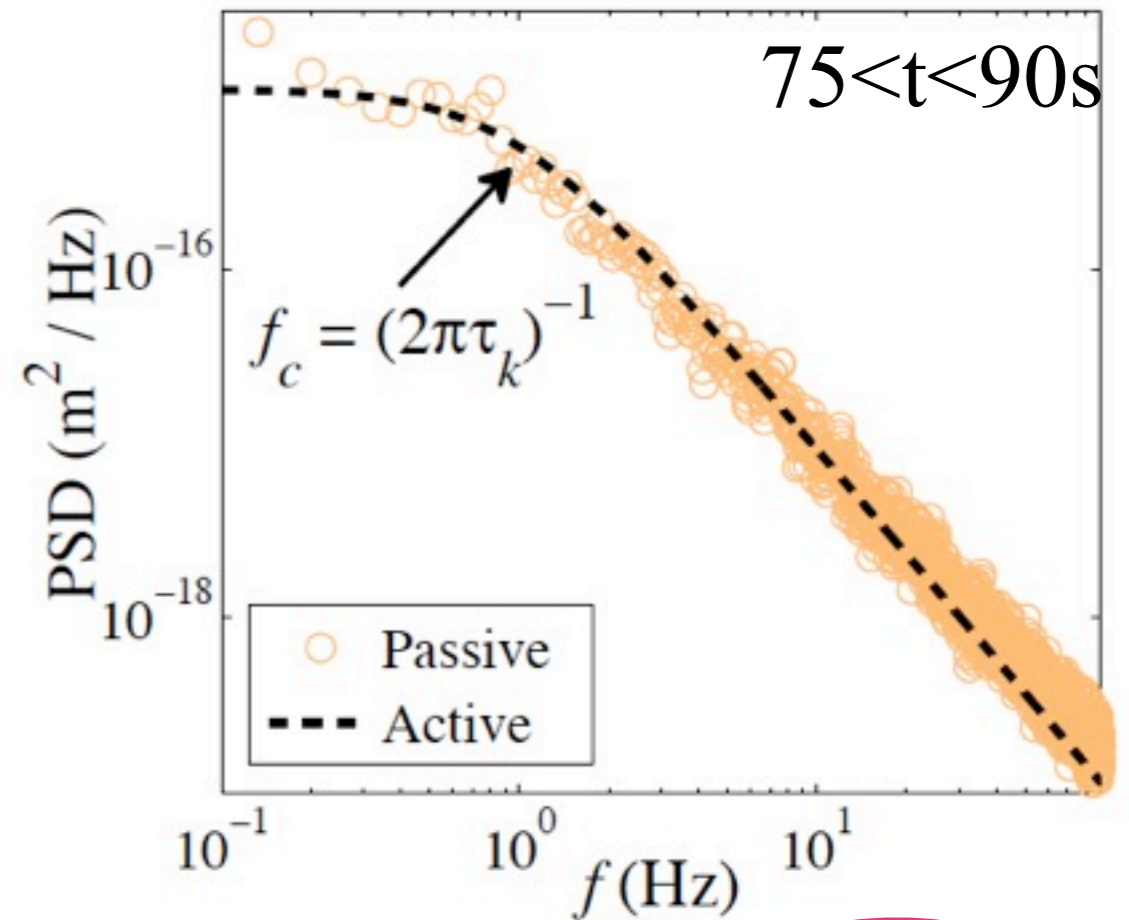
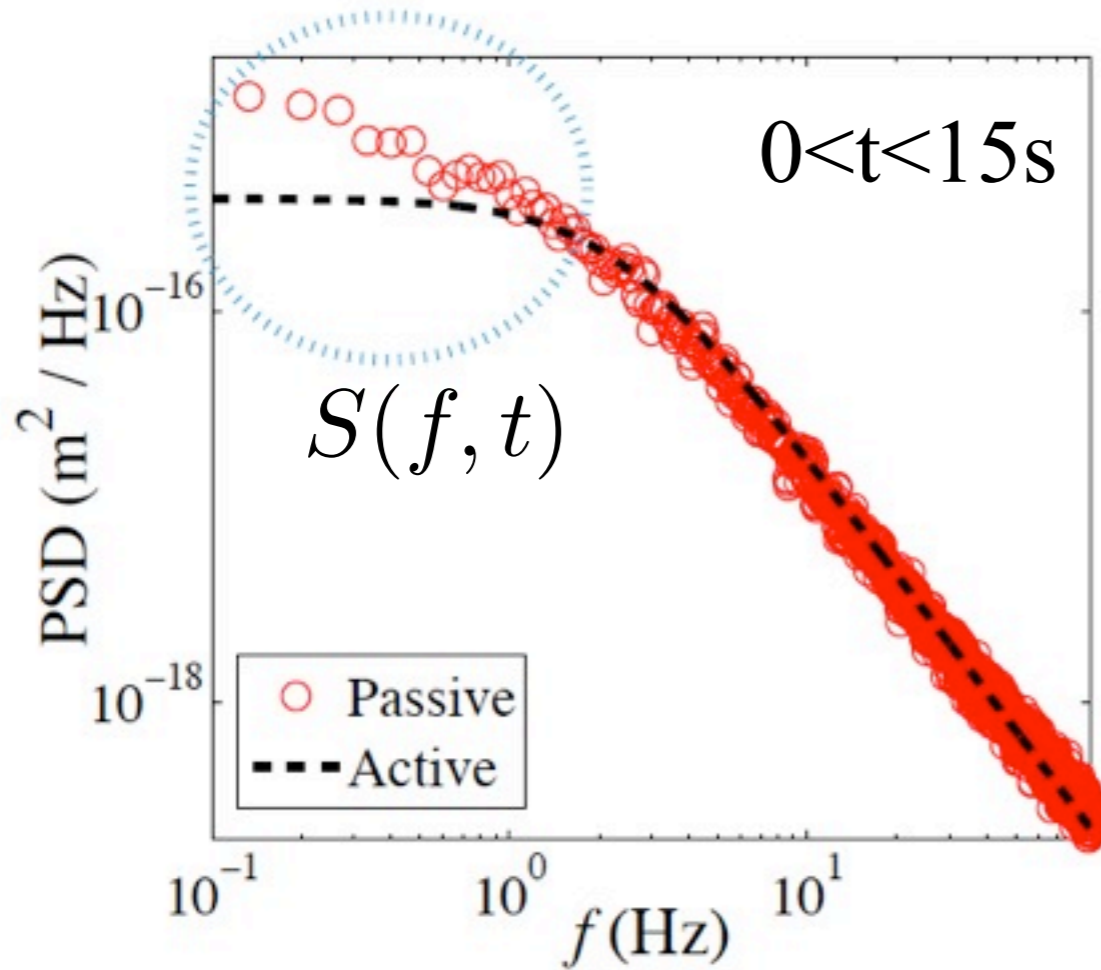


$$\int_0^{\infty} \left[ S(f, t) - \frac{2k_B T}{\pi f} \text{Im}\{R(f, t)\} \right] df = \frac{2\overline{Q}_{t, \Delta t}}{k}$$



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heat dissipated  
in the time  
interval  $[t, t+\Delta t]$



$$\int_0^{\infty} \left[ S(f, t) - \frac{2k_B T}{\pi f} \text{Im}\{R(f, t)\} \right] df = \frac{2\overline{Q}_{t, \Delta t}}{k}$$

As in the generalized FDT for NESS the extra additive term is related to the heat flux.

(Chetrite, Gawedzki, Seifert Speck, Maes, Lipiello, Corberi)

heat dissipated in the time interval  $[t, t+\Delta t]$

## Conclusions

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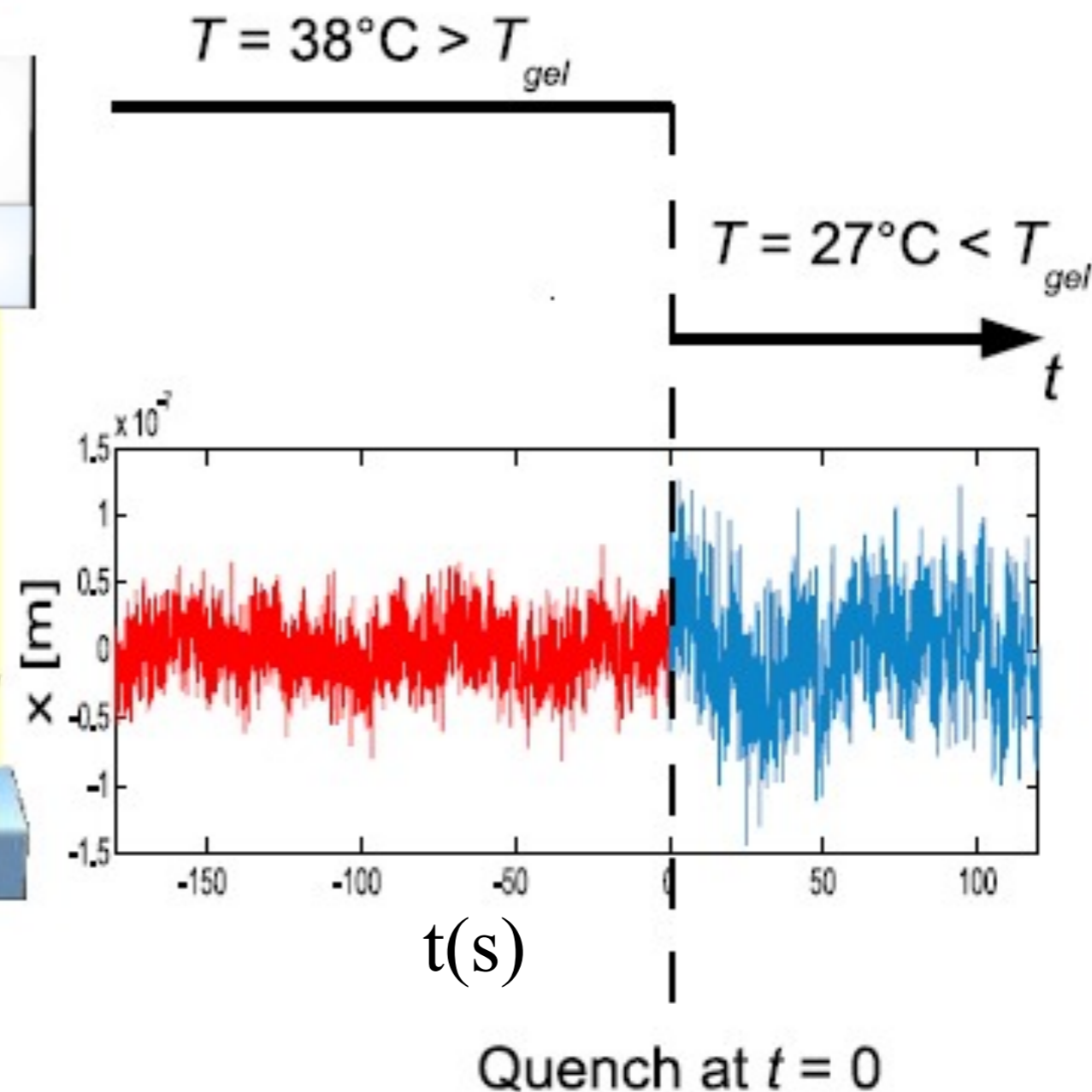
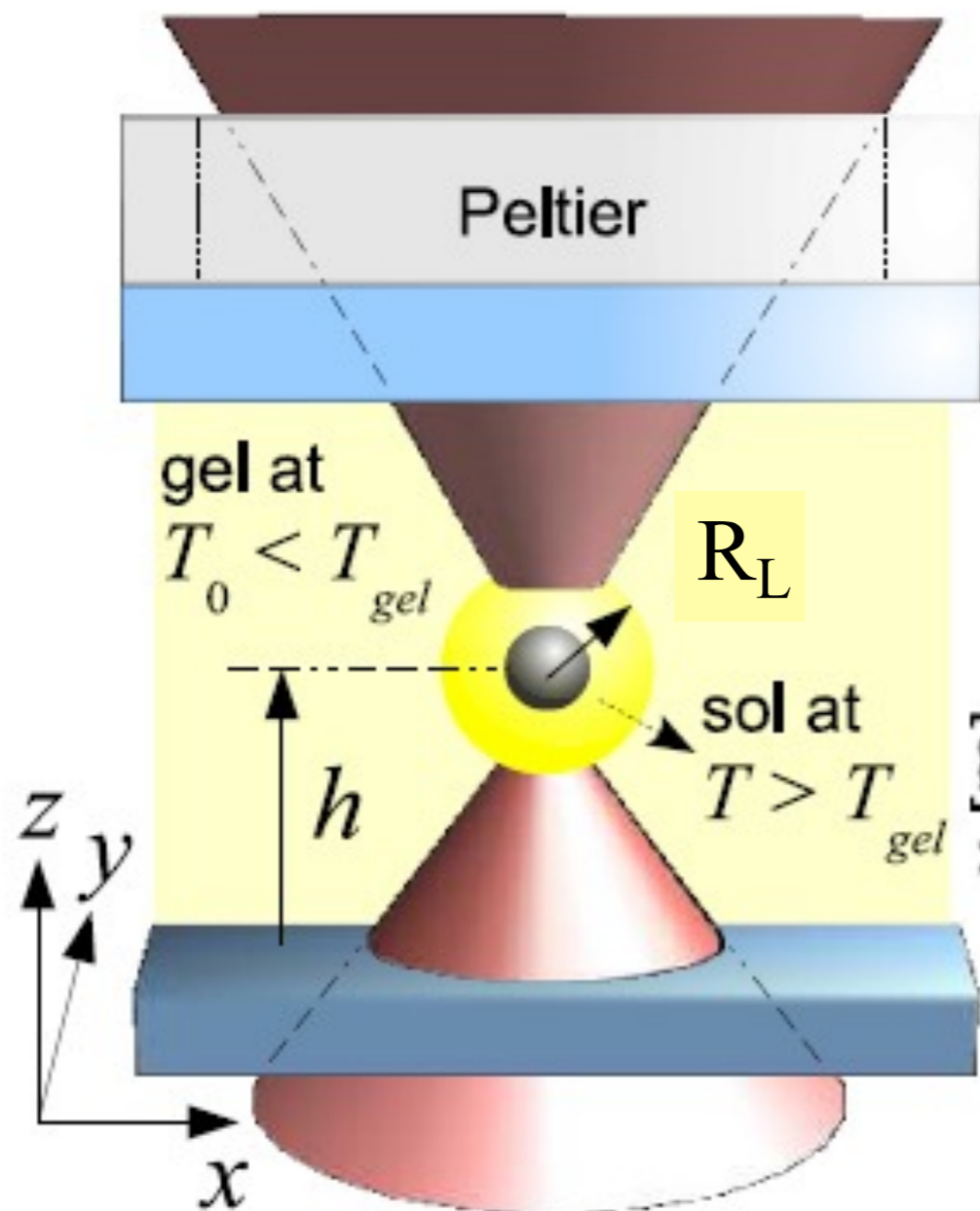


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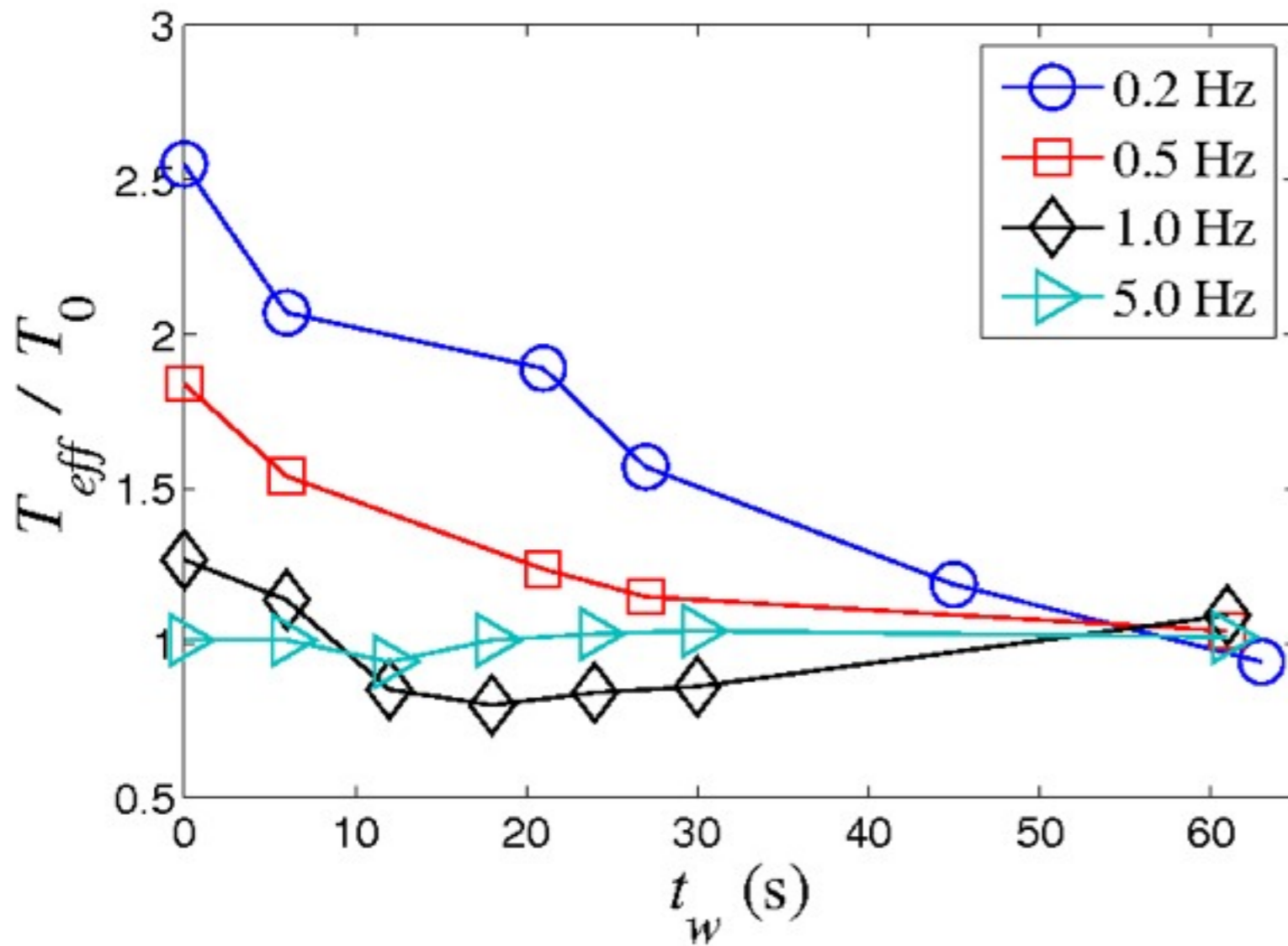
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- a) The fluctuations of heat are asymmetric, i.e. the dynamics transfer heat towards the bath
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- c) The Fluctuation Dissipation Theorem is violated.  
The amount of the violation is related to the heat flux as for the Generalized FDT for NESS.

- ▶ Fast quench of the droplet to  $T = 27^\circ \text{C} < T_{gel}$  by decreasing the laser power: heat diffusion into the gel bulk in  $\sim 1 \text{ ms}$ .





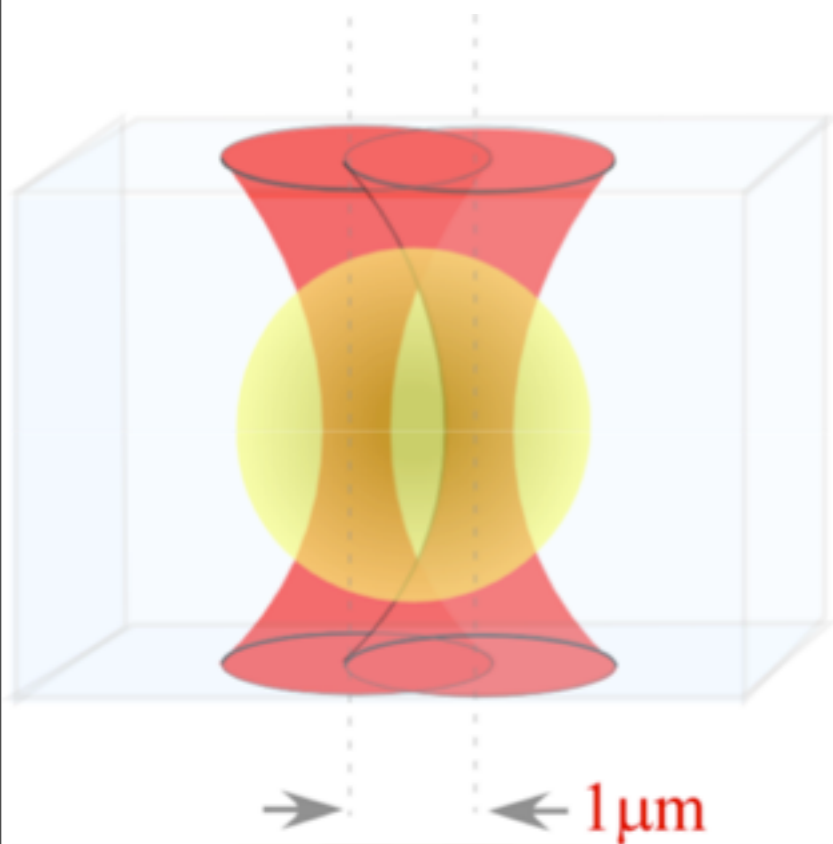


Experiment in gelatine  
at 10%wt  
sol-gel transition at 28°C

## The stochastic resonance and Fluctuation Theorem

P.Jop, A. Petrosian, S. Ciliberto, Eur. Phys. Lett. **81**, 50005 (2008)

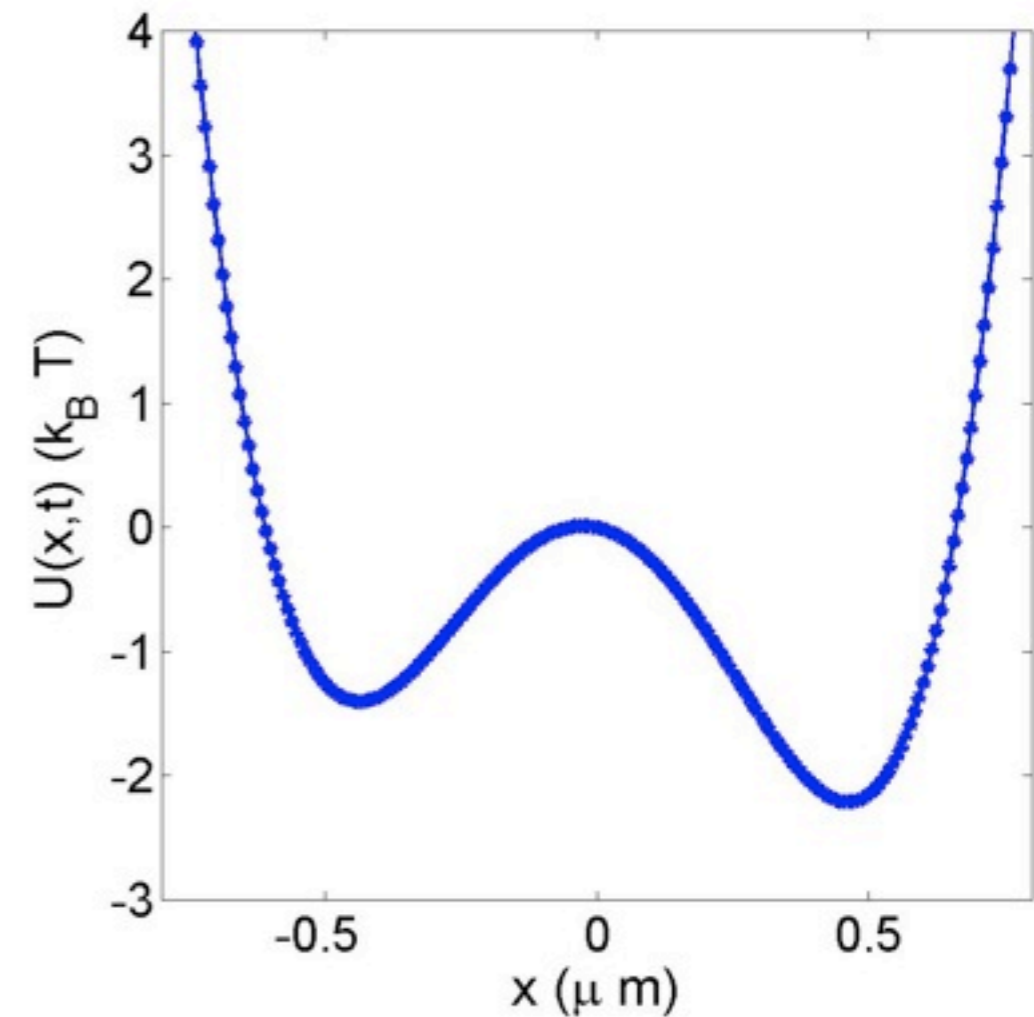
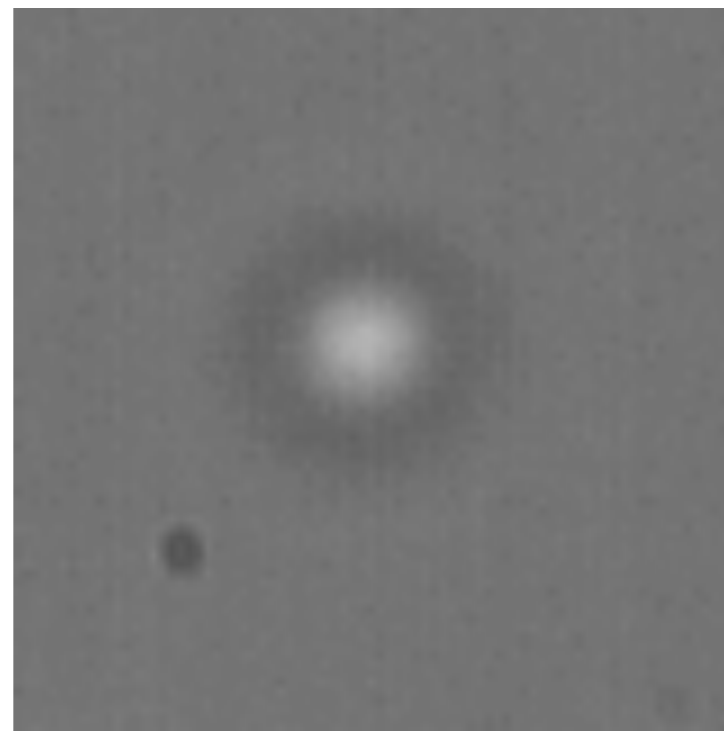
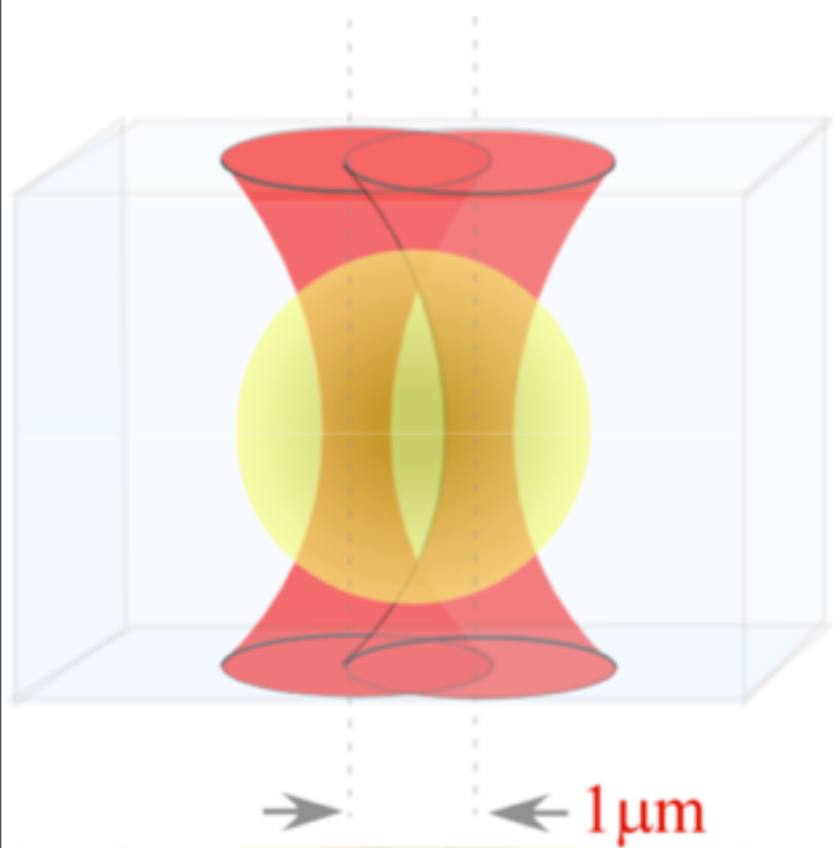
### Brownian particle trapped by two laser beams



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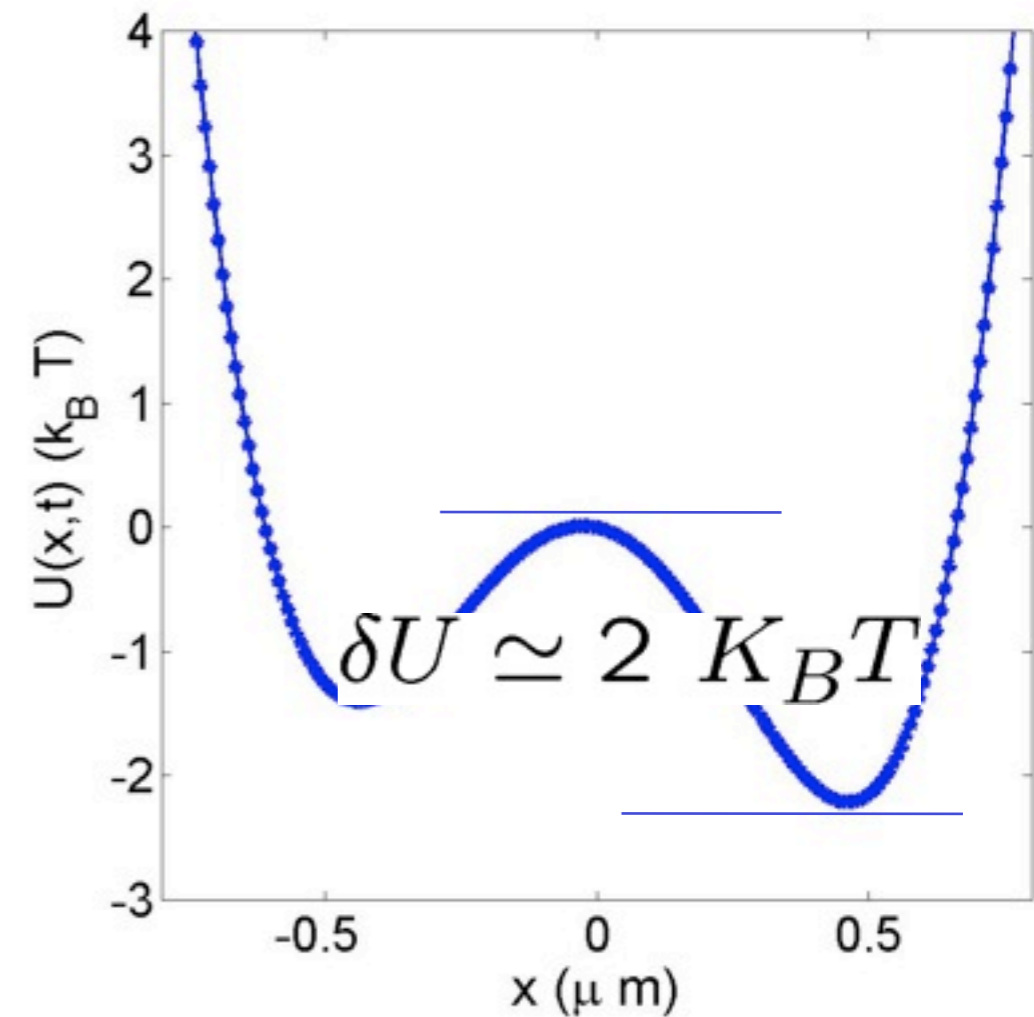
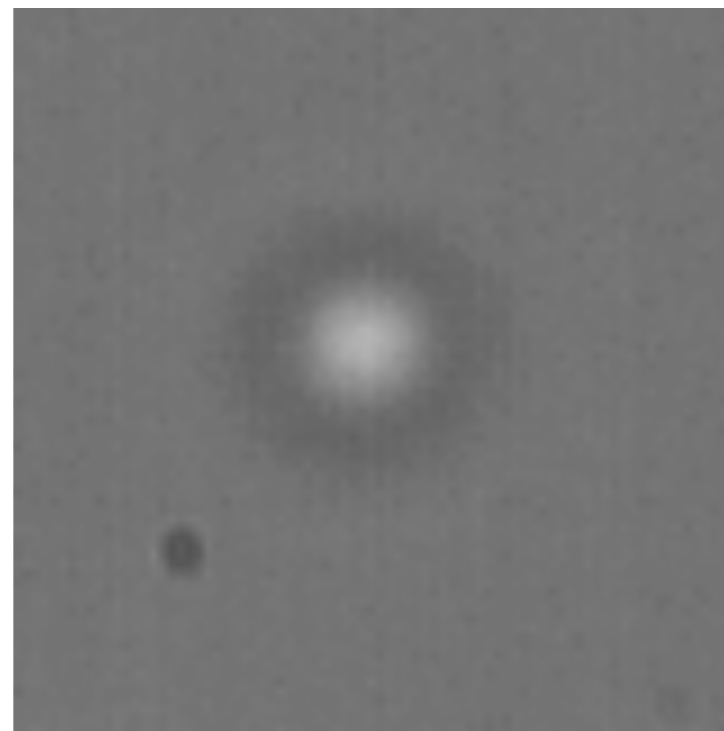
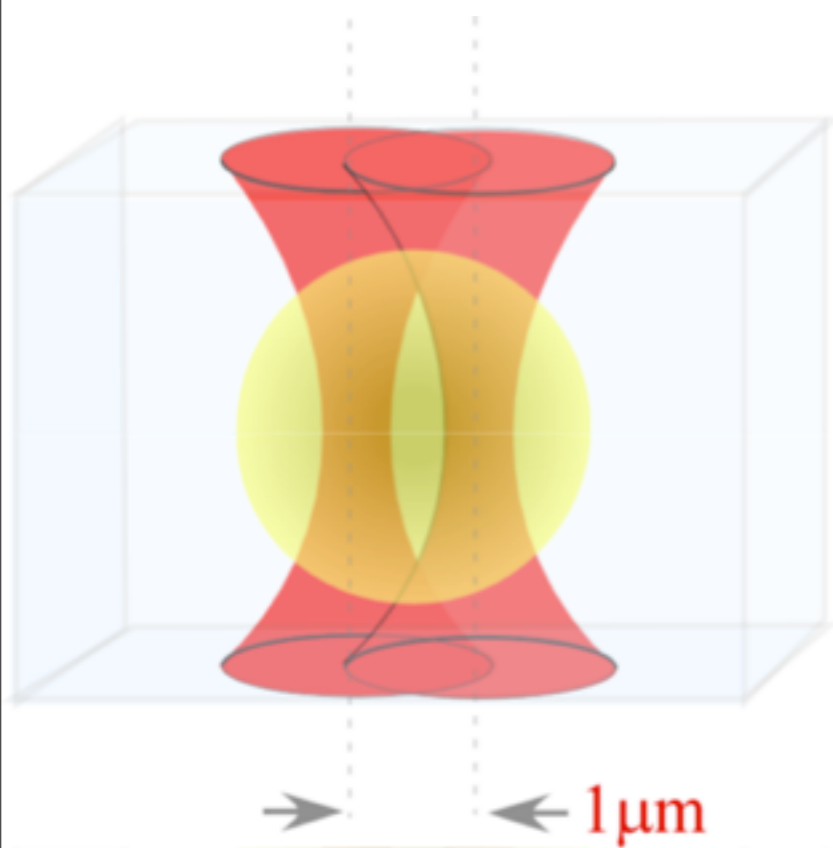


$$U_0(x) = ax^4 - bx^2 - dx$$

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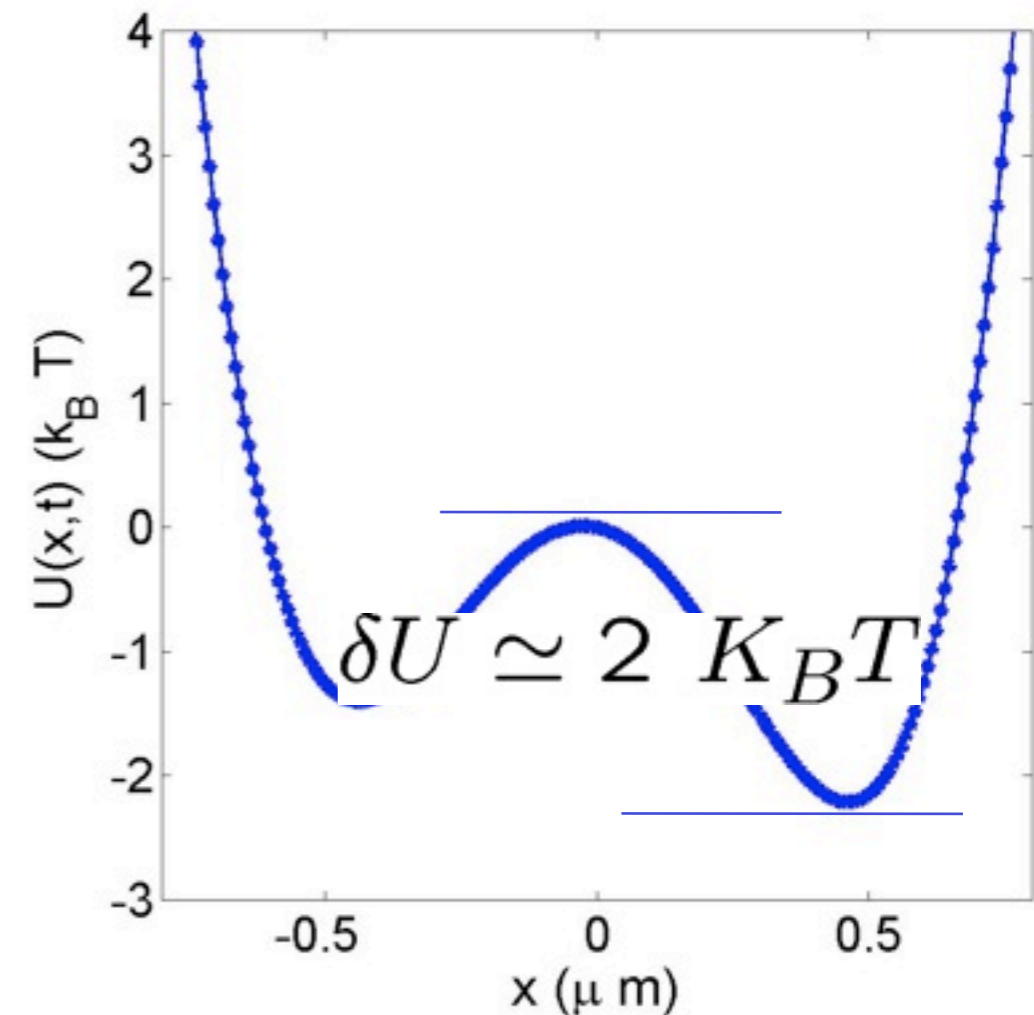
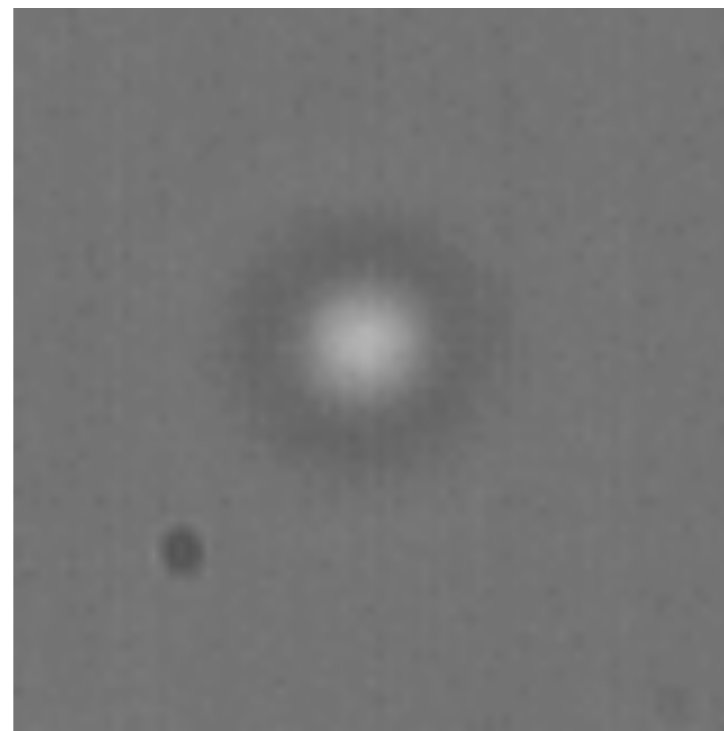
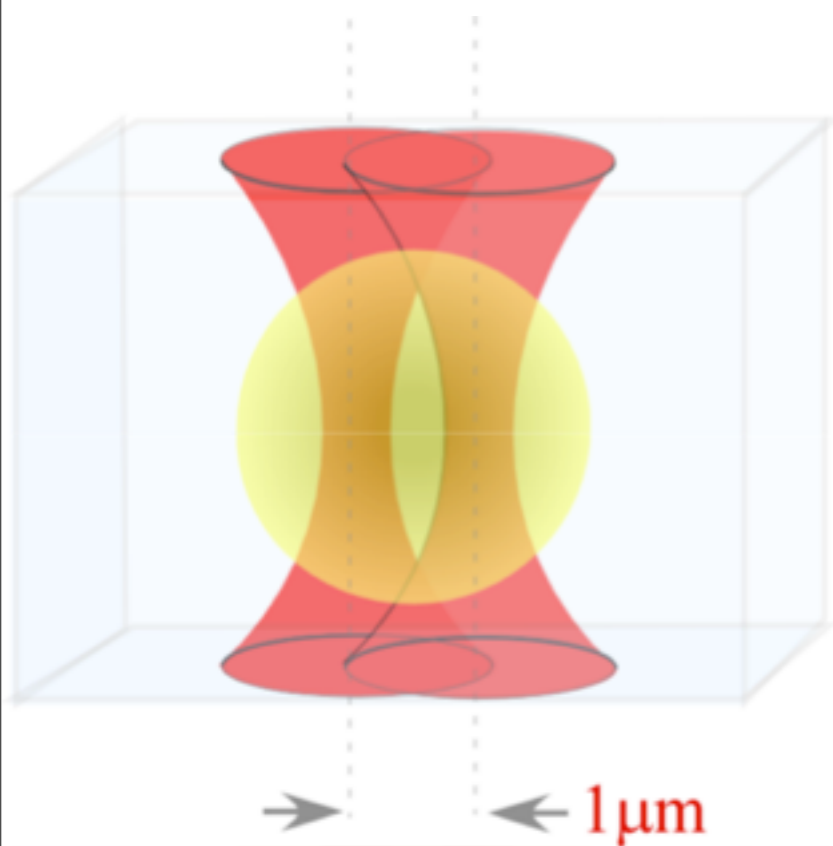


$$U_0(x) = ax^4 - bx^2 - dx$$

# The stochastic resonance and Fluctuation Theorem

P.Jop, A. Petrosian, S. Ciliberto, Eur. Phys. Lett. **81**, 50005 (2008)

## Brownian particle trapped by two laser beams



The Kramer rate is

$$r_k = \tau_0^{-1} \exp\left(-\frac{\delta U}{k_B T}\right)$$

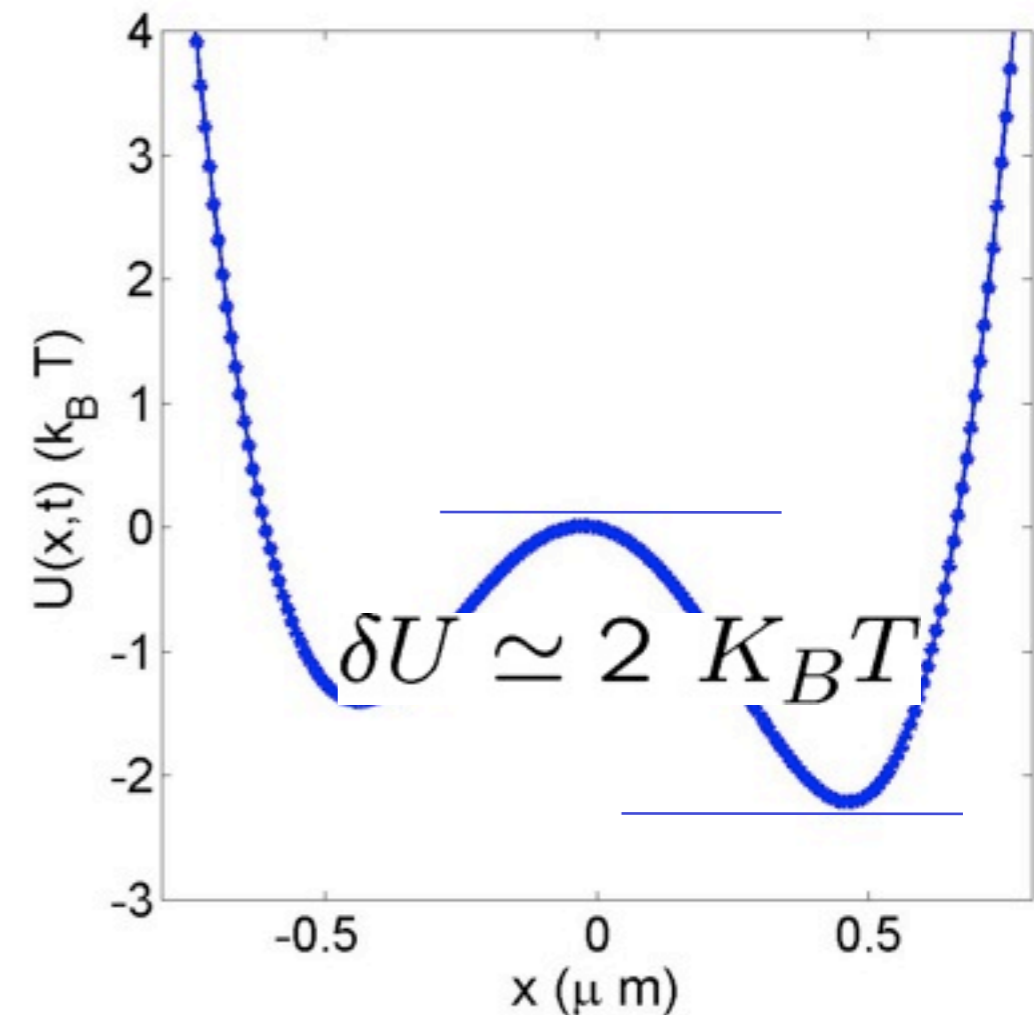
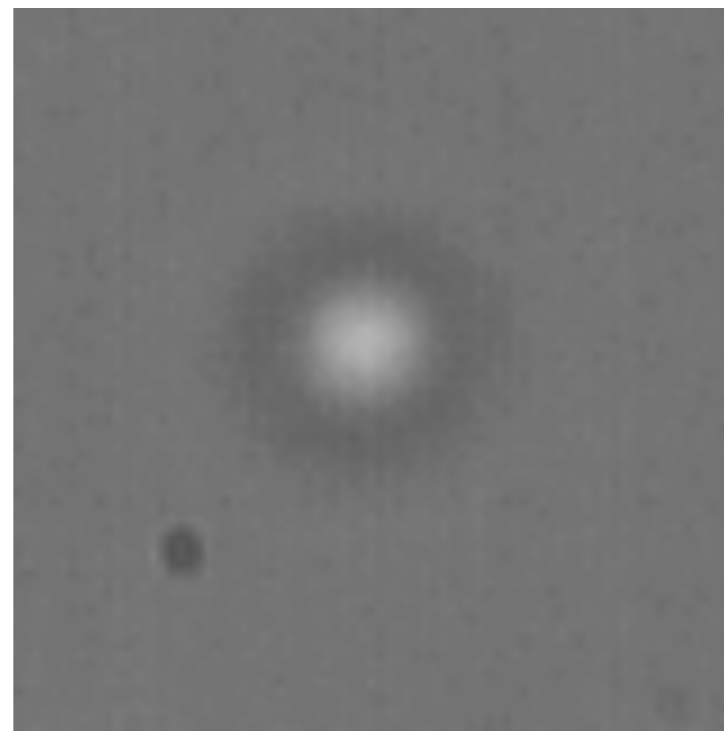
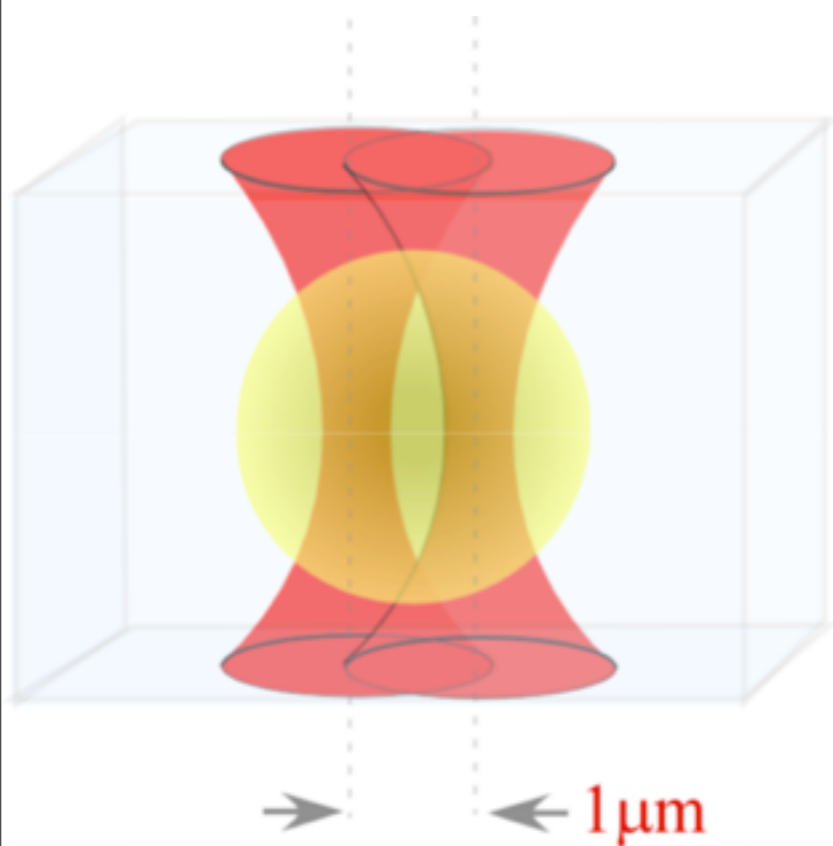
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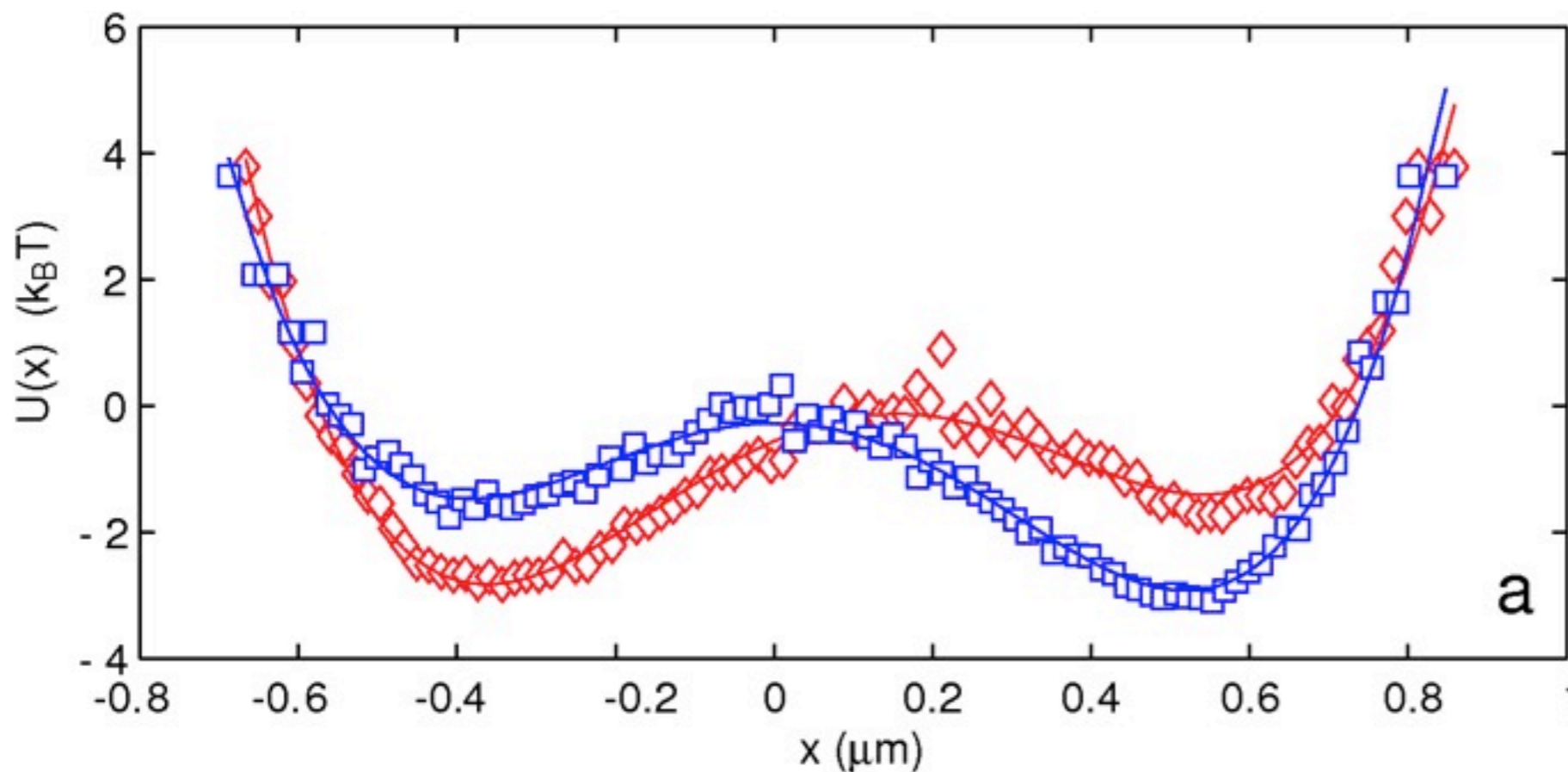
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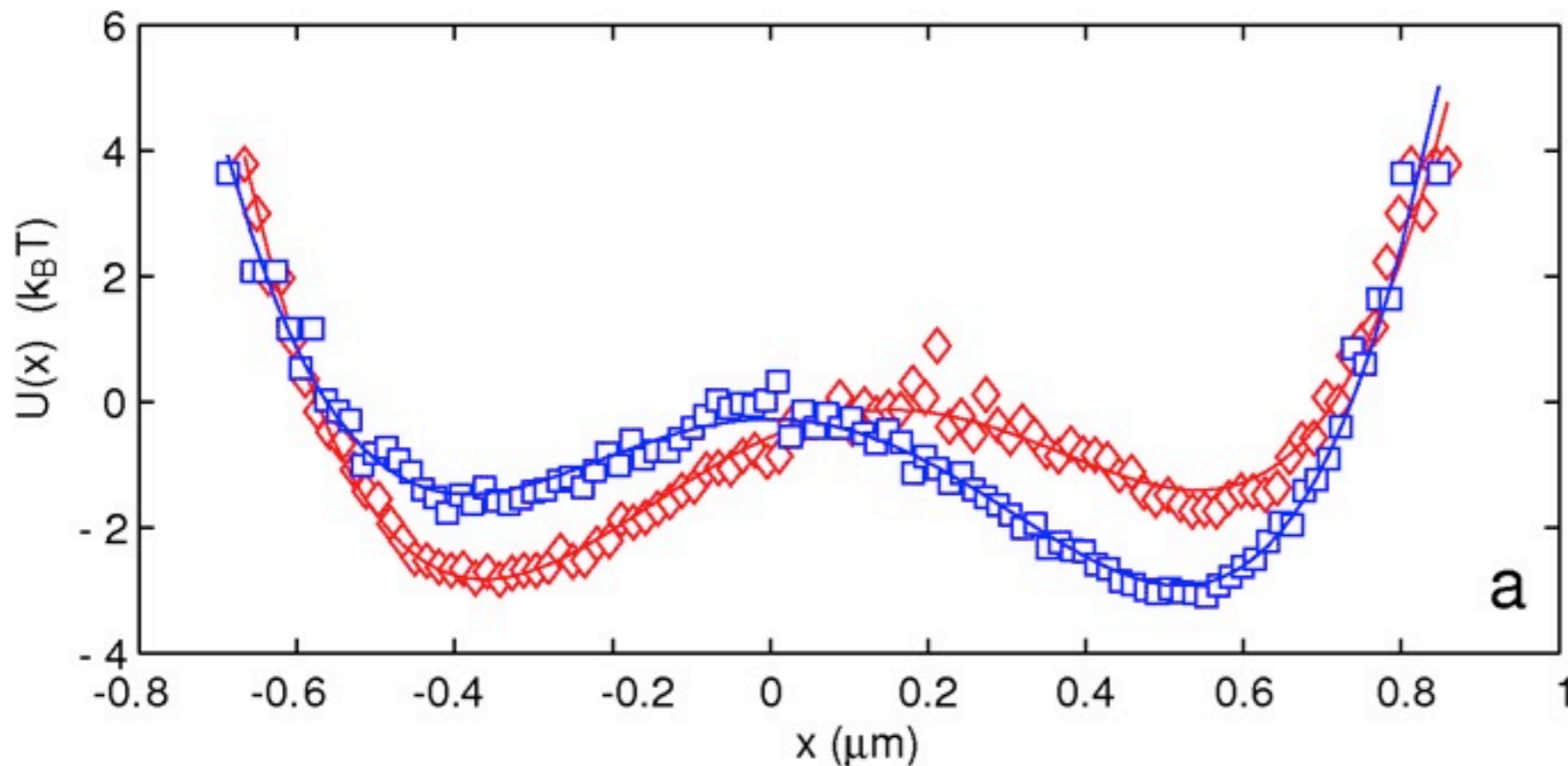
Kramer rate  
 $r_k = \tau_0^{-1} \exp\left(-\frac{\delta U}{k_B T}\right)$

$$U_0(x) = ax^4 - bx^2 - dx$$

$$U(x, t) = U_0(x) + U_p(x, t) = U_0 + cx \sin(2\pi ft),$$

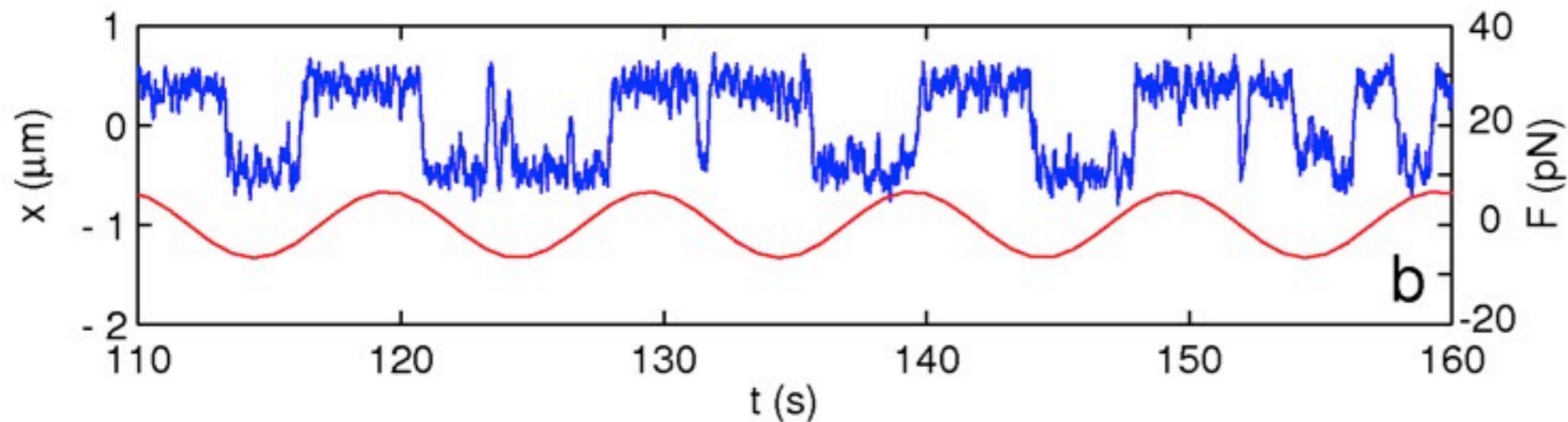
$$\nu \dot{x} = -\frac{\partial U_0(x)}{\partial x} - c \sin(2\pi ft) + \eta$$

# The non linear potential



Kramer rate  

$$r_k = \tau_o^{-1} \exp\left(-\frac{\delta U}{k_B T}\right)$$



$f=0.1\text{Hz}$

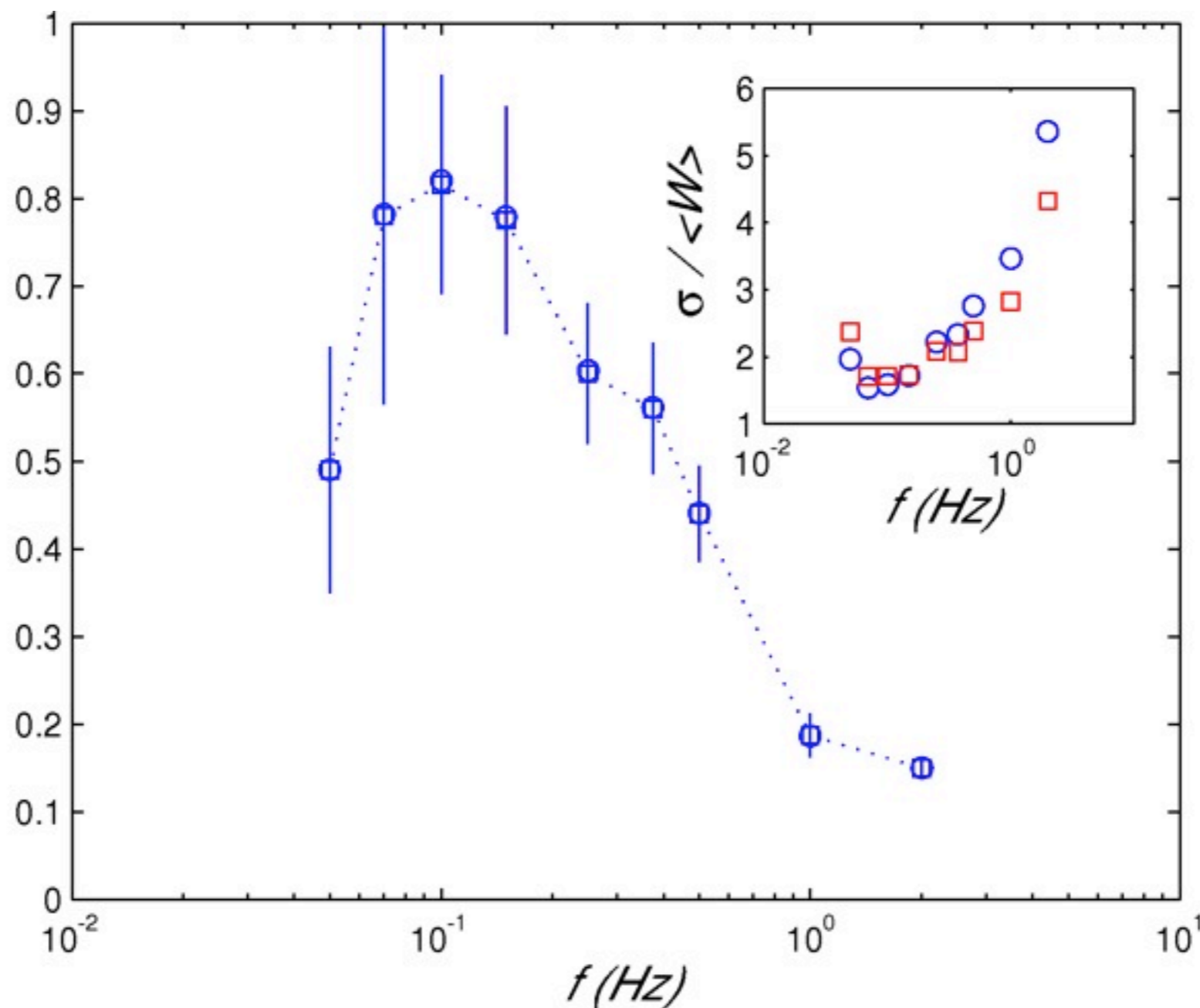
At  $f \simeq r_k$  the hops of the particle synchronise with the external forcing

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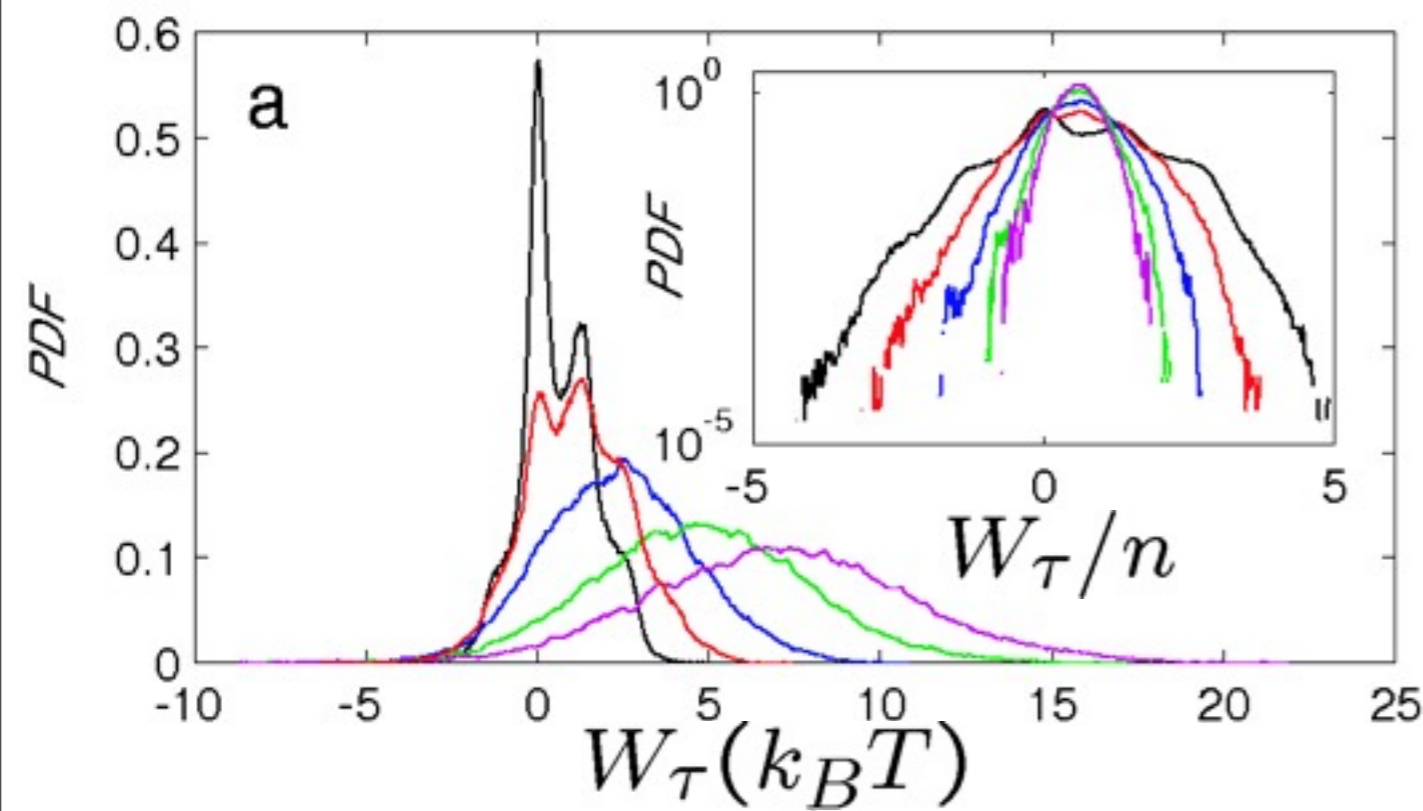
$$W_\tau = c \int_{t_i}^{t_i + \tau_n} \dot{x} \sin(2\pi ft) dt \quad \text{with } \tau_n = n/f$$

$$\langle W_\tau \rangle$$

$$n = 1$$

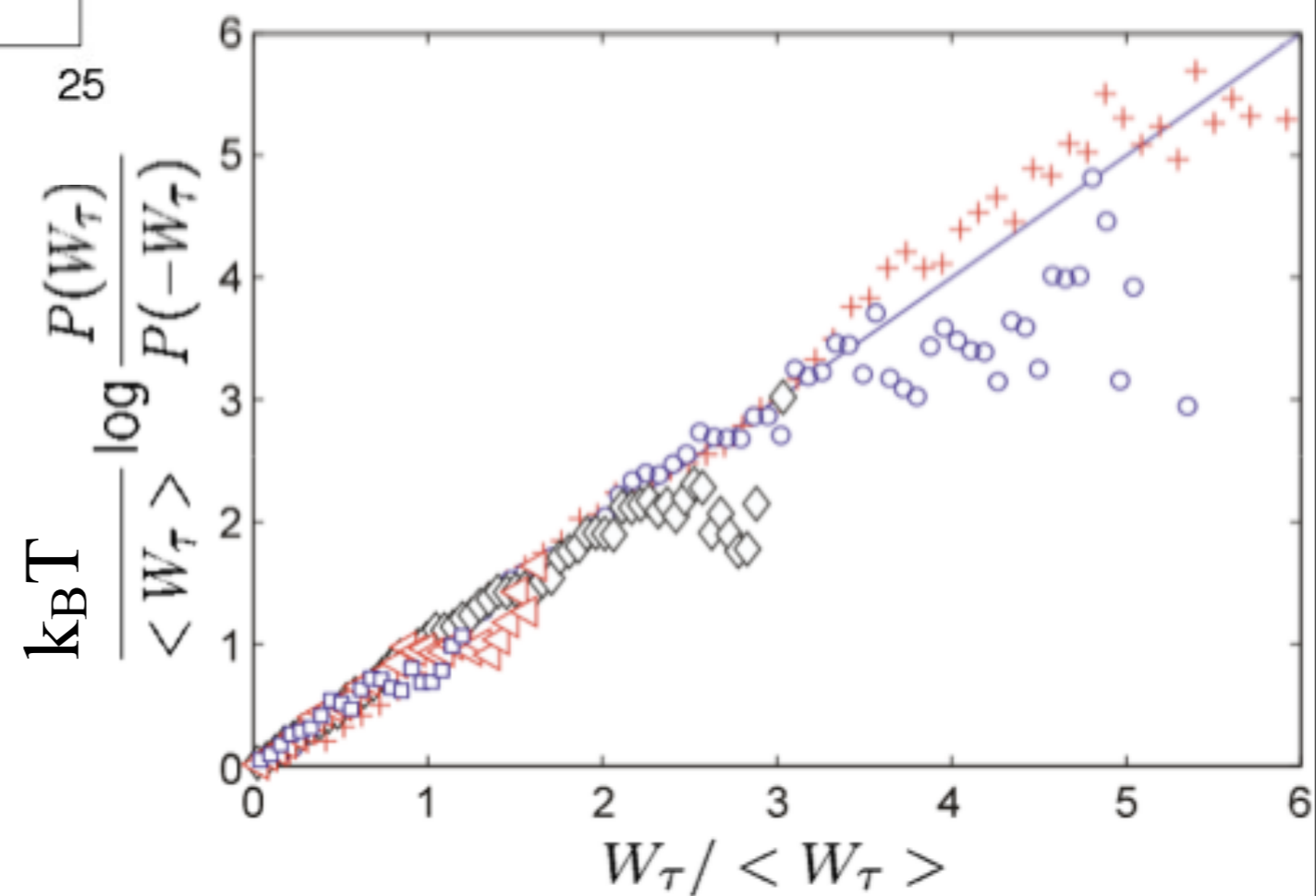


$f=0.25\text{Hz}$  and  $\tau = n / f$

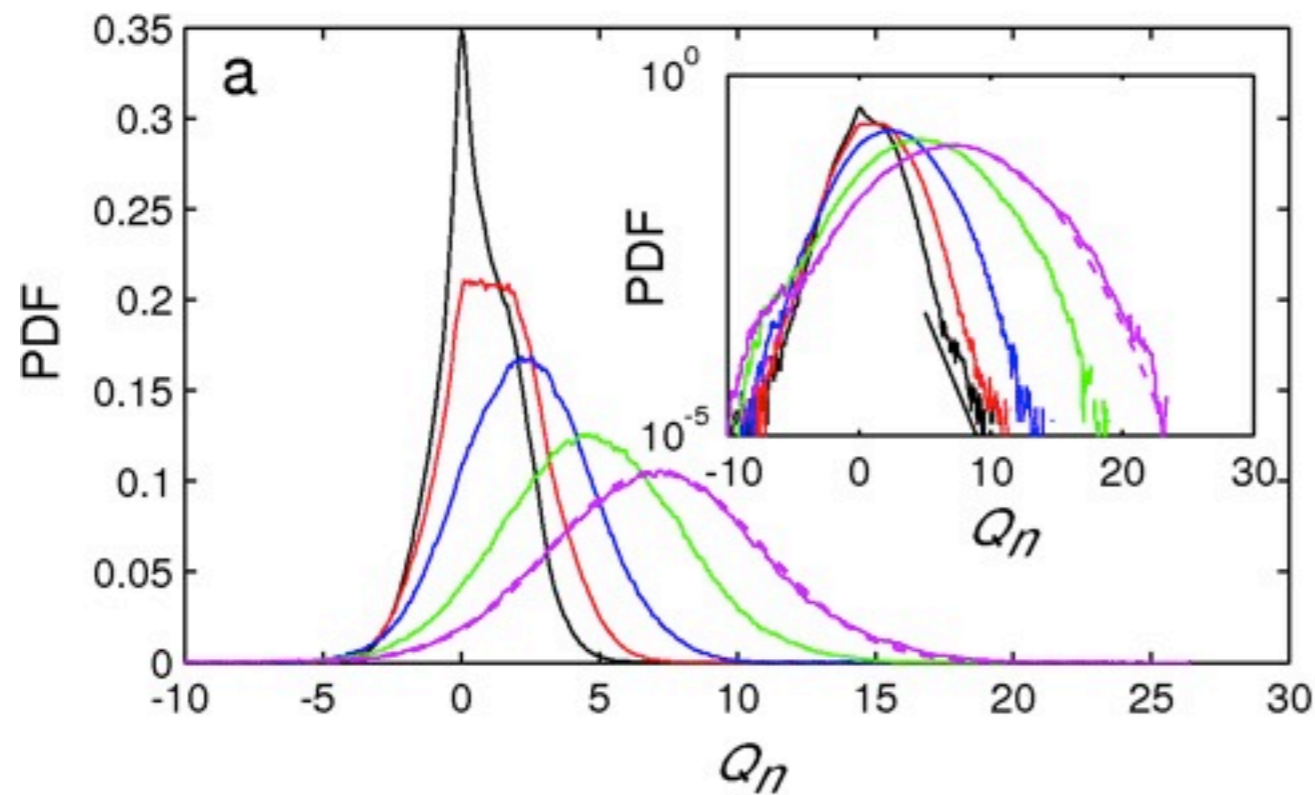


$n = 1, 4, 8$  and  $12$

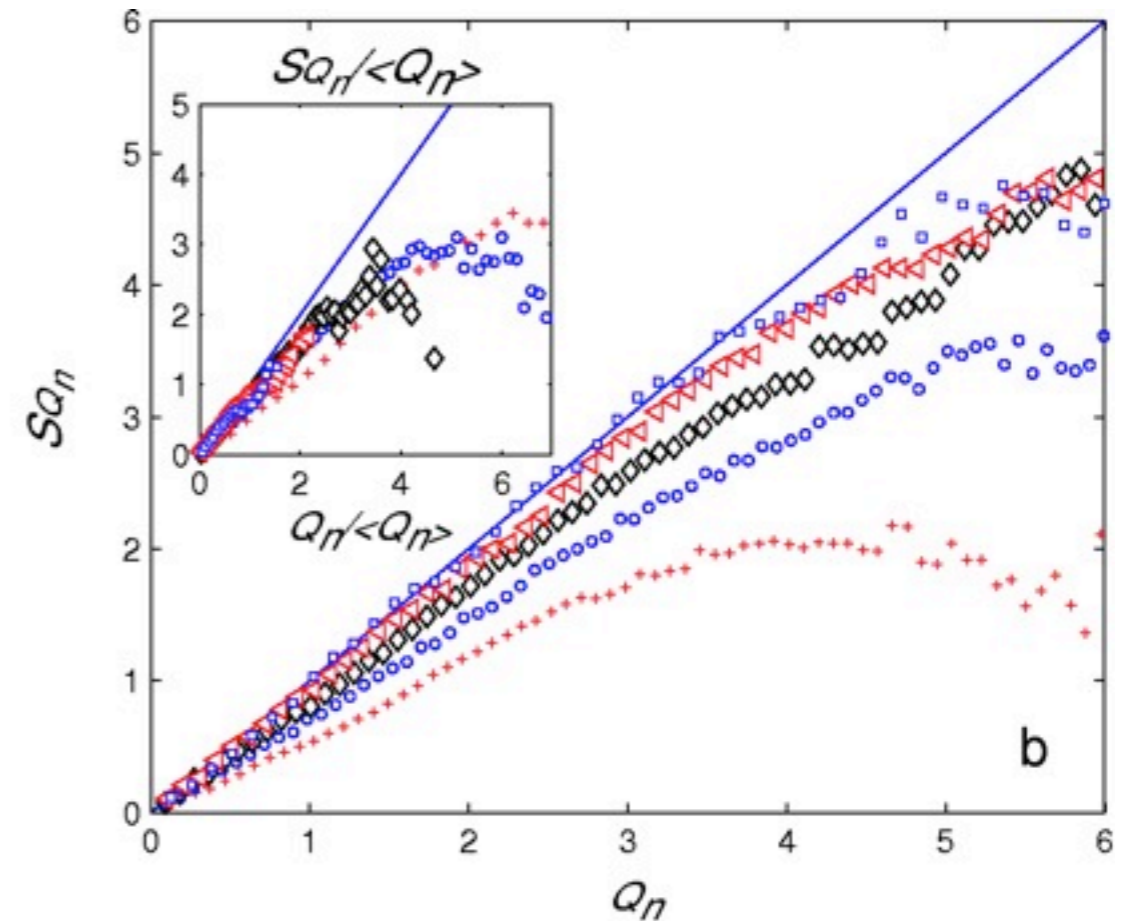
$n = 1$  (+),  $2$  (o),  $4$  (diamond),  
 $8$  (triangle),  $12$  (square)



$$Q_T = -\Delta U_{0,T} + W_T$$



$n = 1, 4, 8 \text{ and } 12$



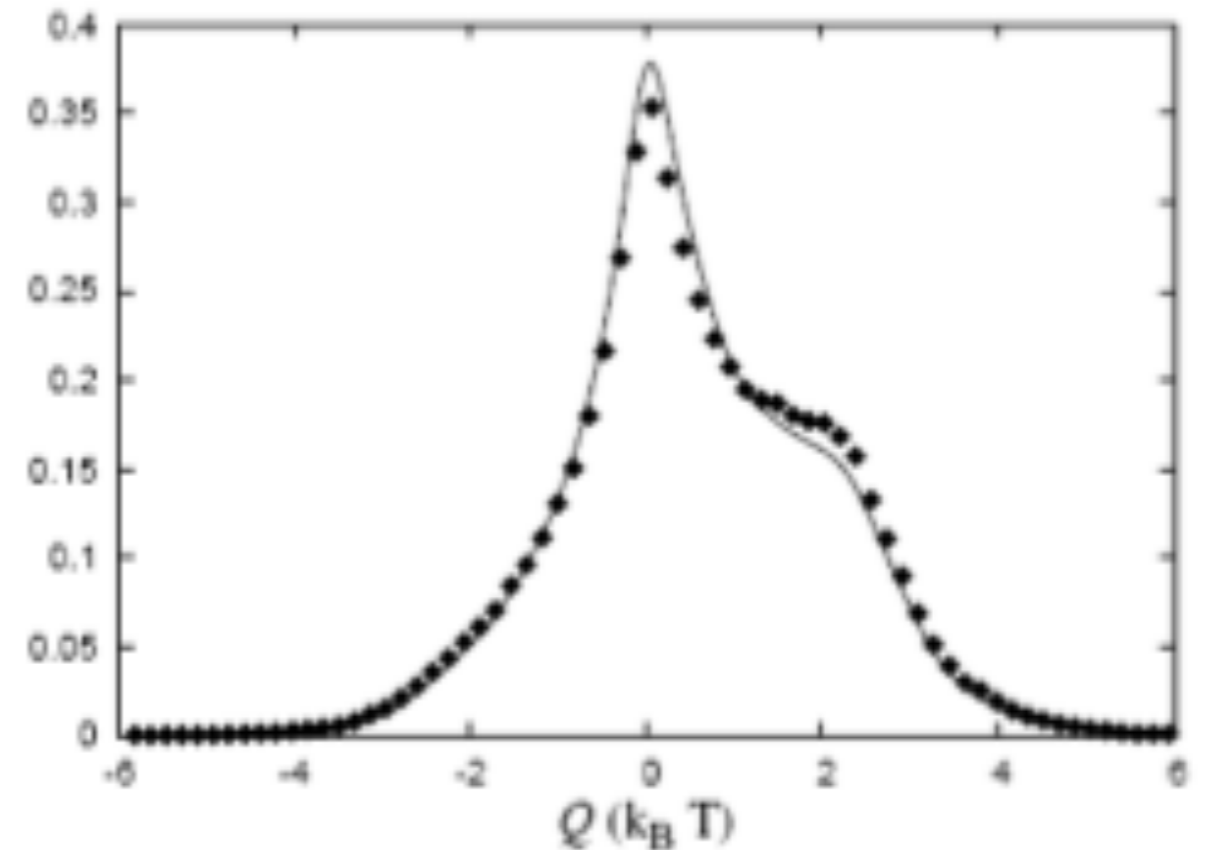
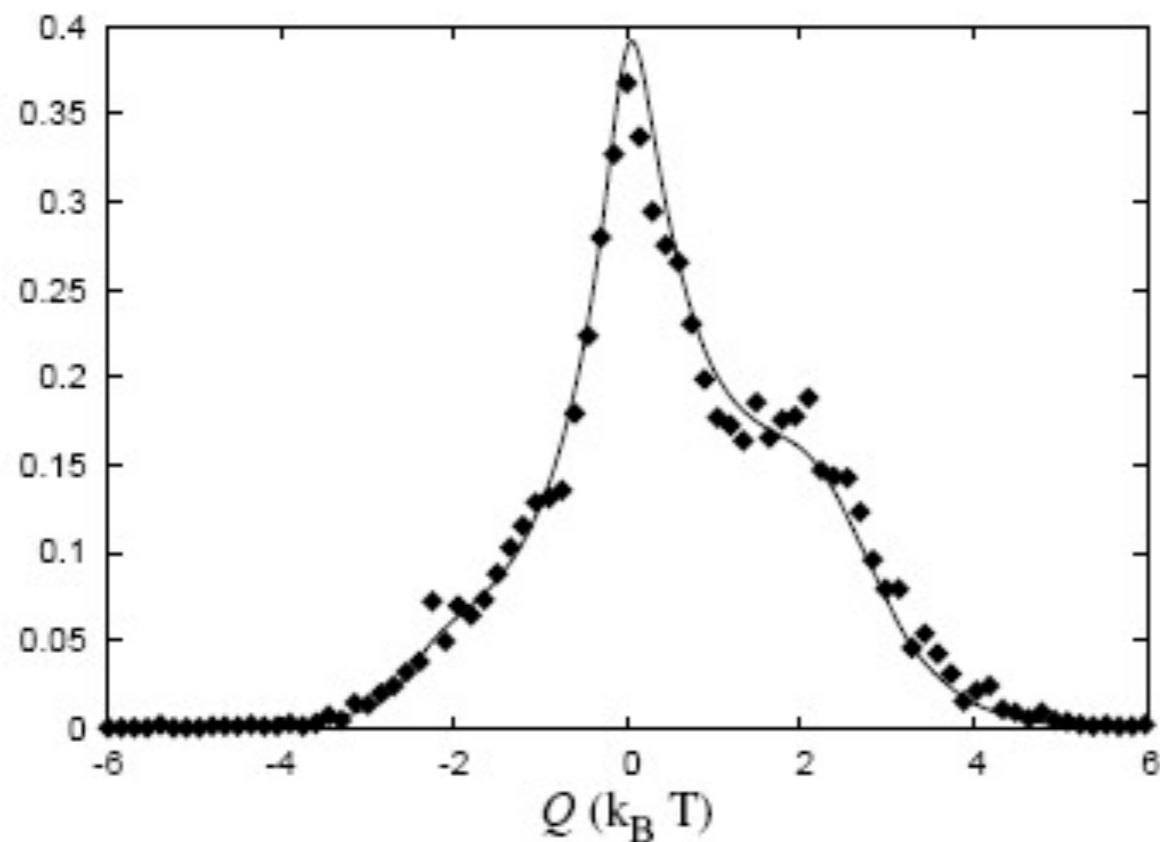
$n = 1 (+), 2 (o), 4 (\diamond), 8 (\triangle), 12 (\square)$

A. Imparato, P. Jop, A. Petrosyan and S. Ciliberto, J. Stat. Mech. (2008) P10017

## PDF of the heat computed on a single period :

(initial phase=0)

(averaged over different initial phases)



Experimental data



Theoretical prediction based on Fokker-Planck equation

## Conclusions on FT (partial)

- We have studied the energy fluctuations of a harmonic oscillator driven out of equilibrium by an external force.
- We have measured the **finite time corrections** for **SSFT** and compared to the theoretical predictions. **TFT** is instead verified for all times.
- The “**trajectory dependent entropy**” has been measured and we checked that **SSFT** is verified for all times for the “**total entropy**”.
- We have shown that in this specific example the “**total entropy**” takes into account only the entropy produced by the external driving, without the **entropy fluctuations at equilibrium**.
- We have applied also **SSFT** to the strongly non-linear case of the **stochastic resonance**